

Fast Neutron Processes on Molybdenum Isotopes

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Molybdenum nucleus has many natural and artificial isotopes important for fundamental and applicative researches. ^{94}Nb nucleus, important in nuclear technology, can be obtained in $^{94}\text{Mo}(n,p)$ and $^{95}\text{Mo}(n,np)$ processes. Cross sections, angular correlations and isomer ratios in fast neutrons induced reactions up to 20 MeV were evaluated using codes realized by authors as well as dedicated software. Contributions of different nuclear reaction mechanisms in the cross sections were also determined. Parameters of nuclear optical potential, density levels and radius channels were extracted. Theoretical evaluations were compared with existing experimental data. The results of present work were realized in the frame of the fast neutrons scientific program at FLNP basic facilities (IREN and EG5) and are necessary for future experiment preparation .

STRUCTURE OF THE PRESENTATION

1. INTRODUCTION

2. THEORETICAL BACKGROUND

3. COMPUTER CODES

4. RESULTS

5. DISCUSSION

6. CONCLUSIONS

1. INTRODUCTION – FAST NEUTRON PROCESSES

FAST NEUTRONS ACTIVATION ANALYSIS

- COMPLEMENTARY TO ACTIVATION WITH SLOW NEUTRONS
- POSSIBILITY TO CREATE BETTER GAMMA EMITTERS COMPARED WITH SLOW NEUTRONS
- POSSIBILITY TO INVESTIGATE LARGE SAMPLE DUE TO:
 - PENETRATION DEPTH OF NEUTRONS
 - ESCAPE FROM SAMPLE OF EMITTED GAMMAS

PROCESSES

- (n,n') , $(n,n'\gamma)$, $(n,2n)$, (n,p) , (n,np) , (n,α) , $(n,n\alpha)$ etc

DIFICULTIES

- HIGH BACKGROUND

METHODS OF BACKGROUND REDUCTION

- NEUTRONS TAGGING

1. INTRODUCTION – FAST NEUTRONS PROCESSES – ANALYZED ELEMENTS

GENERAL

Precise nuclear data for:

- Nuclear energy – existing fission reactors ; future fusion reactors
- Long lived radioactive waste
- Reprocessing of U and Th (Transmutation and Energy)
- Accelerated Driven Systems (ADS)

FAST NEUTRONS REACTIONS – ^{94}Nb PRODUCTION

Processes:

- $^{94}\text{Mo}(n,p)^{94}\text{Nb}$, $^{95}\text{Mo}(n,np)^{94}\text{Nb}$

Fast Neutrons with Emission of Charged Particles

- Nuclear reaction mechanisms
- Nuclear Data for Structural Material needed to estimate gas production by (n,p) and (n, α) reactions

2. THEORETICAL BACKGROUNDS

Cross Sections Evaluations

-CS calculated with Talys

Incident energy - from threshold up to 20 MeV with the contribution of:

- Direct Processes -> DWBA
- Compound Processes – >Hauser – Feshbach Formalism
- Pre - equilibrium – >Two Component Exciton Model

Nuclear Potential (implemented in Talys)

- Wood Saxon of Type: Volume and Surface
- Spin Orbit Interactions
- Potential Parameters: Obtained from Nuclear Data Processing
 - Local with Real and Imaginary Part
 - Global with Parameters by Koning - Delaroche

Levels Density – Constant Temperature Fermi Gas Model

2. THEORETICAL BACKGROUNDS – HAUSER FESHBACH APPROACH

Cross section

$$\sigma_{\alpha\beta} = \pi\lambda_{\alpha}^2 \frac{T_{\alpha}T_{\beta}}{\sum_c T_c}$$

Historically first HF expression

$$\sigma_{\alpha\beta} = \pi\lambda_{\alpha}^2 \frac{T_{\alpha}T_{\beta}}{\sum_c T_c} W_{\alpha\beta}$$

Hauser - Feshbach

$W_{\alpha\beta} =$ Widths Fluctuation Factor (WFC)

WFC

- Indicates a correlation between the ingoing channel (incident) and outgoing channels
- At low energies (<1 MeV) WFC=1 - no correlation between *in* and *out* channels
- Decreases slowly with the energy
- It is calculated by complicate procedures (ex Moldauer expression)

2. THEORETICAL BACKGROUNDS – ISOMER RATIO

$$R = \frac{Y^m}{Y^g} = \text{Experimentally measured isomeric ratio}$$

$Y_m, Y_g =$ Yields of isomeric and unstable ground states

General Expression

$$R = \frac{Y_m}{Y_g} = \frac{\int_{E_{th}}^{E_m} N_0 \phi(E) \sigma_m(E) dE}{\int_{E_{th}}^{E_m} N_0 \phi(E) \sigma_g(E) dE}$$

$E_{th} =$ Threshold energy of nuclear reaction

$E_m =$ Maximal energy of incident particle

2. THEORETICAL BACKGROUNDS – ACTIVITY

$$A_{obs} = \frac{N\sigma\phi a\varepsilon}{\lambda} [1 - \text{Exp}(-\lambda t)] \text{Exp}(-\lambda T) [1 - \text{Exp}(-\lambda\Delta T)]$$

Where:

N = Number of atoms of the isotope of the element

σ = cross section

a = γ -ray abundance

ϕ = Neutron Flux

ε = Detector efficiency

λ = Decay constant

t = Irradiation time

T = Cooling time

ΔT = Counting time

Yields and Activities – features not implemented yet in Talys

3. THEORETICAL BACKGROUNDS – TALYS

TALYS – Freeware soft working under LINUX – dedicated to nuclear reactions, fission and nuclear structure calculation

Possibility - to calculate inclusive and exclusive cross sections

Nuclear Reaction (binary) – $X(x,y)Y$

Inclusive cross section – including y particle from other open channels like (x,ny) , $(x,2ny)$,...

Exclusive cross section – taking into account the y particle only from $X(x,y)Y$ reaction

4. RESULTS.

FAST NEUTRON REACTIONS WITH CHARGED PARTICLES EMISSION

CASE OF $^{94}\text{Mo}(n,p)^{94}\text{Nb}$ Reaction ; $Q_{np} = -1.26 \text{ MeV}$

Importance – Obtaining of ^{94}Nb Nucleus

Natural Molybdenum: Mo Z=42

Natural Isotopes of Mo with their abundance (%):

- ^{92}Mo (14.65), ^{94}Mo (9.19), ^{95}Mo (15.87), ^{96}Mo (16.67), ^{97}Mo (9.58), ^{98}Mo (24.29) - stables
- ^{100}Mo (9.74) – Decay $\beta^- \beta^-$ to ^{100}Ru

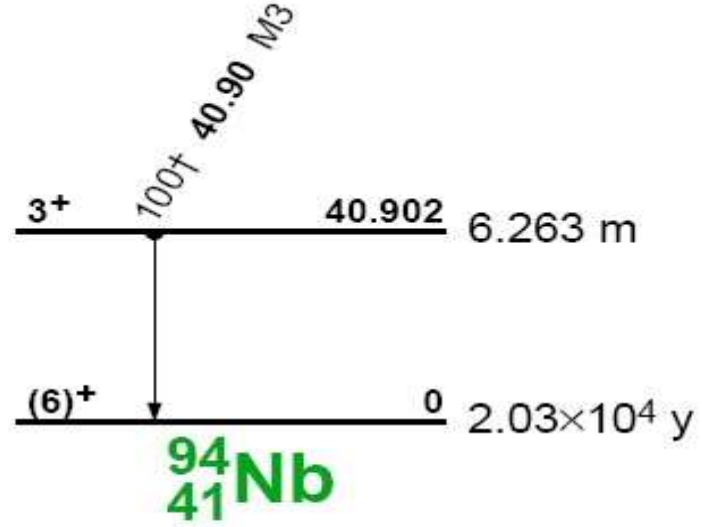
Density of Natural Mo: 10.28 g/cm³ :

Spin and Parity of ^{94}Mo : 0⁺

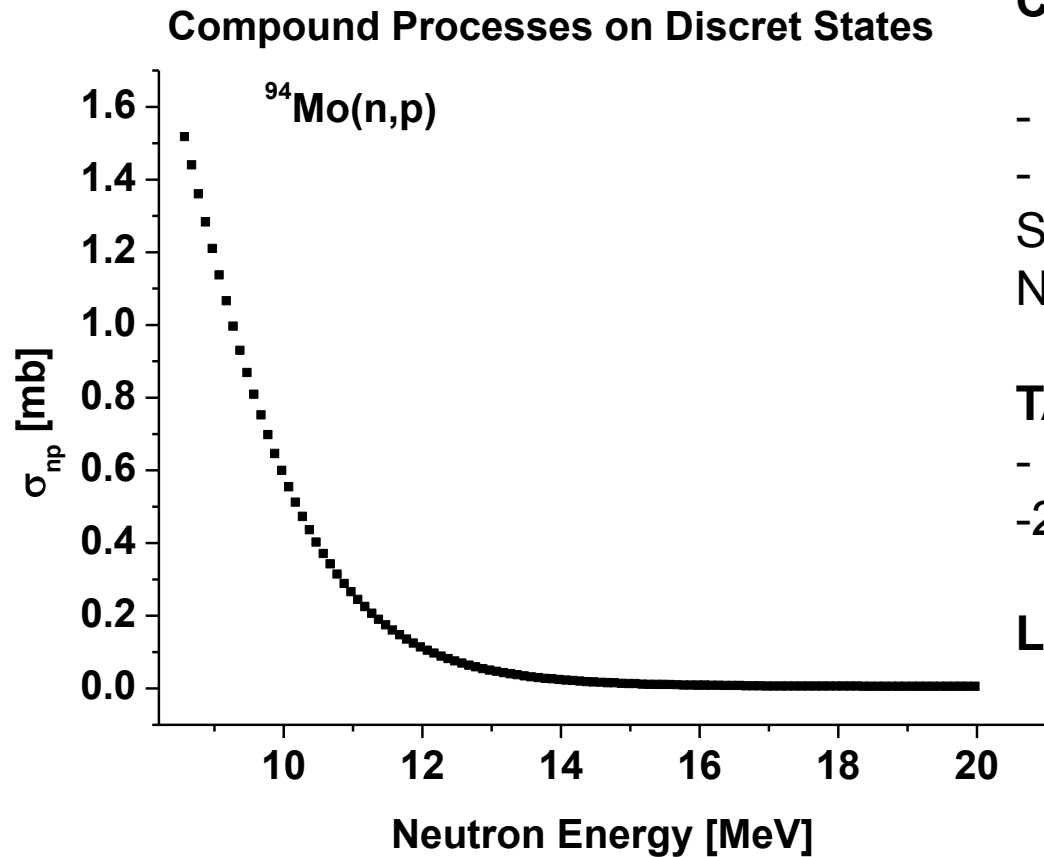
Isomers in $^{94}\text{Mo}(n,p)^{94m,g}\text{Nb}$ Reaction

Results on:

- Inclusive and Exclusive Cross Sections
- Production of isomer and ground states of ^{94}Nb (m and g states)
- Parameters of Nuclear Potentials in incident and exit channels
- Activities and other Concurrent Processes



4. RESULTS. INCLUSIVE REACTIONS



CROSS SECTION (CS) ANALYSIS CONTRIBUTION OF:

- NUCLEAR REACTION MECHANISM
- DISCRETE AND CONTINUUM STATES OF THE COMPOUND NUCLEUS

TAKEN INTO ACCOUNT:

- 10 DISCRETE STATES FOR (n,x)
- 20 DISCRETE STATES FOR (n,n')

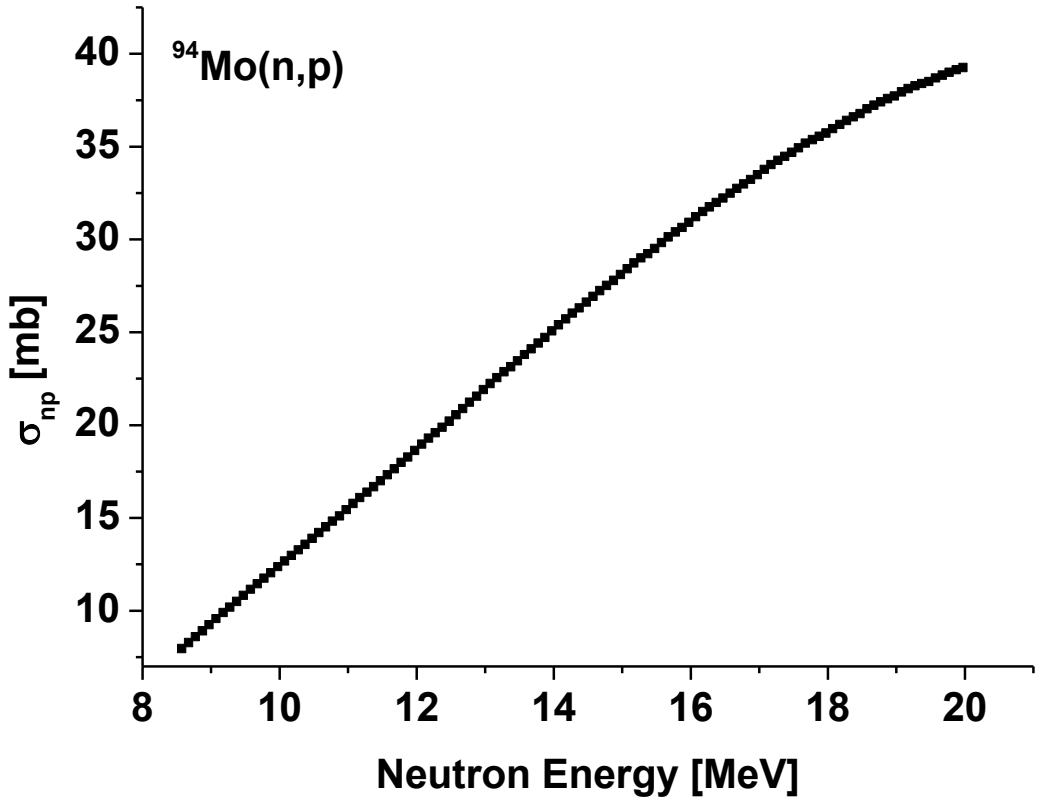
LOW CONTRIBUTION TO THE CS

OBSERVATION:

- CONTRIBUTION OF DIRECT PROCESSES ON DISCRET STATES NEGLECTED BECAUSE THEY ARE ABOUT 10 TIME LOWER THAN THE RESULTS FROM THE FIGURE

4. RESULTS. INCLUSIVE REACTIONS

Compound Processes on Continuum States

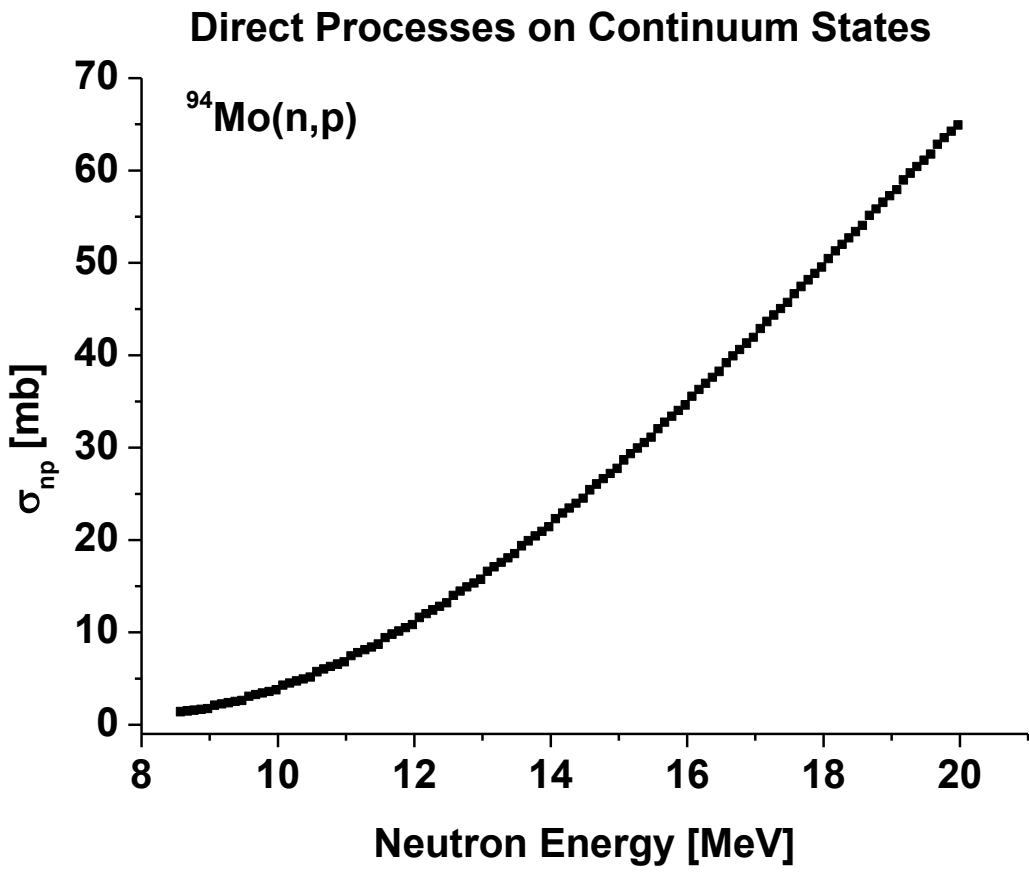


CS HAS THE EXPECTED SHAPE
- IT WILL INCREASES UP TO SOME MAXIMUM AND AFTER THAT WILL SLOWLY DECREASE (NOT REPRESENTED)

CONTINUUM STATES - IMPORTANT

- COULOMB BARRIER FOR CHARGED PARTICLES

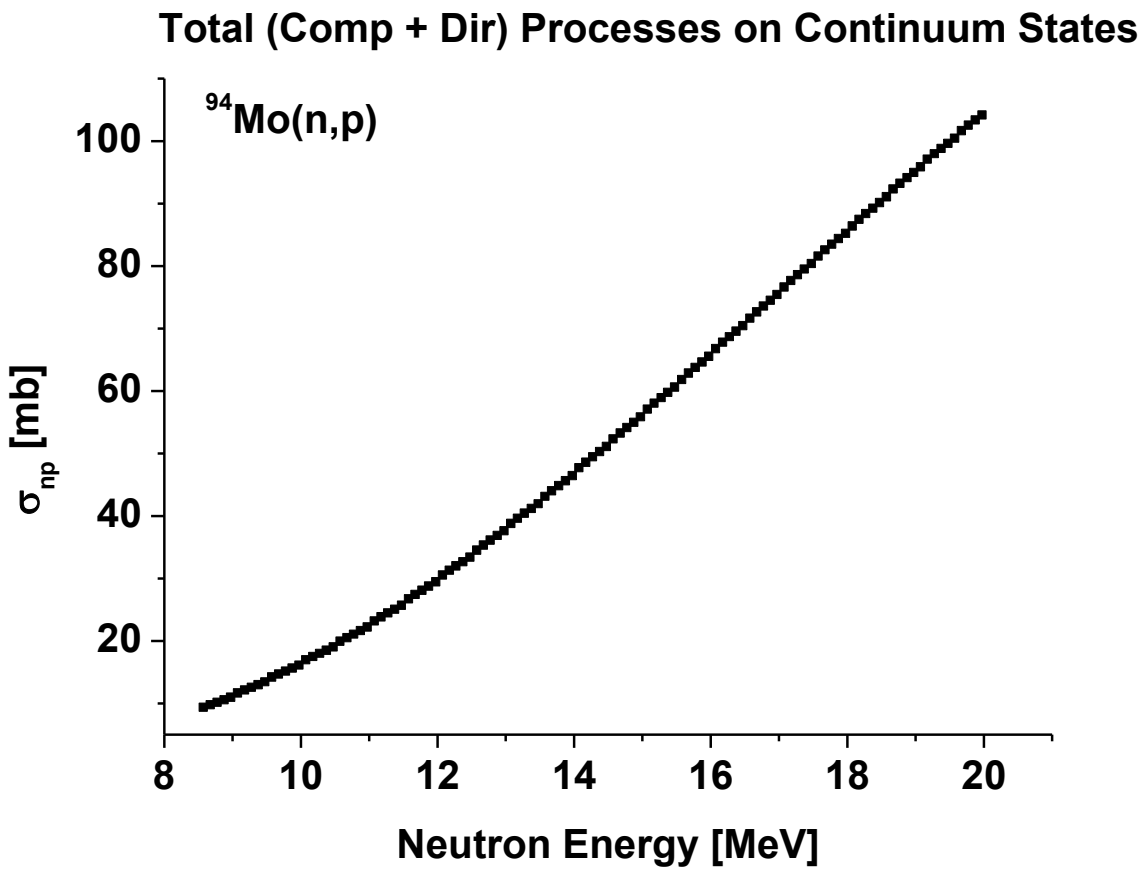
4. RESULTS. INCLUSIVE REACTIONS



DIRECT PROCESSES

- THEIR CONTRIBUTION TO CS IS INCREASING WITH THE INCIDENT ENERGY
- IN THE ANALYSED REACTION DIRECT PROCESSES BECOME DOMINANT WITH THE INCREASING OF THE ENERGY

4. RESULTS. INCLUSIVE REACTIONS



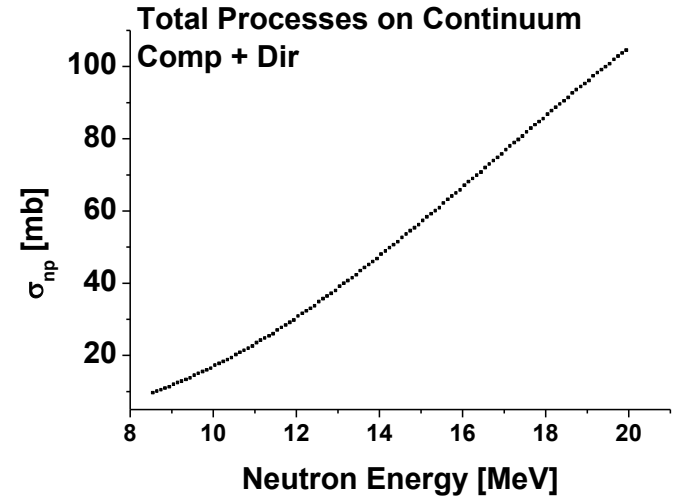
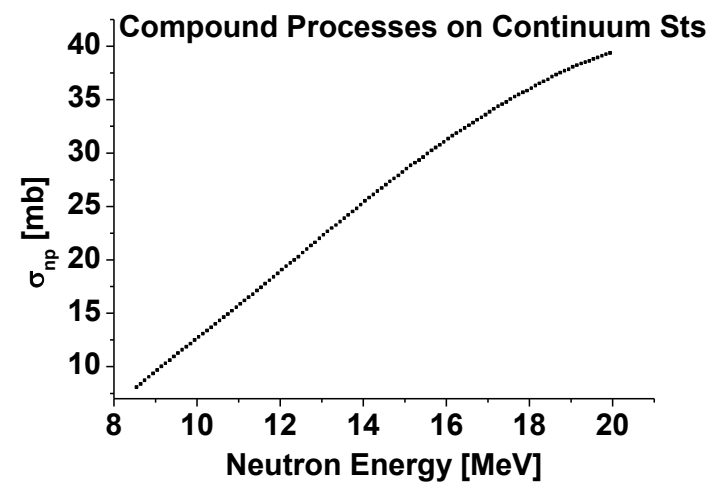
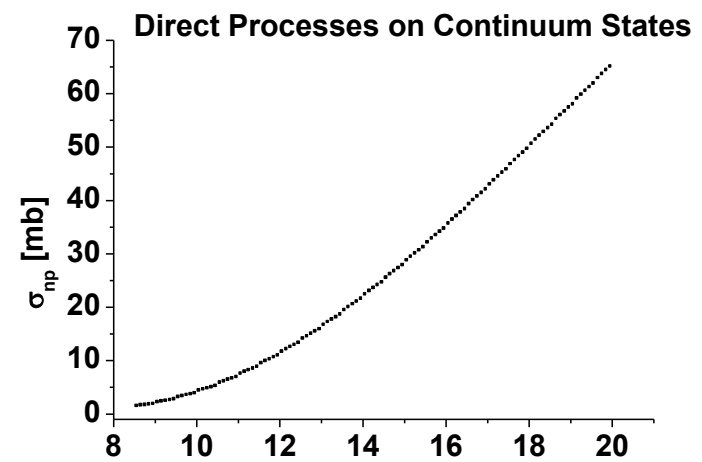
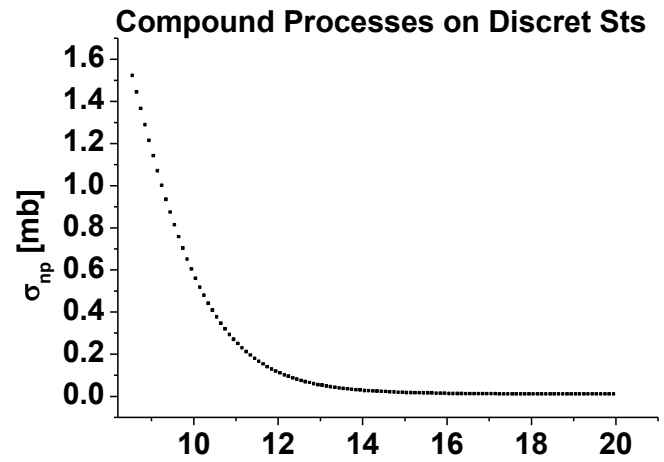
TOTAL CONTRIBUTION TO INC. CROSS SECTION

- NEGLECTED DISCRETE STATES

- CONSIDERED CONTINUUM STATES

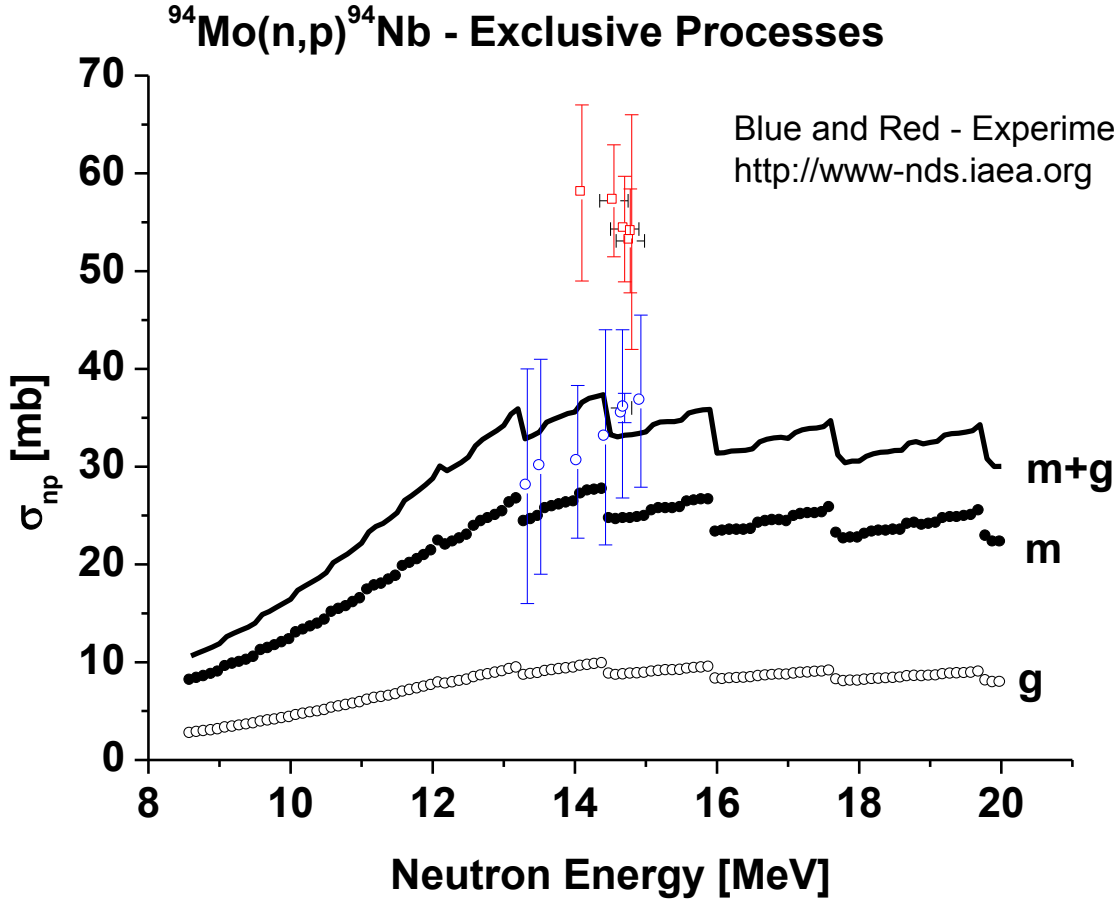
4. RESULTS. INCLUSIVE REACTIONS. ALL EVALUATIONS

$^{94}\text{Mo}(n,p)$ - Inclusive Processes



**THE NUCLEAR REACTION $^{94}\text{Mo}(n,p)^{94}\text{Nb}$:
DIRECT AND COMPOUND MECHANISM ORIGINATED MAINLY BY PRE –
EQUILIBRIUM PROCESSES**

4. RESULTS. EXCLUSIVE REACTIONS



PRODUCTION OF:

- ⁹⁴Nb nucleus in isomer and ground state (m, g)

Standard Talys Input:

- Potentials
- Density Levels

Experimental Data:

- Described Well
- Further Analysis of Experimental Data and Talys Input Parameters

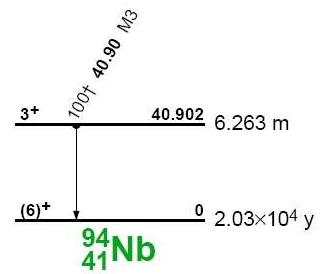
Cross Section of Isomer and Ground States of ⁹⁴Nb

Isomer Ratio

R = 2.852 ± 0.013 – Incident Neutron Flux = 1

R = 2.860 ± 0.010 – Incident Neutron Flux ~ 1/E^{0.9}

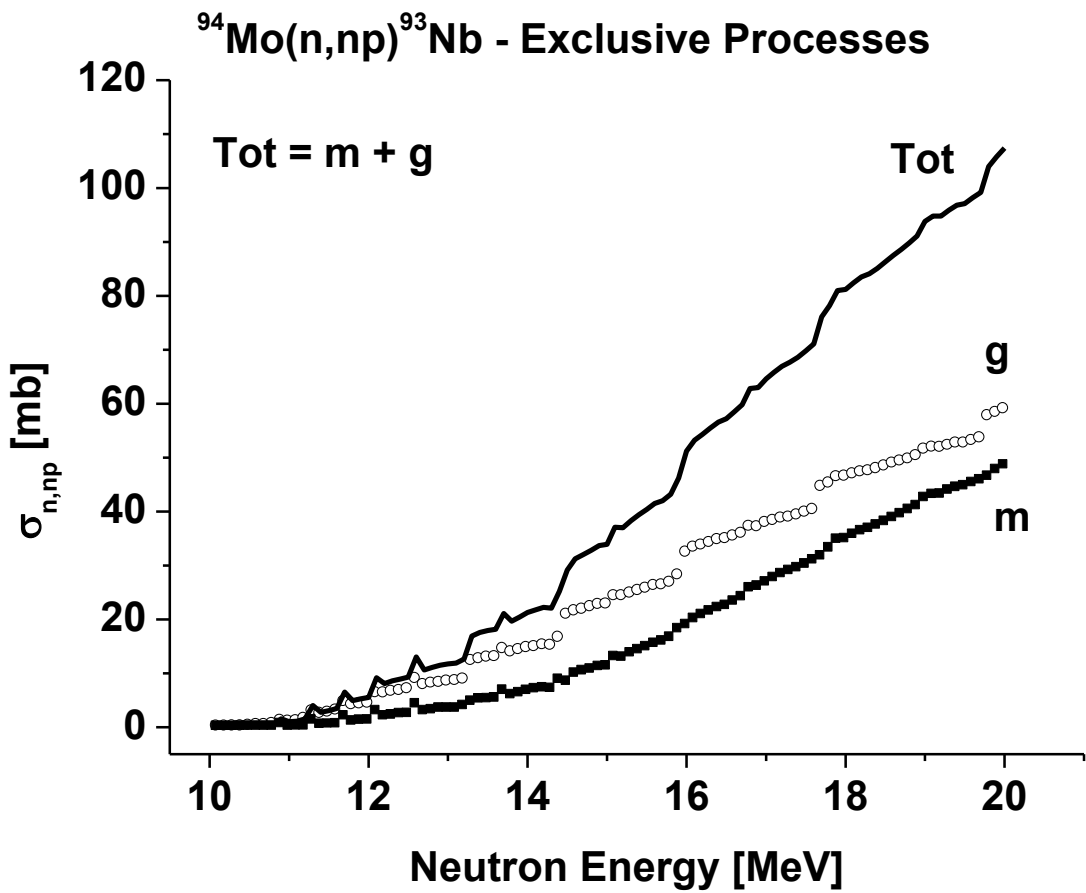
Gamma Transitions E_γ = 0.0409 MeV



4. RESULTS. EXCLUSIVE REACTIONS. CONCURRENT PROCESSES

In the $^{94}\text{Mo}(n,p)^{94}\text{Nb}$ Reactions for Incident Neutrons from Threshold up to 20 MeV many channels are open

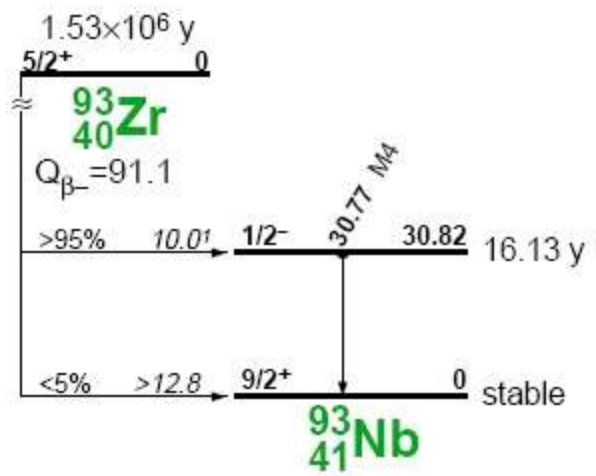
- 2 channels: $^{94}\text{Mo}(n,np)^{93}\text{Nb}$ ($Q=-8.49$ MeV) and $^{94}\text{Mo}(n,2n)^{93}\text{Mo}$ ($Q=-9.67$ MeV)



$$R = 1.51 \pm 0.025 - \text{Neutron Flux} = 1$$

CS of (n,p), (n,np) and (n,2n) are of the same order of magnitude

Gamma Transitions $E_\gamma = 0.0307$ MeV

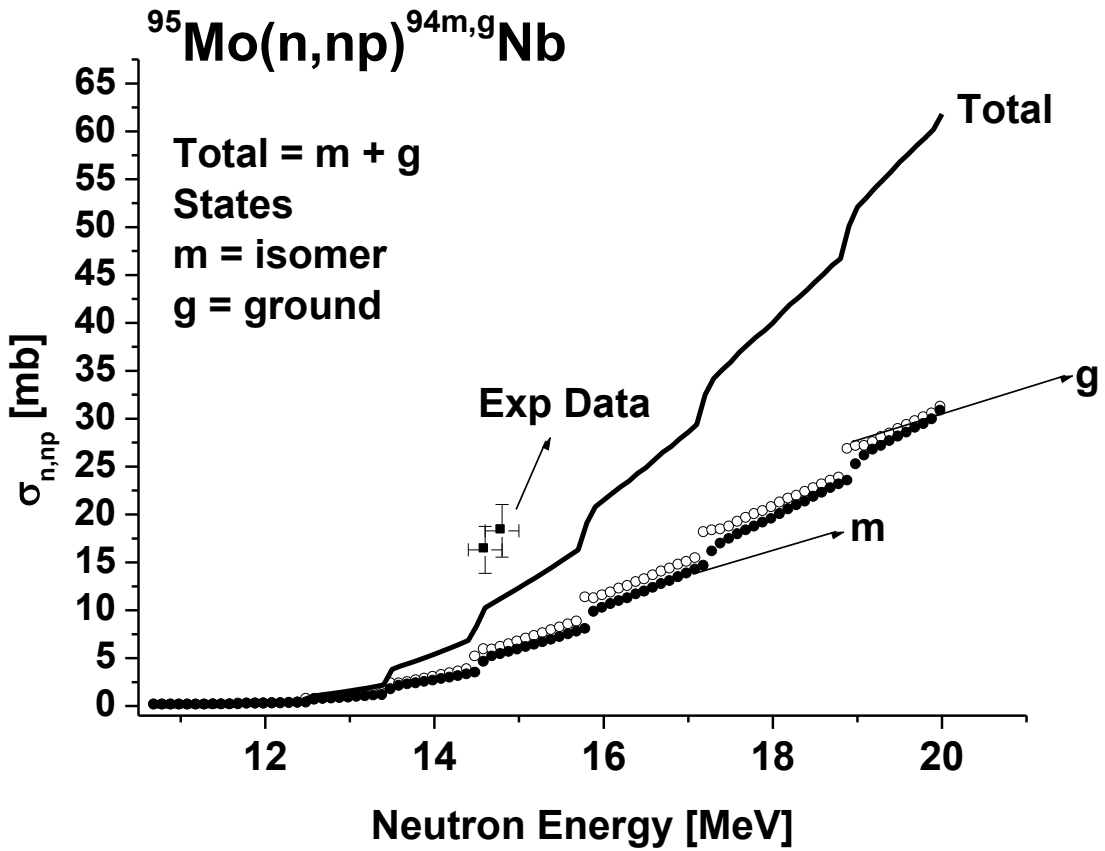


4. RESULTS. EXCLUSIVE REACTIONS. SECOND WAY OF ⁹⁴Nb PRODUCTION

⁹⁴Nb isotopes – obtained by ⁹⁵Mo(n,np)⁹⁴Nb reaction (Q= - 8.63 MeV)

Realized an analyze of Inclusive and Exclusive Reactions

Presented only the main Results on Exclusive Reactions



Concurrence between Direct and Compound Processes of Pre – Equilibrium origin mainly

CS close to ⁹⁴Mo(n,p)

High Energy part dominated by Direct Processes -> Increasing of High Energy Region

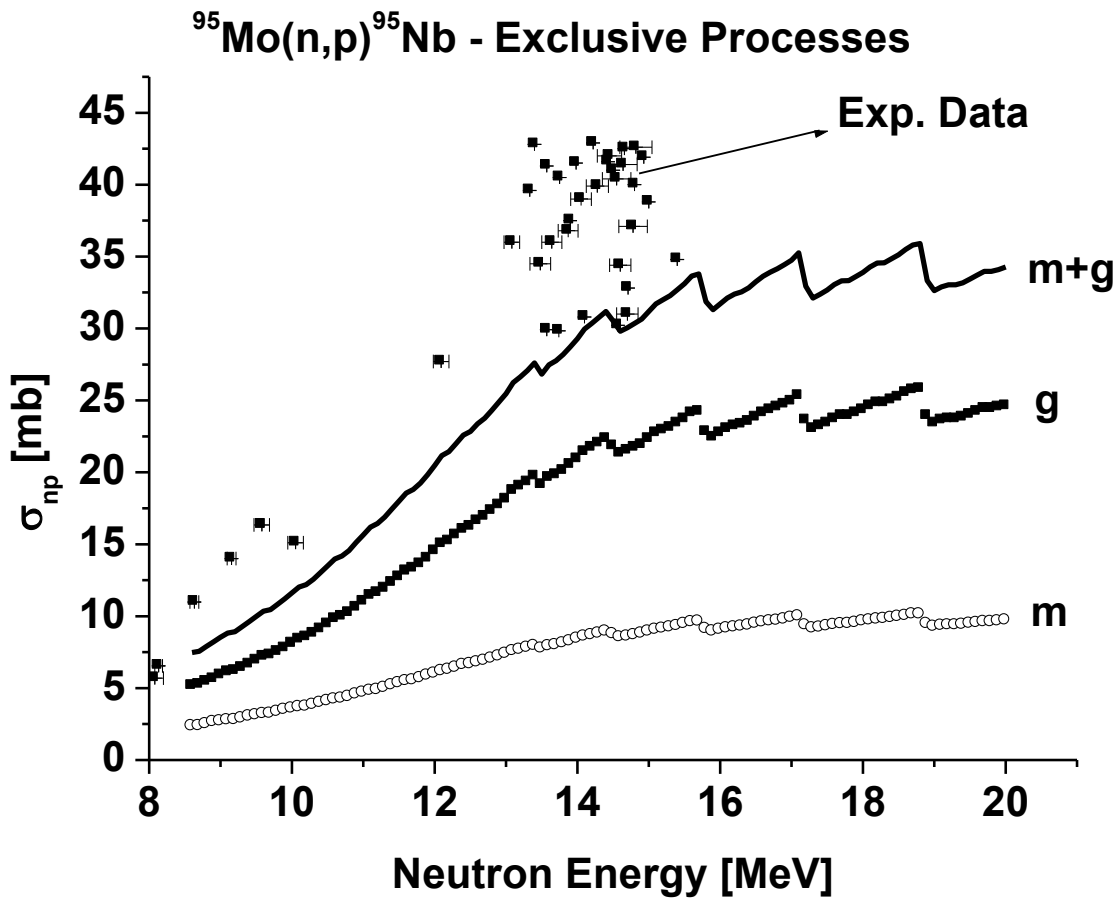
Isomer Ratio
 - Neutron Flux = 1
 $R = 0.927 \pm 0.019$
 - Neutron Flux $\sim 1/E^{0.9}$
 $R = 0.923 \pm 0.018$

4. RESULTS. EXCL REACTIONS. ⁹⁴Nb PRODUCTION. CONCURRENT PROCESSES

Concurrent Processes:

- ⁹⁵Mo(n,p)⁹⁵Nb (Q = - 0.1432 MeV);
- ⁹⁵Mo(n,2np)⁹³Nb (Q = -15.857 MeV)

Exclusive Processes for ⁹⁵Mo(n,p)⁹⁵Nb



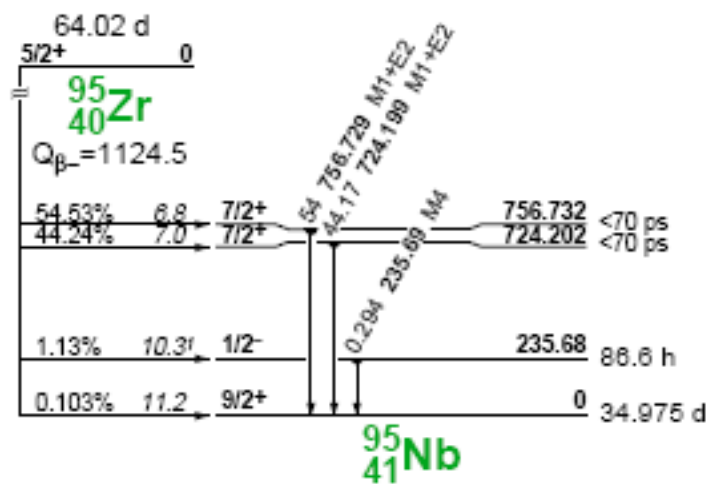
Production of ⁹⁵Nb

Standard Talys Input – Acceptable
Description of Experimental Data

Isomer Ratio

Neutron Flux = 1
 $R = 0.4024 \pm 0.025$
 Gam. Tr. $E_\gamma = 0.2356$ MeV

(n,2np)–importance at 17–20 MeV



4. RESULTS. EXCL REACTIONS. TALYS POTENTIAL PARAMETERS

Cross Sections Evaluation Realized with Standard Input of Talys

Wood – Saxon Potential Parameters – $^{94}\text{Mo}(n,p)^{94}\text{Nb}$

n + ^{94}Mo channel

V [MeV]	r_v [fm]	a_v [fm ⁻¹]	W [MeV]	r_w [fm]	a_w [fm ⁻¹]	V_{so} [MeV]	r_{vso} [fm]	a_{vso} [fm ⁻¹]
50.99	1.22	0.658	0.16	1.22	0.658	5.99	1.05	0.58

p + ^{94}Nb channel

V [MeV]	r_v [fm]	a_v [fm ⁻¹]	W [MeV]	r_w [fm]	a_w [fm ⁻¹]	V_{so} [MeV]	r_{vso} [fm]	a_{vso} [fm ⁻¹]
61.94	1.215	0.664	0.13	1.215	0.664	6.03	1.043	0.59

4. RESULTS. EXCL REACTIONS. TALYS POTENTIAL PARAMETERS

Cross Sections Evaluation Realized with Standard Input of Talys

Wood – Saxon Potential Parameters – $^{95}\text{Mo}(n,np)^{94}\text{Nb}$

n + ^{95}Mo channel

V [MeV]	r_v [fm]	a_v [fm⁻¹]	W [MeV]	r_w [fm]	a_w [fm⁻¹]	V_{so} [MeV]	r_{vso} [fm]	a_{vso} [fm⁻¹]
51.27	1.215	0.664	0.16	1.215	0.664	5.99	1.044	0.59

p + ^{94}Nb channel

V [MeV]	r_v [fm]	a_v [fm⁻¹]	W [MeV]	r_w [fm]	a_w [fm⁻¹]	V_{so} [MeV]	r_{vso} [fm]	a_{vso} [fm⁻¹]
62.10	1.215	0.664	0.13	1.215	0.664	6.03	1.044	0.59

4. RESULTS. ACTIVITIES. ISOMER RATIO MEASUREMENTS

MODEL - REAL TARGET OF 1 CM X 1 CM X 0.1 CM

DESINSITY – 10.28 g/cm³

Goal – Activity obtained in Experiment at Different Energies

⁹⁵ Mo(n,np) ^{94m} Nb			⁹⁵ Mo(n,np) ^{94g} Nb			⁹⁵ Mo(n,p) ^{95m} Nb			⁹⁵ Mo(n,p) ^{95g} Nb		
E _n [MeV]	σ [mb]	A _{obs} [dez]	σ [mb]	A _{obs} [dez]	σ [mb]	A _{obs} [dez]	σ [mb]	A _{obs} [dez]			
14.1	5.76	1.86 · 10 ⁶	3.09	1.7 · 10 ⁻³	8.56	9818	6.95	7			
20	61.8	2.00 · 10 ⁷	31.1	1.7 · 10 ⁻²	9.67	1109	48.5	47			

$$\tau_m = 6.263\text{m}; \tau_g = 2.03 \cdot 10^6\text{y}$$

$$\tau_m = 86.6\text{ h}; \tau_g = 34.975\text{ d}$$

Irradiation time = 3 min; Cooling time = 3 min; Counting time = 5 min

4. RESULTS. ACTIVITIES. ISOMER RATIO MEASUREMENTS

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E _n [MeV]	σ [mb]	A _{obs} [dez]	σ [mb]	A _{obs} [dez]	σ [mb]	A _{obs} [dez]	σ [mb]	A _{obs} [dez]
14.1	27.1	8.75 · 10 ⁶	9.48	6.4 · 10 ⁻³	6.95	0	6.95	0
20	22.2	7.17 · 10 ⁵	7.83	4.3 · 10 ⁻³	9.67	0	48.5	0

$$\tau_m = 6.263\text{m}; \tau_g = 2.03 \cdot 10^6\text{y}$$

$$\tau_m = 16.13\text{ y}; \tau_g = \text{stable}$$

Irradiation time = 3 min; Cooling time = 3 min; Counting time = 5 min

Talys – for gamma and neutrons induced reactions activities and yields calculations on sample target are not implemented

Activities are evaluated by us – simple model of isomer ratios measurements

Results suggest the possibility of the isomer ratio measurements

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5. DISCUSSIONS

Analyzed Nuclear Reactions Induced by Fast Neutrons for:

Fast Neutrons Activation and Isomer Ratio Evaluation

Reactions: $^{94}\text{Mo}(n,p)^{94}\text{Nb}$ and $^{95}\text{Mo}(n,np)^{94}\text{Nb}$

For mentioned Processes were Evaluated with Talys:

- Cross Sections (Inclusive and Exclusive)
- Isomer Ratios
- Activities and Yields on Simple Modeled Measurements

Comparison with Existing Experimental Data

- using a Standard Talys Input the CS Evaluation are in well and / or acceptable

Accordance with Existing Experimental Data

- For many Evaluations like CS productions of isomer and isotopes and Isomer Ratios – no experimental data
- Obtained New Nuclear Data on Potential and Level Densities Parameters

Cross Sections – by Talys

6. CONCLUSIONS

Talys – Rapid and Efficient Codes for Evaluation of Nuclear Data

(Reaction Models ->Cross Section and Nuclear Structure)

Necessary a Better Description of Experimental Data on Analyzed Processes

Fast Neutrons – Obtained New Theoretical Evaluation on Isomer Production and Isomer Ratios - > New Measurements and Experiments

Improvement of Experimental and Theoretical Data for Tagged Neutrons Method
Necessary to test New Elements

Necessary of use Computer Codes for Experiment Simulations – GEANT4

- Activities, Yields and other

Present Evaluations

- Experiment Proposal at JINR Dubna Facilities

- LNF JINR Dubna Facilities – IREN, IBR-2

- LNR JINR Dubna – Microtron MT-25

**THANK YOU VERY MUCH
FOR YOUR ATTENTION! 😊**

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