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# GENERAL TREND AND LOCAL VARIATIONS OF NEUTRON RESONANCE CASCADE GAMMA-DECAY RADIATIVE STRENGTH FUNCTIONS

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# Introduction

- Obtain accurate experimental values of **the level density and radiative strength functions is necessary.**
- **It is necessary to develop the method for determination of  $\rho$  and  $\Gamma$**
- Main problem : **FWHM  $\gg D_i$**
- Two-step gamma cascade method
  
- Dependence form of the radiative strength functions (RSF) of electric and magnetic dipole gamma-transitions in heated nucleus on the excited level density
- New hypothesis: modified dependence of RSF on level density
  
- **The region of possible values of random values of the level density and radiative strength functions which precisely reproduced experimental intensity of two-step cascades for 41 nuclei from  $^{40}\text{K}$  to  $^{200}\text{Hg}$  was determined.**

# 1. Status of modern experiments for determination of radiative strength functions and the level density

## □ a) One – step reaction

$$I_1 \propto \rho\Gamma / \sum(\rho\Gamma)$$

- the precision of cross sections reproduction is determined **only by the product of these variables but not by absolute values of  $\rho$  and  $\Gamma$**
- **the hypothesis of independence of both,  $\rho$  and  $\Gamma$** , on structure of wave function of nucleus excited levels must be used
- it is necessary to use the model calculated parameters  $\Gamma$

## □ b) Two-step cascade quanta

$$I_2 \propto \Gamma / \sum(\rho\Gamma)$$

- detected cascade intensity depends on both, shapes of  $\Gamma$  and  $\rho$  parameters energy dependence and absolute value of the level density
- obtaining information of nuclear structure parameters **without introduction of theoretical models in experimental data fitting**
- possibility to obtain information about influence of real nuclear structure to gamma decay parameters

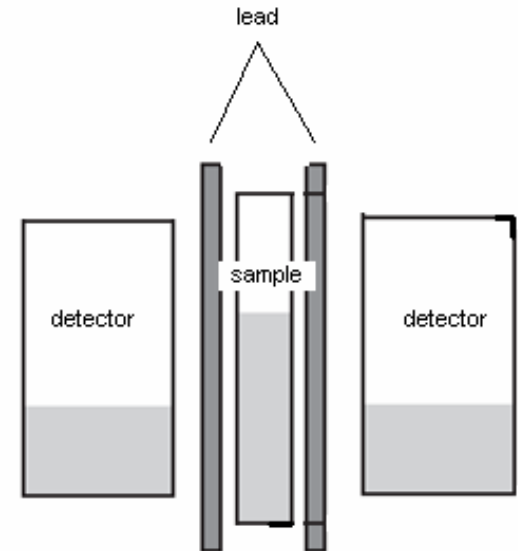
## 2. Dubna two-step gamma cascade method

**Dubna method** of nuclear structure parameters estimation using measurements of **two-step gamma cascades following thermal neutron captures**

Using **ordinary HPGe detectors in coincidence regime** of measurement

### **Advantages of Dubna method:**

1. ability to **obtained levels scheme**
2. possibility to **test different theoretical prediction**
3. obtaining information of nuclear structure parameters **without introduction of theoretical models in experimental data fitting**
4. obtaining **more reliable and precise values of nuclei structure parameters** (level density, radiative strength function or partial radiative width) than by other methods (smaller systematic errors than in other methods)



## 2. Dubna Two-step gamma cascade method

**Intensity of two-step gamma cascades:**

$$I_{\gamma\gamma}(E_1) = \sum_{\lambda,f} \sum_i \frac{\Gamma_{\lambda i}}{\Gamma_{\lambda}} \frac{\Gamma_{if}}{\Gamma_i} = \sum_{\lambda,f} \frac{\Gamma_{\lambda i}}{\langle \Gamma_{\lambda i} \rangle} \frac{\rho_i \Delta E}{m_{\lambda i}} \frac{\Gamma_{if}}{\langle \Gamma_{if} \rangle m_{if}}$$

**Equation** connecting two- step gamma cascade intensity and  $\rho$  and  $\Gamma$  is **undoubtedly degenerated.**

**N** values of experimental cascade intensities always can be converted in  **$\sim 2N$  values of  $\rho$  and  $\Gamma$**  which satisfy conditions:

$$\rho_1 \leq \rho \leq \rho_2 \quad \Gamma_1 \leq \Gamma \leq \Gamma_2$$

Using **iterative process** with randomly chosen functions  $\rho$  and  $\Gamma$ , it is possible to obtain the most **probable values of level density and radiative width (or radiative strength function).**

### 3. Possibilities of development of the effective method for determination of $\rho$ and RSF from $I_{\gamma\gamma}$

#### Previous results:

- $^{59}\text{Co}(p,2\gamma)^{60}\text{Ni}$  - reveal very significant increase in mean intensity of the primary  $E1$ -transition from  $p$ -resonances to two-phonon level of 2.5 MeV (qualitatively corresponding to predictions of QPMN)
- Significant increase of cascade population of levels in region around  $0.5B_n$  for  $\sim 20$  nuclei in mass region from 40 to 200 can be explained at present time only by increase of strength functions values of any cascade gamma-transitions to intermediate levels of, probably, vibration type excitation in energy region of the second (and, possibly, following) nucleons Cooper pairs breakup threshold.
- Evaporation nucleons spectra in reaction  $^{181}\text{Ta}(p,n)^{181}\text{W}$  showed that the excellent reproduction of the Obninsk experimental data can be achieved at accounting of local significant increase of parameter  $T$  for excitation energy which does not practically depend on beam protons energy.

### 3. Possibilities of development of the effective method for determination of $\rho$ and RSF from $I_{\gamma\gamma}$

- ❑ **The main defect** of the existing methods for determination of  $\rho$  and  $\Gamma$  is **absolute lack of model ideas on form of functional relation of these parameters** with each other and with real structure of nucleus.
- ❑ The level density determined from  $(n,2\gamma)$  reaction, is described in the best way by the **Strutinsky model**.
- ❑ Perspective models of  $\rho$  and  $\Gamma$  must take in account **coexistence of levels of phonon and quasi-particle types** and inevitable difference between radiative strength functions of gamma-transitions between them.
- ❑ Modern models of a nucleus (like QPMN or IBMF) to more or less extent take this difference into account. But, unfortunately, in form which is unfit for practical analysis of the experimental data.
- ❑ It is necessary to **develop phenomenological models** for description of experimental set values of nuclear structure parameters.
- ❑ At present this can be **partially performed for radiative strength functions** of cascade gamma-transitions.



### 3. Possibilities of development of the effective method for determination of $\rho$ and RSF from $I_{\gamma\gamma}$

The modified usual strength function  $k$  of dipole transitions in case of gamma-quantum emission is determined by relation:

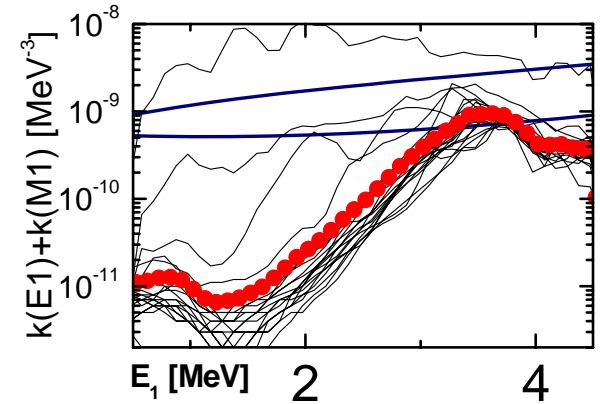
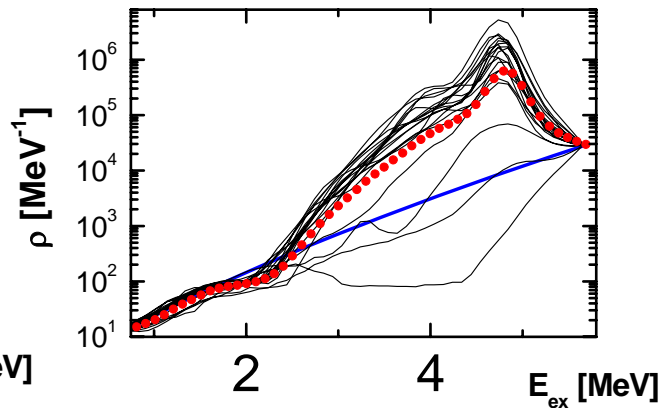
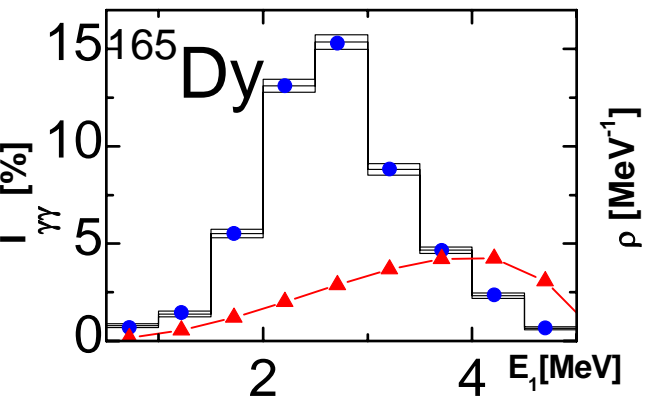
$$K_{\text{modif}} = k_{\text{standard}} \cdot \frac{D_{fg}}{D_i} = \frac{\Gamma_{\lambda i}}{E_\gamma^3 A^{2/3} D_\lambda} \cdot \frac{D_{fg}}{D_i}$$

instead of standard presentation:  $k_{\text{standard}} = \Gamma_{\lambda i} / (E_\gamma^3 A^{2/3} D_\lambda)$

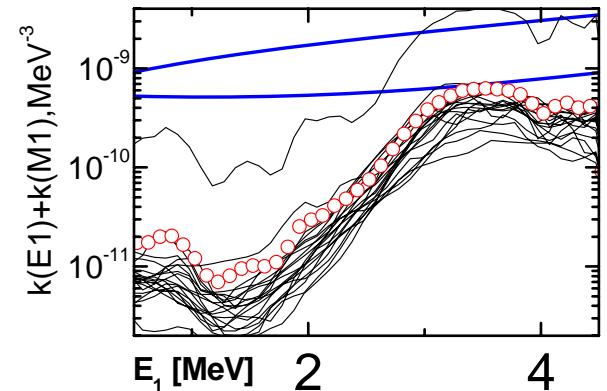
- $D_{fg}$  - spacing between levels of Fermi-Gas model in case of absence of collective type excitations
- $D_i$  fitted (experimental) value

$$K_{\text{modif}} = k_{\text{standard}} \cdot \frac{\rho_{\text{exp}}}{\rho_{fg}}$$

# 4. Results of practical approximation of two-step cascades intensity for proposed model



Modified RSF



Standard RSF

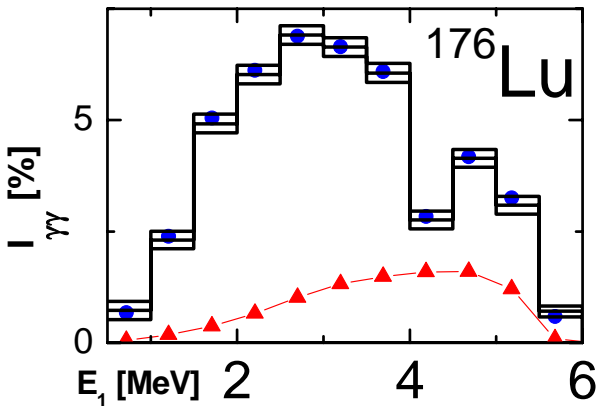
Measured and approximated values of two-step gamma cascade intensity

Level density

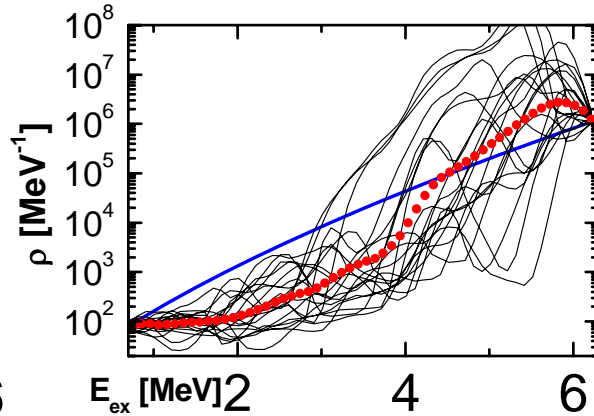
level density - Fermi-gas model

RSF model- Kadenskij, Markushev, Furman

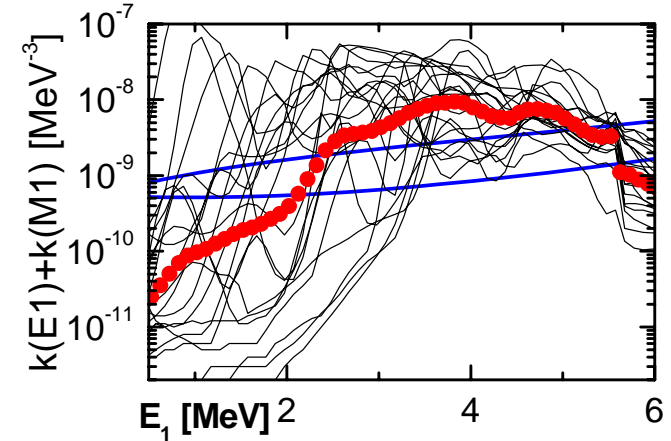
# 4. Results of practical approximation of two-step cascades intensity for proposed model



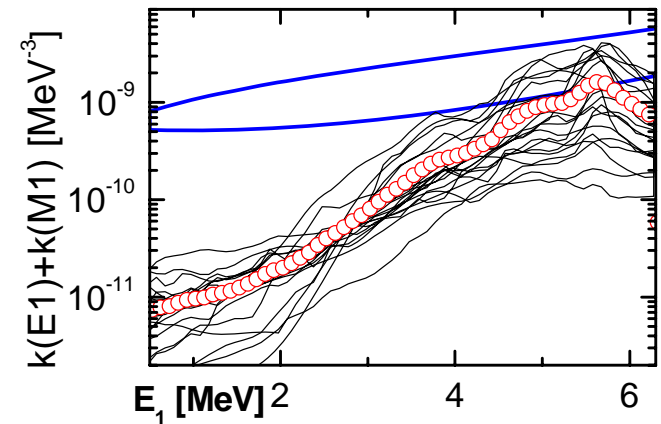
Measured and approximated values of two-step gamma cascade intensity



Level density

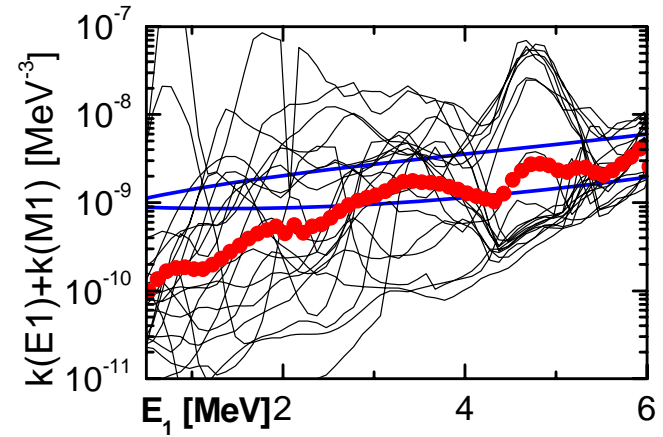
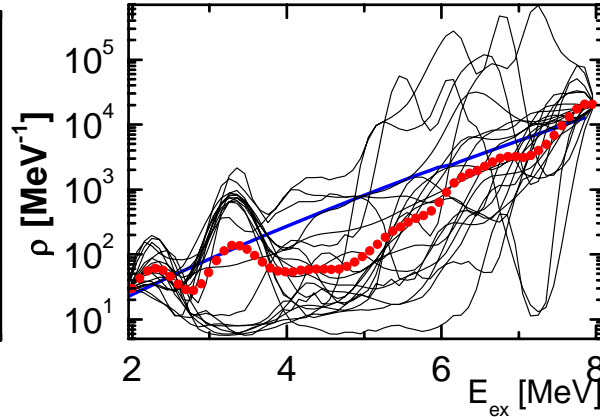
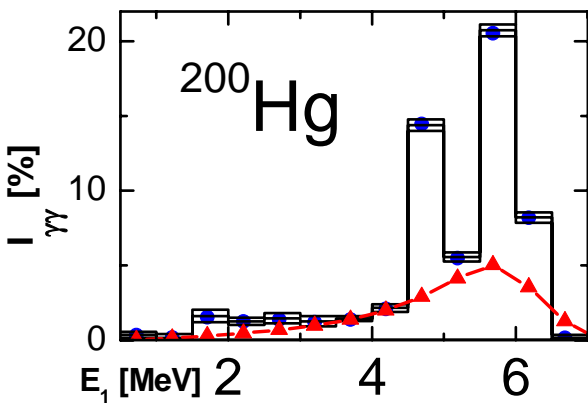


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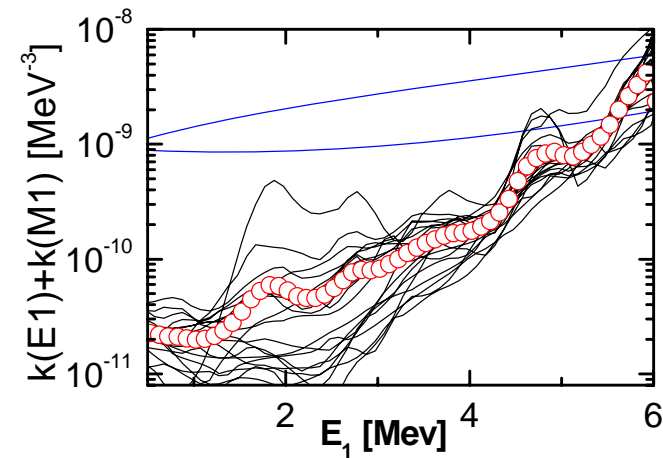


Standard RSF

# 4. Results of practical approximation of two-step cascades intensity for proposed model



Modified RSF

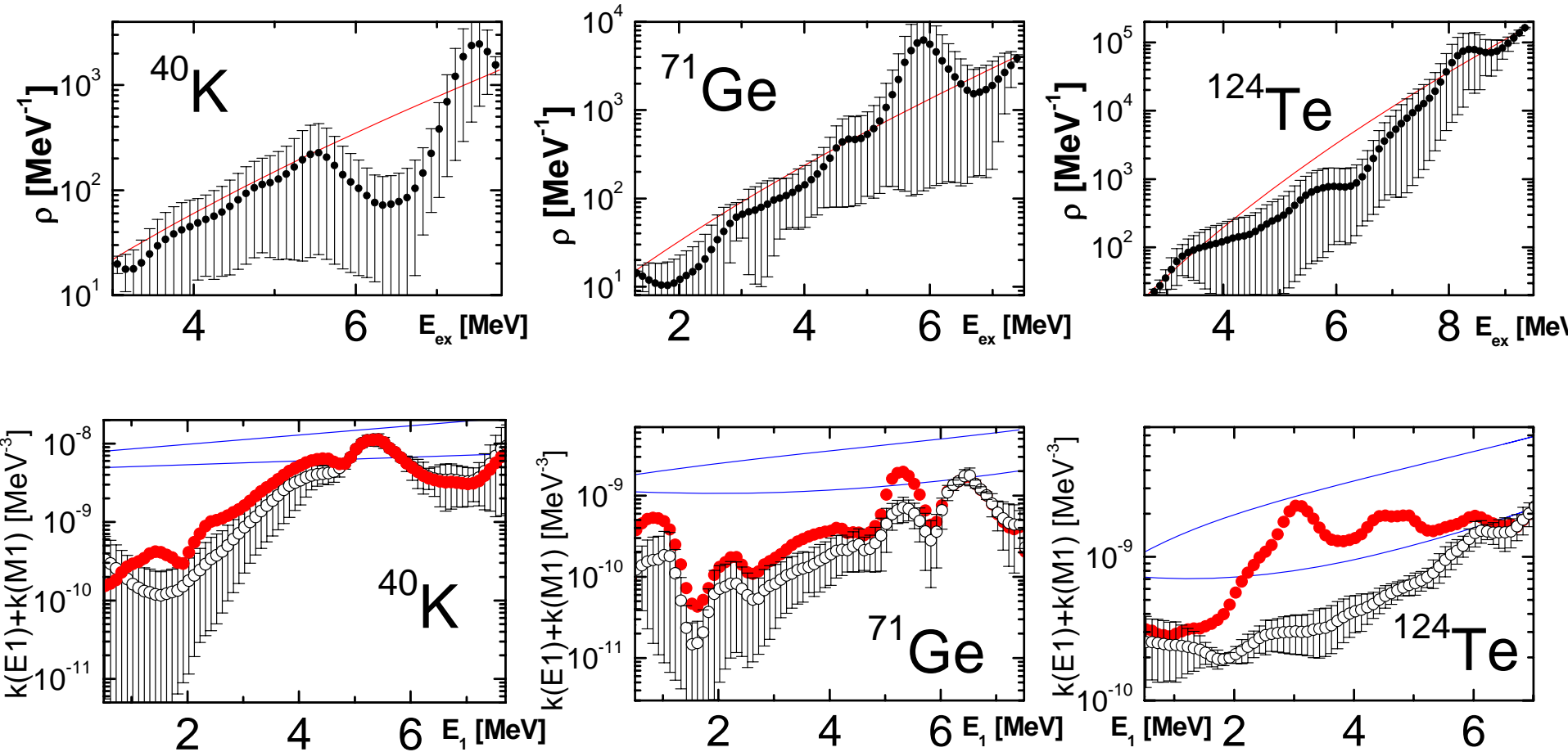


Standard RSF

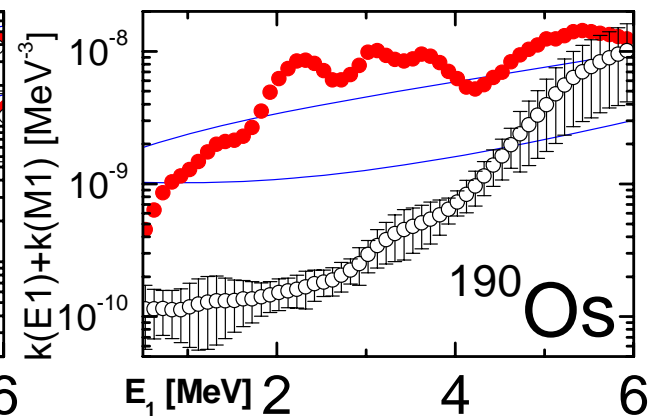
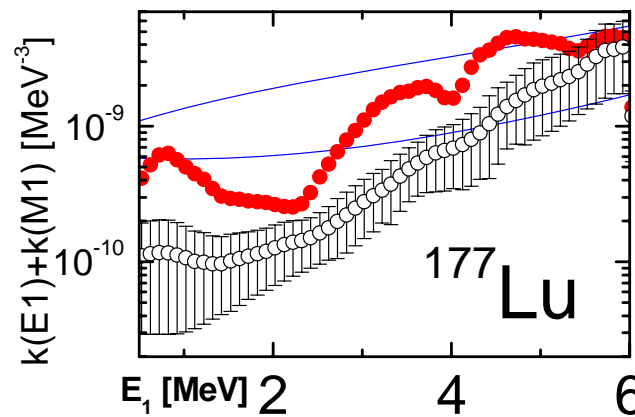
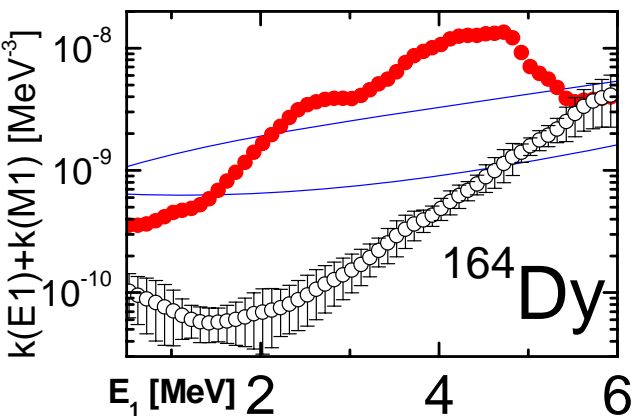
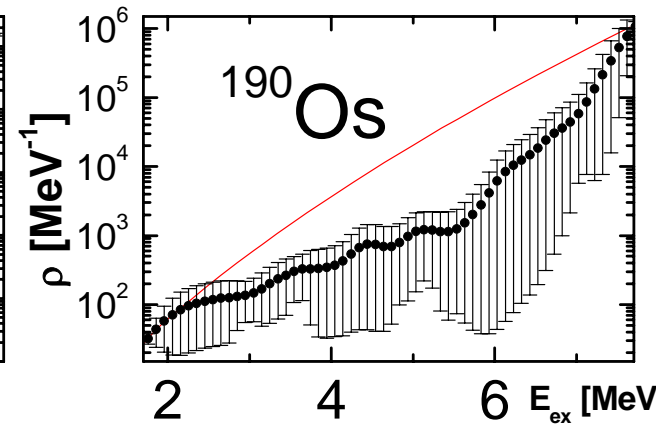
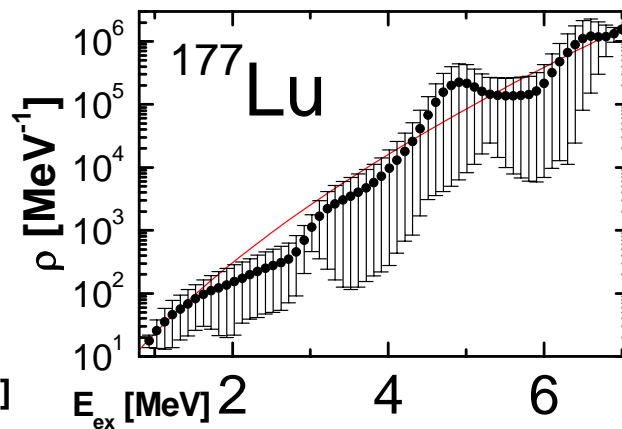
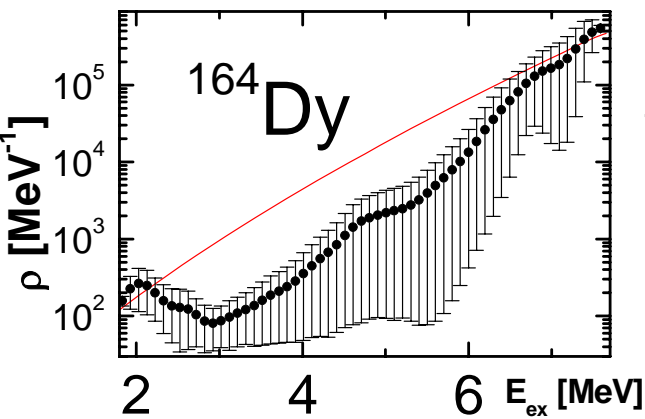
Measured and approximated values of two-step gamma cascade intensity

Level density

# 4. Results of practical approximation of two-step cascades intensity for proposed model



# 4. Results of practical approximation of two-step cascades intensity for proposed model



# Conclusion

- The use of new hypothesis does not remove **step-like structure in level density** below neutron binding energy. In other words –there is a fact of obvious presence of sharp change in structure of nuclei levels of different type, which at present can be interpreted as **break of Cooper pair of nucleons** in heated nucleus.
- RSF of gamma-transitions between excited levels of heated nucleus also confirm **very strong influence of nucleus structure on their partial widths.**

## Conclusion

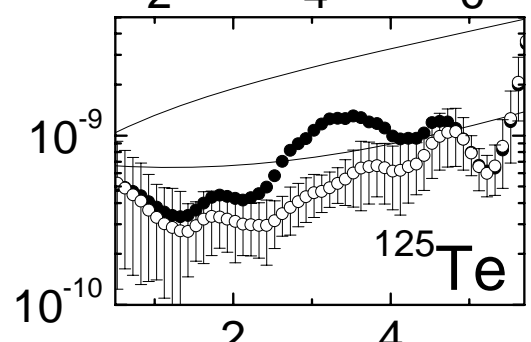
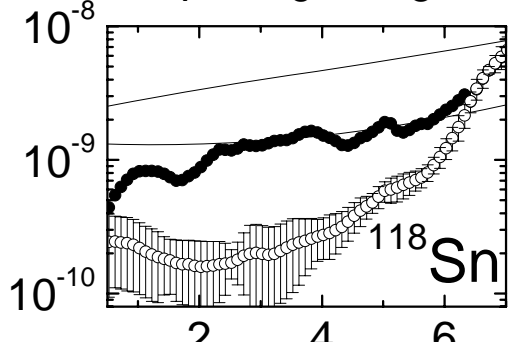
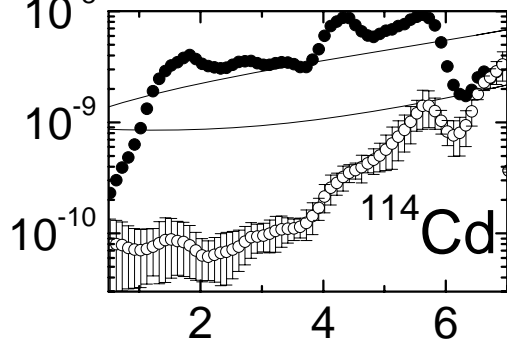
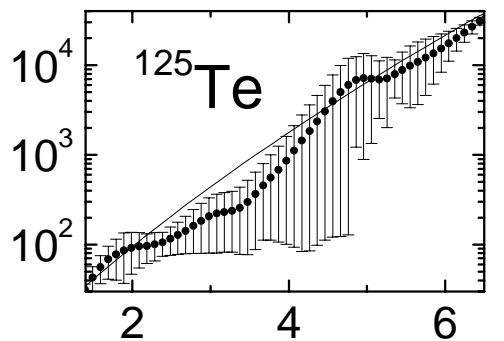
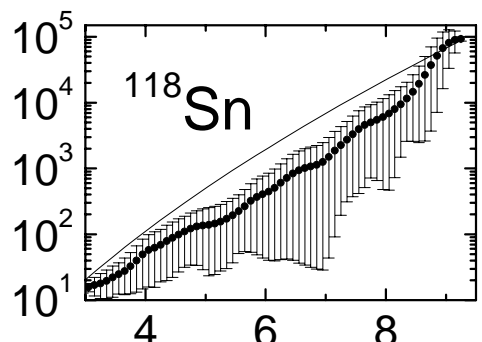
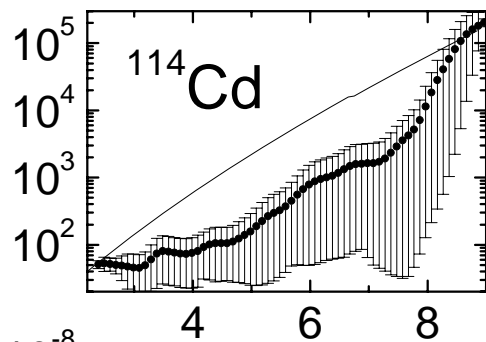
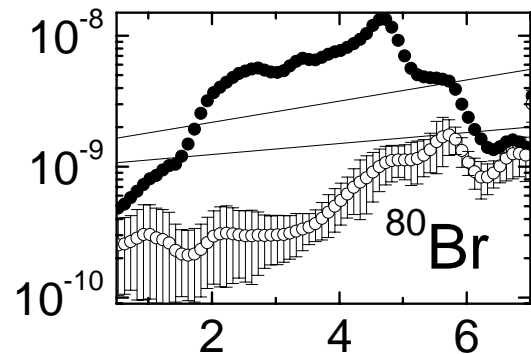
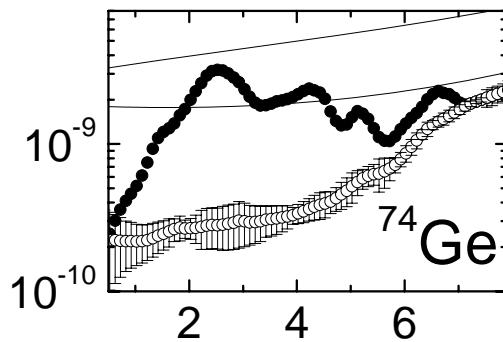
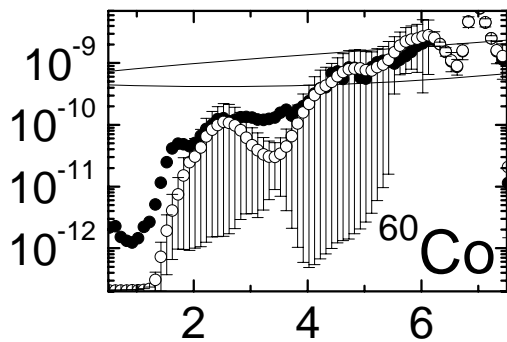
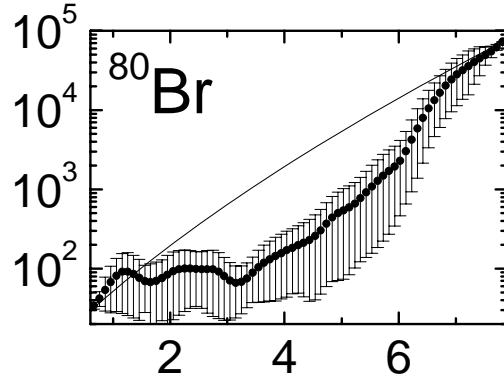
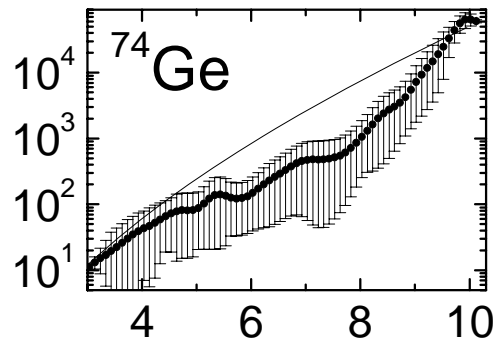
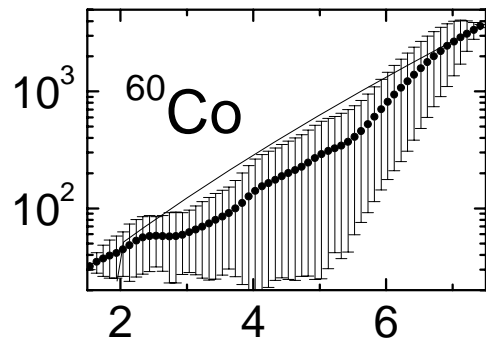
- Intensity of two-step cascades following thermal neutron capture can be precisely reproduced under condition that the **RSF of cascade transitions are considerably increased because of presence of gamma-transitions between the levels with large vibration components of wave functions.** Respectively, such possibility must be taken into account at both, planning of new experiments and creation of new phenomenological models of radiative strength functions and penetrability coefficients for gamma-quanta or evaporation nucleons and light nuclei.

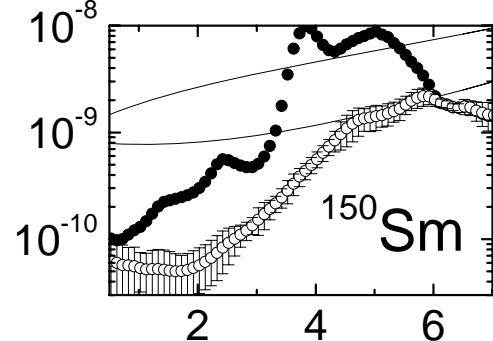
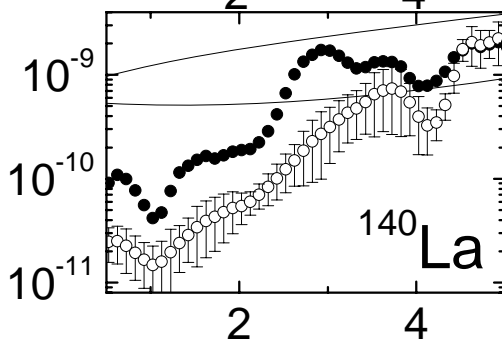
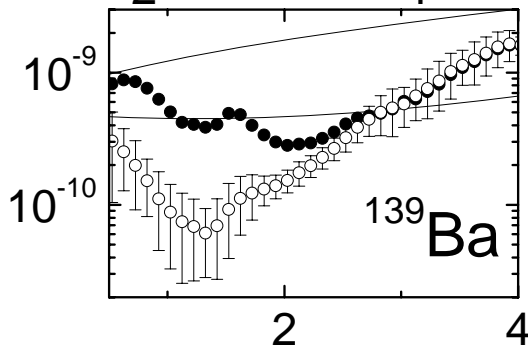
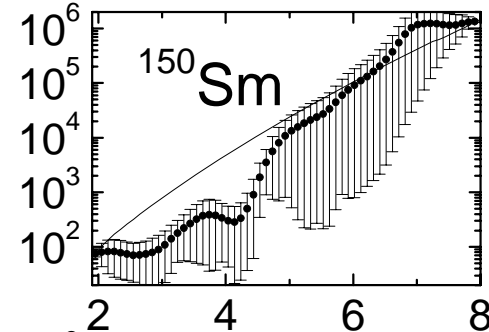
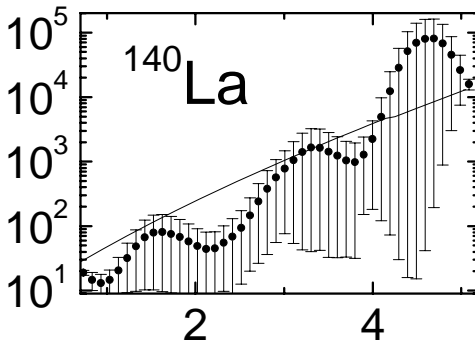
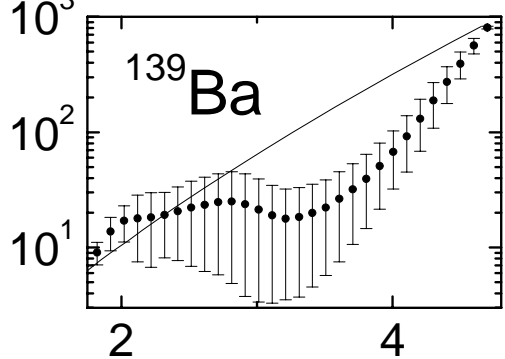
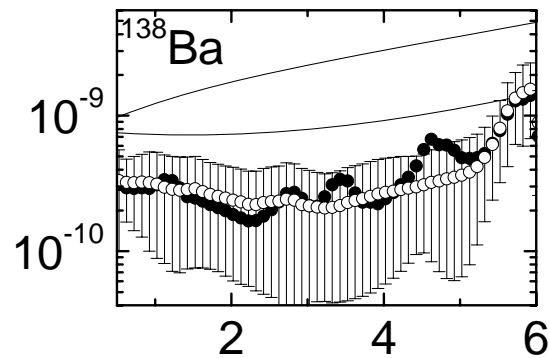
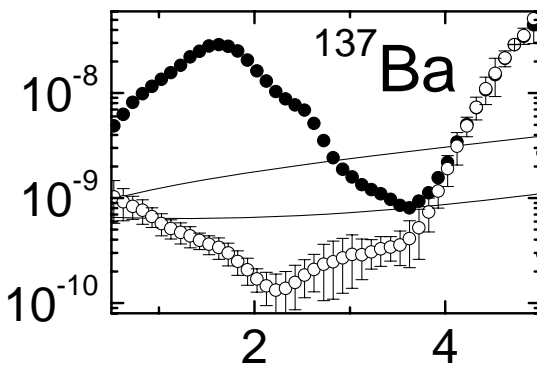
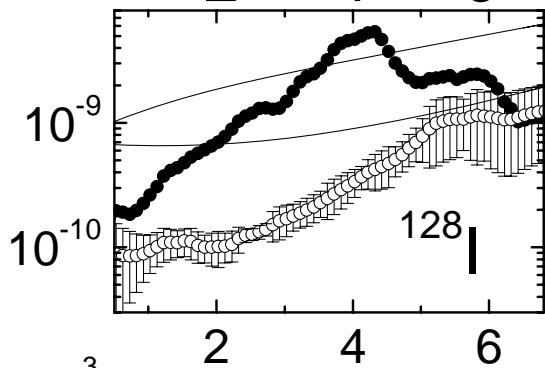
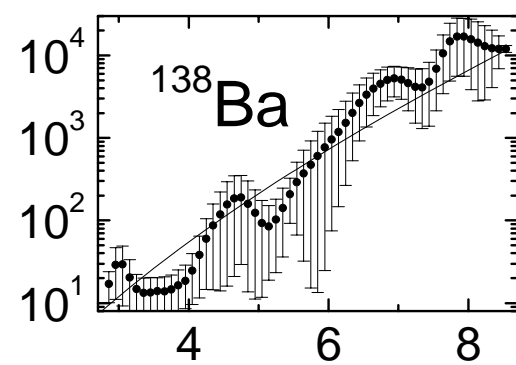
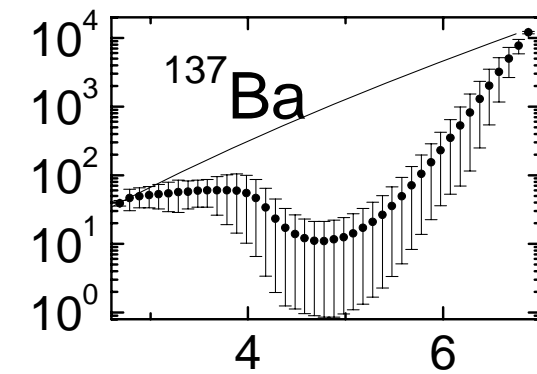
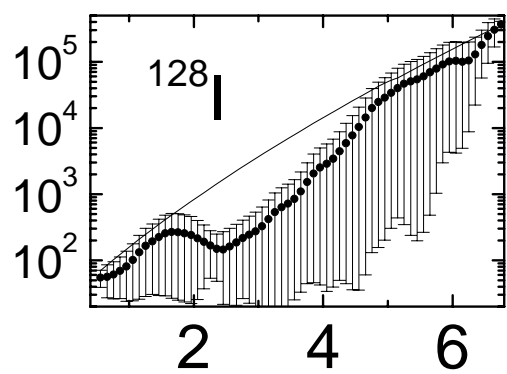


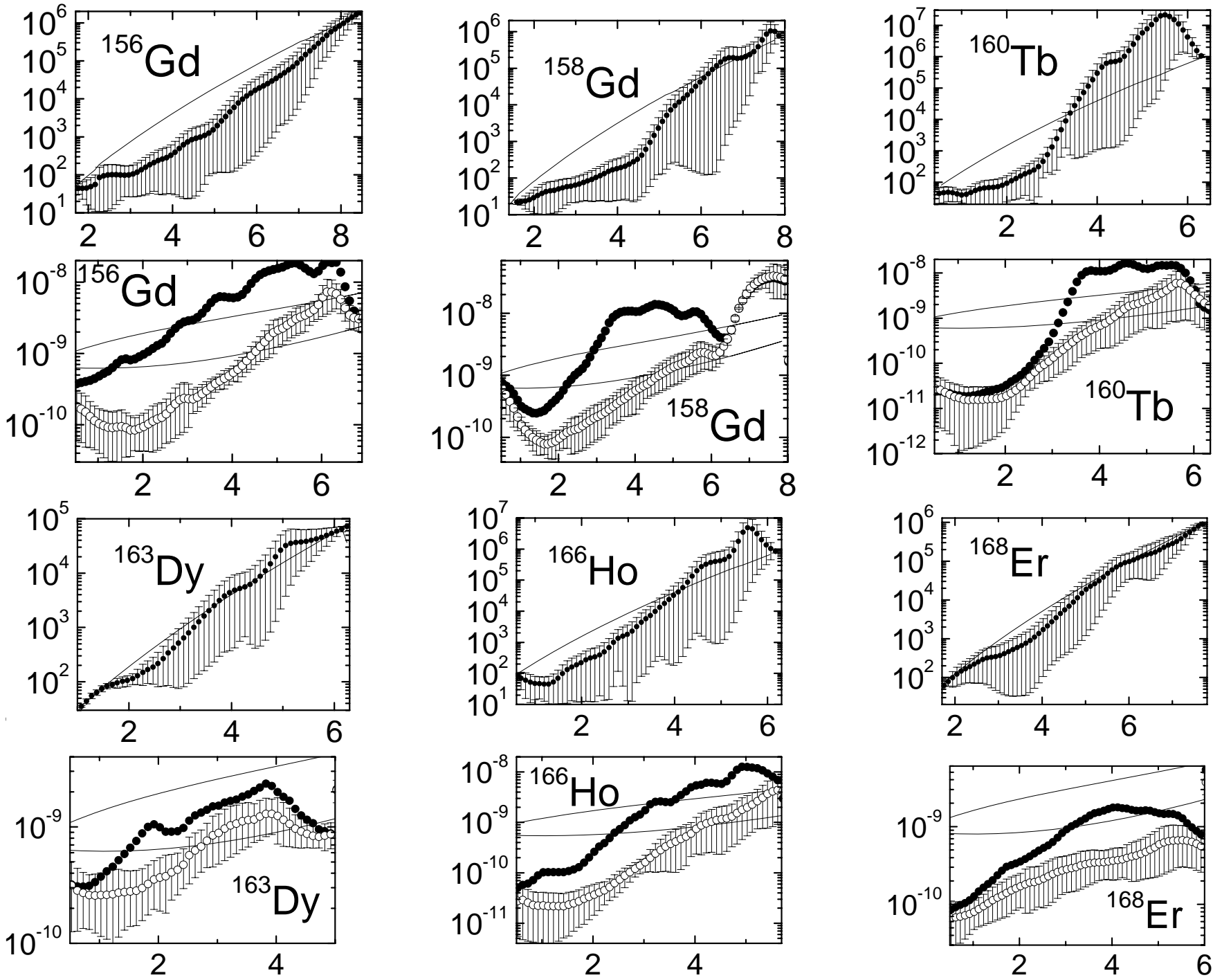
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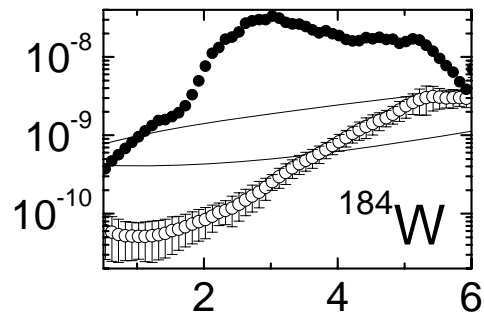
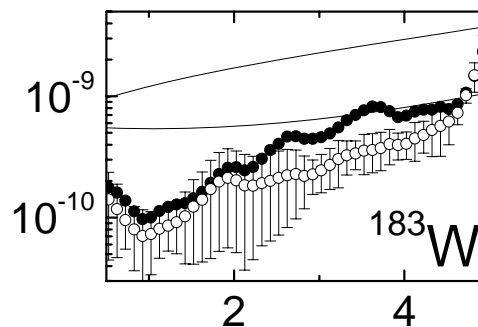
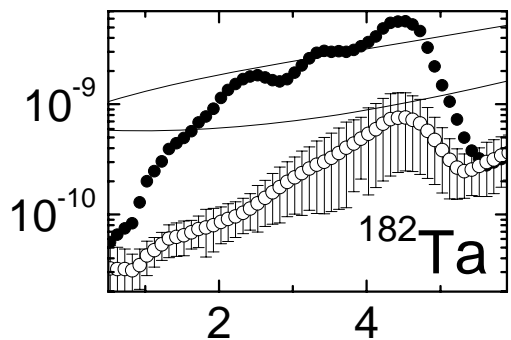
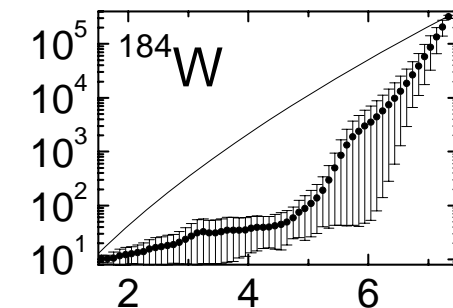
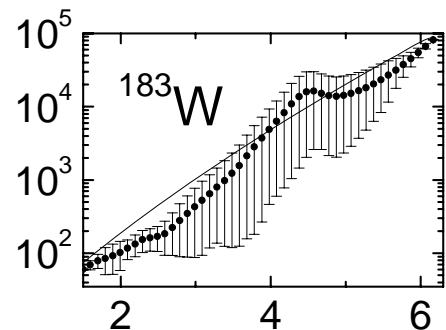
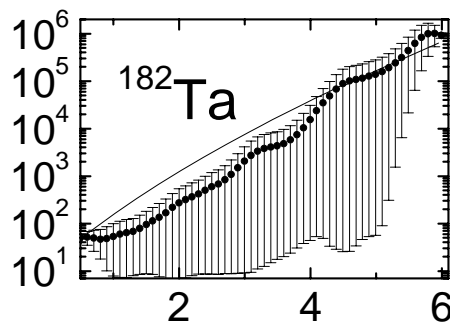
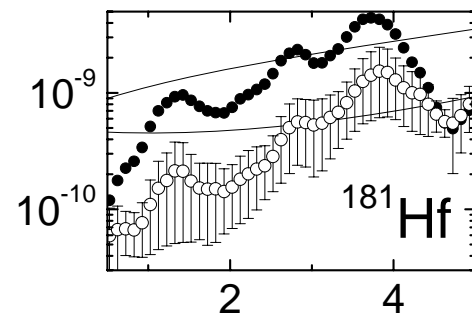
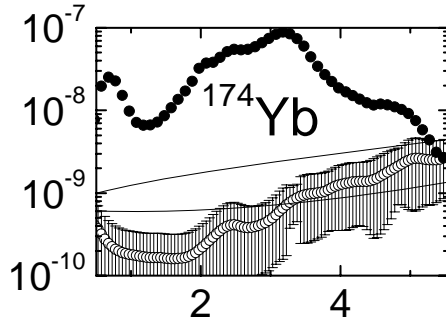
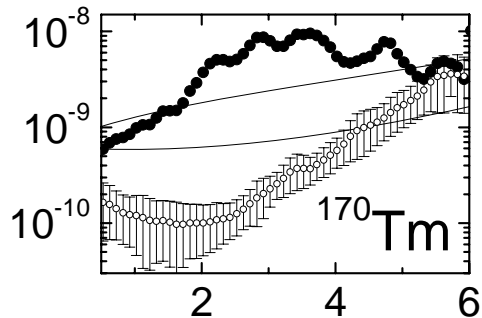
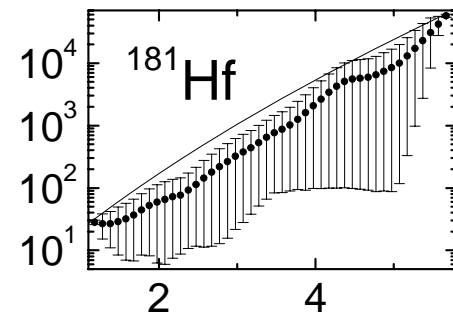
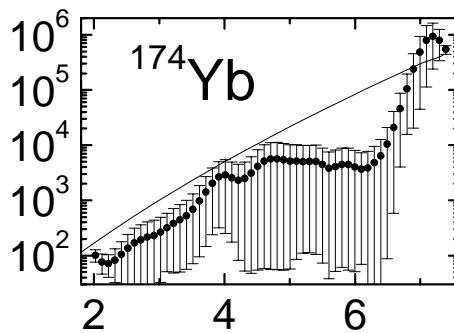
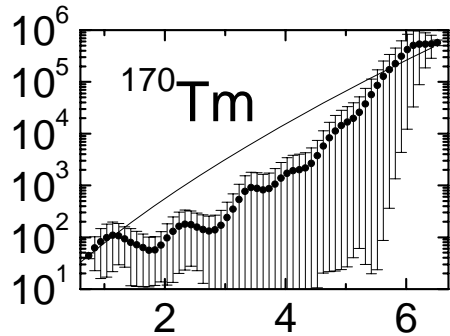
## 4. Results of practical approximation of two-step cascades intensity for proposed model

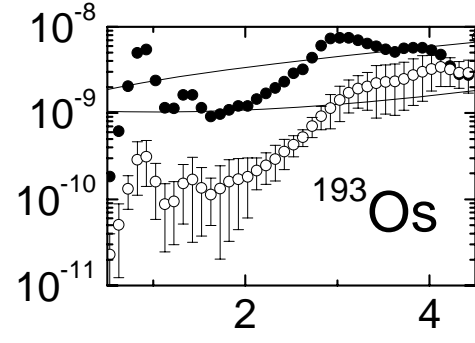
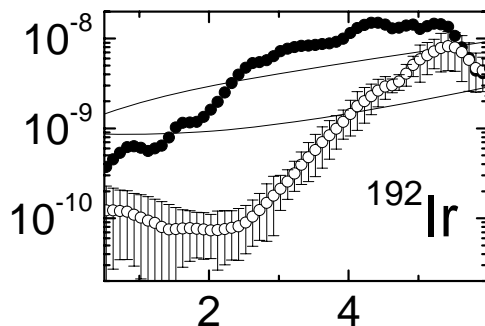
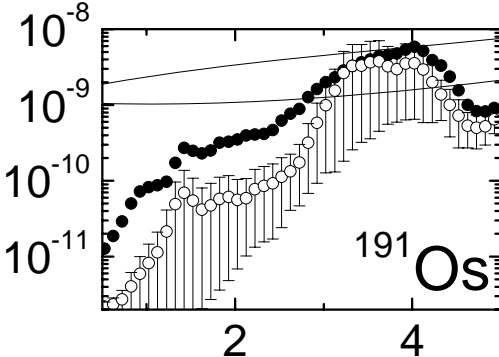
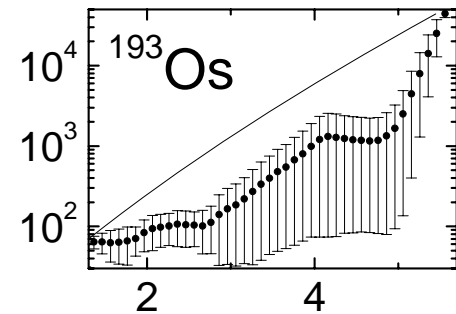
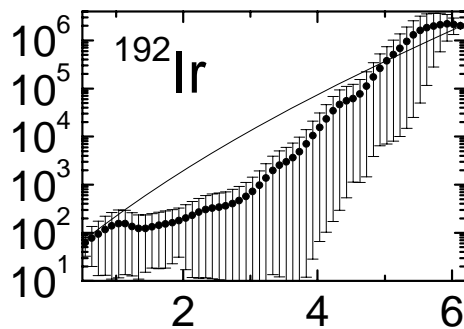
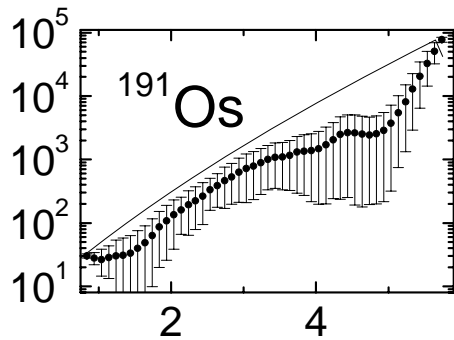
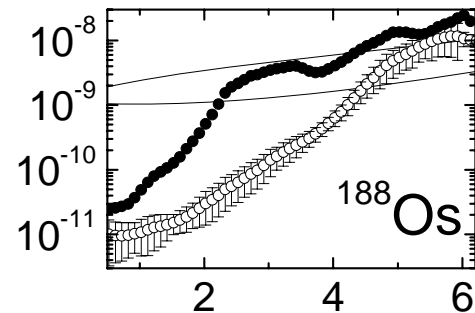
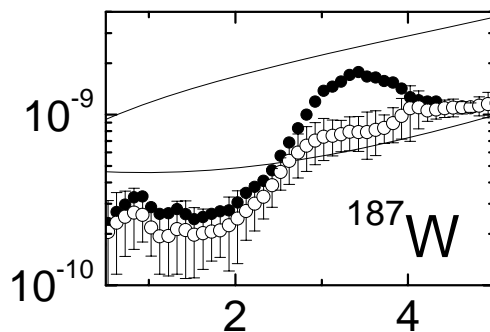
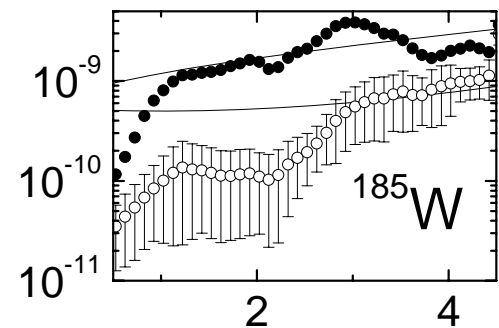
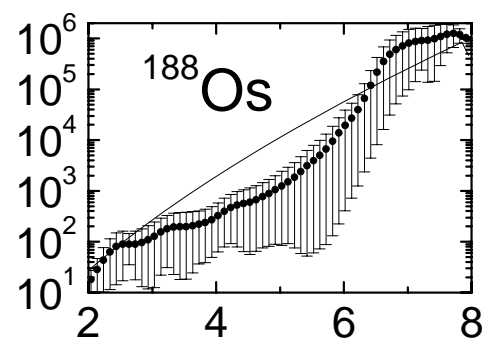
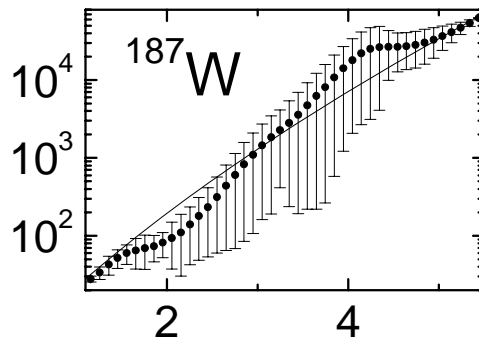
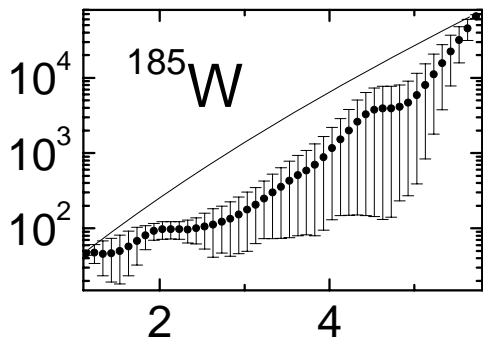
- The unsolved problem is the question on position of points of minimal density (break threshold  $U_n$  of the next Cooper pair of nucleons) for levels with parity  $\pi=+$  and  $\pi=-$ .
- Multipolarities of primary and any next gamma-transitions ending at given nucleus level can be different.
- In region of neutron binding energy, for some nuclei the very strong exceeding of  $\rho_{exp}$  above model value  $\rho_{fg}$  disappeared or considerably decreased as compared with previous the data.
- Disagreement between  $\rho_{exp}$  and  $\rho_{fg}$ :
  - the process of energy exchange between quasi-particles and phonons in different isotopes of the same element
  - omission of large amount of very small neutron resonances

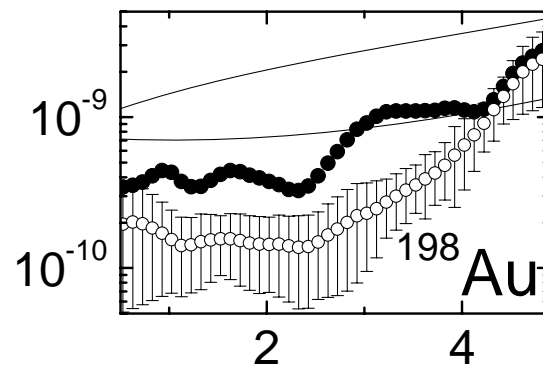
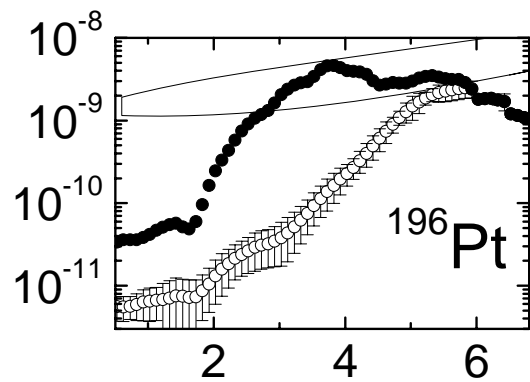
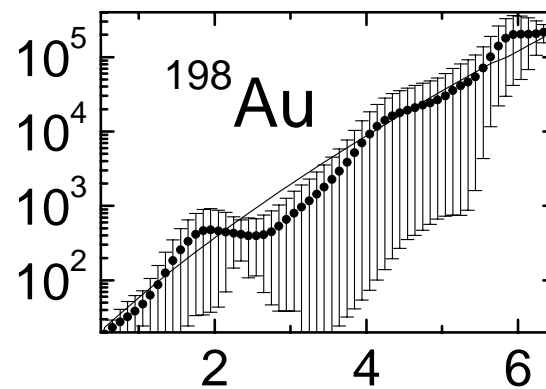
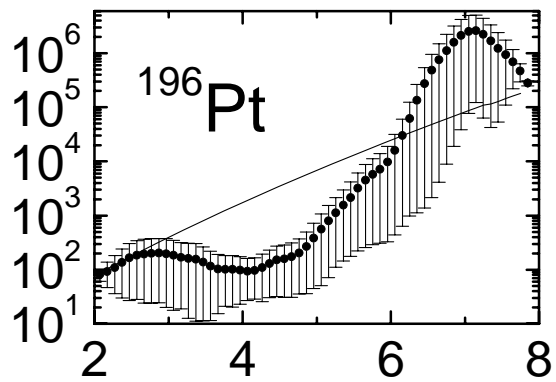














The observed shape of energy dependence of evaporation nucleon spectrum in  $^{181}\text{W}$  and  $^{60}\text{Ni}$  can be reproduced by functions  $\rho_{\text{cas}} = \psi(E_{\text{ex}})$  and  $\Gamma_{\text{cas}} = \varphi(E_1)$  which were obtained from  $(n, 2\gamma)$  reaction and satisfy functional dependence:

$$\Gamma_{om}/D_{ev} = \Gamma_{cas}/D_{cas} \quad T_{om} \rho_{ev} = T_{cas} \rho_{cas} \quad \text{or}$$