



ISINN-25

FRANK LABORATORY  
OF NEUTRON PHYSICS

# Method for investigation of the superfluidity of excited nucleus

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# Introduction



- The method was created, developed and tested in FLNP, JINR.
- Taking advantage of experimental intensities of two-step cascade gamma-decay following capture neutron reaction.
- The experiment on recording this cascade gamma-transition was carried out in Dubna (Russia), Riga (Latvia), Rez (Czech Republic) and Dalat (Vietnam).

# Nuclear superfluidity

- The nuclear superfluidity was caused by pairing of nucleons and was presented by N. N. Bogolubov in 1958.
- This effect is revealed because of the existence of energy gap between superfluid and normal states.
- To understand dynamic of changing phase of nuclear matter, it is necessary to determine simultaneously the level density and the partial widths at all excitation energies.

# How do we do?

- Step 1: Extract the cascade intensity distribution of primary transition  $I_{\gamma\gamma}(E1)$  from the spectrum of experimental cascade intensity  $I_{\gamma\gamma}(E1, E2)$ .
- Step 2: Parameterize level density  $\rho$  and partial width  $\Gamma$  ( $(\rho = \varphi(p1, p2 \dots); \Gamma = \psi(q1, q2))$ ).
- Step 3: Fit  $I_{\gamma\gamma}(E1)$  to their experimental values.

# Model's Foundation

1. The model of density of n-quasi-particle states, which is presented by V. M Strutinsky for describing the level density of fermion type.
2. A phenomenological relation between changing a density of quasi-particle levels and nuclear entropy for describing the collective enhancement of level density.
3. The model of S. G. Kadmenskij, V. P Markushev and W. I Furman (KMF) with adding some peaks (from 2 to 4) have shape of the asymmetrical Lorentzian curve to describe a distribution of widths of E1 and M1-transmissions.

# Dubna practical model

The cascade intensity distribution that depends on energy of primary transition is presented:

$$I_{\gamma\gamma}(E_1) = \sum_{\lambda, f} \sum_i \frac{\Gamma_{\lambda i}}{\Gamma_{\lambda}} \frac{\Gamma_{if}}{\Gamma_i} = \sum_{\lambda, i} \frac{\Gamma_{\lambda i}}{\langle \Gamma_{\lambda i} \rangle m_{\lambda i}} n_{\lambda i} \frac{\Gamma_{if}}{\langle \Gamma_{if} \rangle m_{if}} \quad (1)$$

- $m_{\lambda i}$  : number of excited levels in intervals from the compound state  $\lambda$  to the intermediate level  $i$ .
- $m_{if}$  : number of excited levels in intervals from the intermediate level  $i$  to the final level  $f$ .
- $n_{\lambda i}$  : number of intermediate cascade levels in small interval  $\Delta E$  of energy of primary transitions.

# Fitting Process

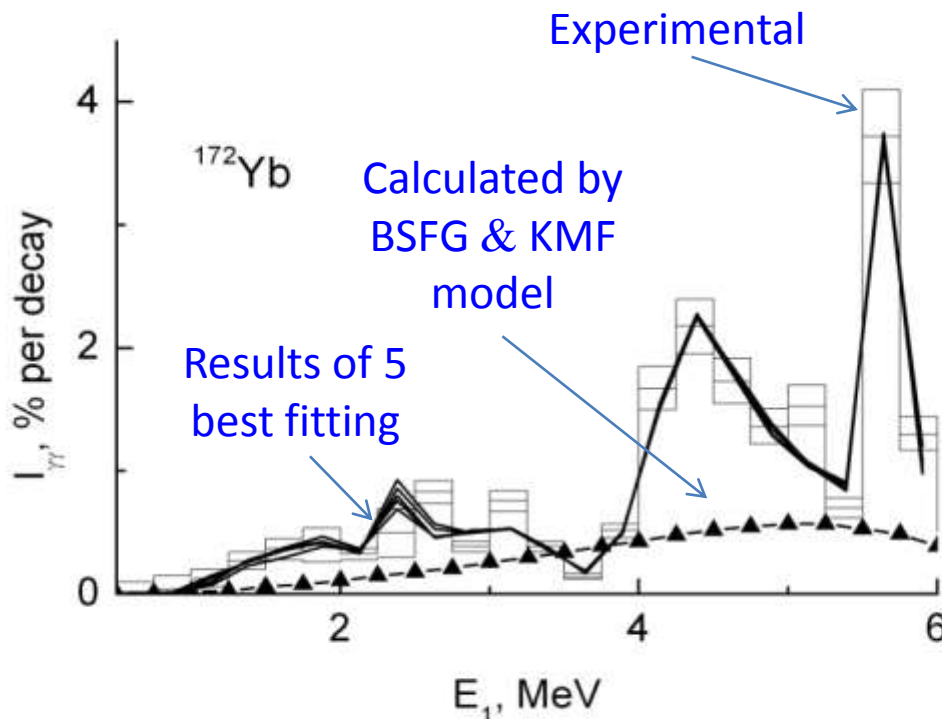


- Using the maximum likelihood fitting method we obtain parameters:
  - The breaking thresholds of Cooper nucleon pairs  $U_i$ ;
  - A common parameter  $E_u$  for all Cooper nucleon pairs;
  - The independent parameters  $A_l$  of the density of vibrational levels above the break up threshold  $U_i$ ;
- Uncertainty of experimental distribution  $I_{\gamma\gamma}(E1) \leq 10\text{-}20\%$  in any energy interval, we obtain the most accurate parameters.



# Results

- Recently, we have been using the Dubna method to study for compound nucleus  $^{172}\text{Yb}$ .
- Experiment of this study was performed at DDNR reactor, in Dalat, Vietnam.



*Fig. 1. the cascade intensity distribution of primary transition.*

# Results

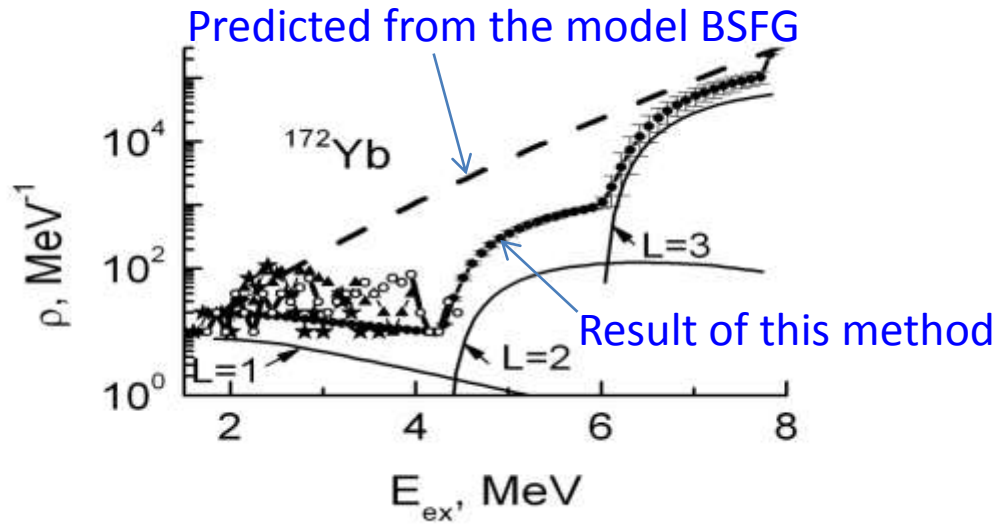


Fig. 2. The level density of  $^{172}\text{Yb}$  nucleus.

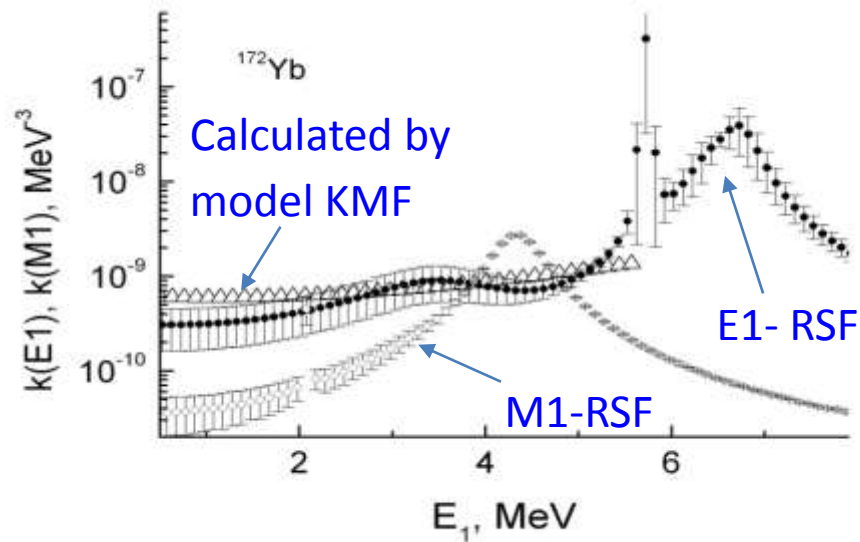
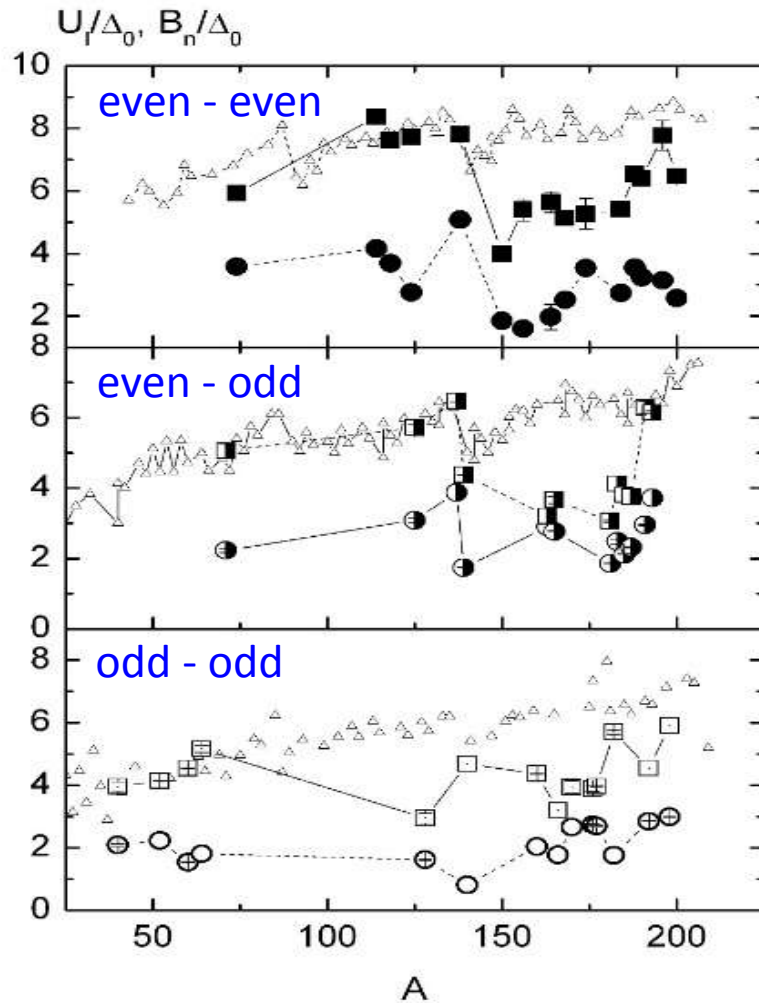


Fig. 3. E1- and M1-radiative strength function

# Result



- Up to now **44** excited nuclei with different parities have studied by the Dubna method.
- For spherical nuclei ( $A < 150$ )  $U_3 \approx B_n$ , for deformed nuclei ( $150 < A < 190$ ) this value is twice less.

*Fig.4. Dependence of the breaking thresholds of Cooper pairs on the nuclear mass  $A$ .*

# Conclusion

- We can make a statement that the Cooper pairs breaking thresholds for spherical nuclei are higher than for deformed nuclei.
- Both a number of breaking Cooper nucleon pairs and a shape of excited nucleus have an influence on the dynamics of superfluid phase of nuclear matter.
- The Dubna practical model is a unique model that has the possibility to reproduce the experimental cascade intensity distribution with high accuracy.

**Thank you for your attention!**