



## **ISINN-28 Agenda**

**P-even T-odd asymmetries in differential cross sections of fission reactions of nonorientied nuclei by cold polarized neutrons with emission of prescission and evaporation light particles**

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## Purpose of work

Demonstration of the possibility of describing the characteristics of P - even T - odd asymmetries in the differential cross sections of fission reactions of nonoriented target nuclei by cold polarized neutrons with the emission of light particles, such as precession  $\alpha$  - particles and prompt neutrons and  $\gamma$  - quanta in the framework of the quantum theory of fission using a single mechanism the appearance of these asymmetries, due to the influence of the Coriolis interaction of the total spin of a composite fissile nucleus on fission fragments and light particles.

## Introduction

In paper [Jessinger P., Koetzle A., Gonnenwein F. et al. // Phys. At. Nucl. 2002. V. **65**. P. 662.], the differential cross section  $d\sigma_{nf,p}/d\Omega$  was represented as

$$d\sigma_{nf,p}/d\Omega = d\sigma_{nf,p}^0/d\Omega + d\sigma_{nf,p}^1/d\Omega, \quad (1)$$

where  $d\sigma_{nf}^0/d\Omega$  is a similar cross section of the reaction under study with the participation of cold nonpolarized neutrons ( $\sigma_n = 0$ ), and  $d\sigma_{nf}^1/d\Omega$  is the component of the differential cross section (1), linearly dependent on  $\sigma_n$ . In this case, the ratio was used:

$$d\sigma_{nf,p}^0/d\Omega = \sigma_{nf}^0 P^0(\theta), \quad (2)$$

where  $\sigma_{nf}^0$  is the total cross section, and  $P^0(\theta)$  is the normalized angular distribution of emitted light particles in the reaction with nonpolarized neutrons.

To describe the asymmetry under consideration, an asymmetry coefficient of  $D(\Omega)$  was introduced, determined by:

$$D(\Omega) = \left( \frac{d\sigma_{nf,p}^{(+)}}{d\Omega} - \frac{d\sigma_{nf,p}^{(-)}}{d\Omega} \right) / \left( \frac{d\sigma_{nf,p}^{(+)}}{d\Omega} + \frac{d\sigma_{nf,p}^{(-)}}{d\Omega} \right). \quad (3)$$

Using (1), this coefficient can be represented as

$$D(\Omega) = (d\sigma_{nf,p}^{1+}/d\Omega) / (d\sigma_{nf,p}^0/d\Omega). \quad (4)$$

# 1. Characteristics of P - even T-odd asymmetries in the differential cross sections of nuclear fission reactions with the escape of precession $\alpha$ -particles

The normalized angular distribution of  $\alpha$  - particles,  $P^0(\theta)$ , is the unperturbed component of cross section (2) and has the form:

$$P^0(\theta) = |A^0(\theta)|^2 = \left| \sum_l d_l Y_{l0}(\theta) \right|^2 = \left| \sum_l \{d_l\} e^{i\delta_l} Y_{l0}(\theta) \right|^2, \quad (5)$$

where  $\{d_l\}$  and  $\delta_l$  are the main value and the phase of the value  $d_l$ .

$$A^0(\theta) = A_-^0(\theta) + A_+^0(\theta), \quad (6)$$

$$P^0(\theta) = P_-^0(\theta) + P_+^0(\theta), \quad (7)$$

where even  $P_-^0(\theta)$  and odd  $P_+^0(\theta)$  components of the angular distribution  $P^0(\theta)$ , taking into account (5-6), are represented as

$$P_-^0(\theta) = \{A_-^0(\theta)\}^2 + \{A_+^0(\theta)\}^2; \quad P_+^0(\theta) = 2\{A_-^0(\theta)\}\{A_+^0(\theta)\}. \quad (8)$$

# 1. Characteristics of P - even T-odd asymmetries in the differential cross sections of nuclear fission reactions with the escape of precession $\alpha$ -particles

In [*Kadmensky S.G., Titova L.V., Bunakov V.E. // Phys. Atom. Nucl.* 2019. V. **82**. № 3. P. 254; *Kadmensky S.G., Bunakov V.E., Lyubashevsky D.E. // Bull. Russ. Acad. Sci. Phys.* 2019. V. **83**. № 9. P. 1128.; *Kadmensky S.G., Lyubashevsky D.E., Kostryukov P.V. // Phys. Atom. Nucl.* 2019. V. **82**, № 3. P. 267.], the component of the differential cross section (1)  $d\sigma_{nf,\alpha}^1/d\Omega$ , taking into account the influence of the Coriolis interaction of the total spin of a composite fissile nucleus with the orbital angular momenta of fission fragments and a  $\alpha$  - particle, can be represented in terms of the sum of the derivatives of the unperturbed angular distributions  $\alpha$  - particles  $P_-^0(\theta)$  and  $P_+^0(\theta)$  included in (7) as

$$\frac{d\sigma_{nf,\alpha}^1}{d\Omega} = \left( \frac{d\sigma_{nf,\alpha}^1}{d\Omega} \right)_- + \left( \frac{d\sigma_{nf,\alpha}^1}{d\Omega} \right)_+ = \Delta_{\alpha,-} \sigma_{nf}^0 \frac{d(P_-^0(\theta))}{d\theta} + \Delta_{\alpha,+} \sigma_{nf}^0 \frac{d(P_+^0(\theta))}{d\theta}. \quad (9)$$

# 1. Characteristics of P - even T-odd asymmetries in the differential cross sections of nuclear fission reactions with the escape of precession $\alpha$ -particles

Since the dependences of  $P_-^0(\theta)$  and  $P_+^0(\theta)$  on angles can be described by sums of the form  $\sum_n A_n (\cos \theta)^n$  with even  $n = 0, 2, 4, \dots$  and odd  $n = 1, 3, 5, \dots$  values of  $n$ , respectively, it can be shown

that the quantities  $\frac{d(P_+^0(\theta))}{d\theta}$  and  $\frac{d(P_-^0(\theta))}{d\theta}$  included in (9) are represented as

$$\left( \frac{d\sigma_{nf,\alpha}^1}{d\Omega} \right)_+ = B_+(\theta) \sin(\theta); \quad \left( \frac{d\sigma_{nf,\alpha}^1}{d\Omega} \right)_- = B_-(\theta) \cos(\theta) \sin(\theta), \quad (10)$$

where the coefficients  $B_-(\theta)$  and  $B_+(\theta)$  are related to the sums of the quantities  $\cos^n(\theta)$  with even values of  $n$ . Therefore, the quantities considered in (10) satisfy the symmetry conditions:

$$\left( \frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega} \right)_+ = \left( \frac{d\sigma_{nf,\alpha}^1(\pi - \theta)}{d\Omega} \right)_+; \quad \left( \frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega} \right)_- = - \left( \frac{d\sigma_{nf,\alpha}^1(\pi - \theta)}{d\Omega} \right)_-. \quad (11)$$

# 1. Characteristics of P - even T-odd asymmetries in the differential cross sections of nuclear fission reactions with the escape of precession $\alpha$ -particles

Then the differential sections  $\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_+$  and  $\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_-$  (10) can be represented by:

$$\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_+ = B_+(\theta)(\sigma_n[\mathbf{k}_{LF}, \mathbf{k}_\alpha]); \quad \left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_- = B_-(\theta)(\sigma_n[\mathbf{k}_{LF}, \mathbf{k}_\alpha])(\mathbf{k}_{LF}, \mathbf{k}_\alpha). \quad (12)$$

Using the relationship of equation (4) for the asymmetry coefficient  $D(\theta)$  with (2, 9) and the symmetry condition (11), we can obtain the relations:

$$\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_\pm = 1/2 \left[ D(\theta) \frac{d\sigma^0(\theta)}{d\Omega} \pm D(\pi - \theta) \frac{d\sigma^0(\pi - \theta)}{d\Omega} \right]. \quad (13)$$

# 1. Characteristics of P - even T-odd asymmetries in the differential cross sections of nuclear fission reactions with the escape of pre-scission $\alpha$ -particles

Values  $\Delta_{\alpha,-}$  and  $\Delta_{\alpha,+}$  calculated using the  $\chi^2$  - method for target nuclei  $^{233}\text{U}$ ,  $^{235}\text{U}$ ,  $^{239}\text{Pu}$ , and  $^{241}\text{Pu}$

Target nuclei	$\Delta_{\alpha,-}$	$\Delta_{\alpha,+}$	$\Delta_{\gamma}$	$\Delta_n$
$^{233}\text{U}$	0.0003	-0.00033	-0.0003	-0.00065
$^{235}\text{U}$	0.0015	0.0016	0.0021	0.0012
$^{239}\text{Pu}$	0.00017	0.0001		
$^{241}\text{Pu}$	0.00021	0.0005		



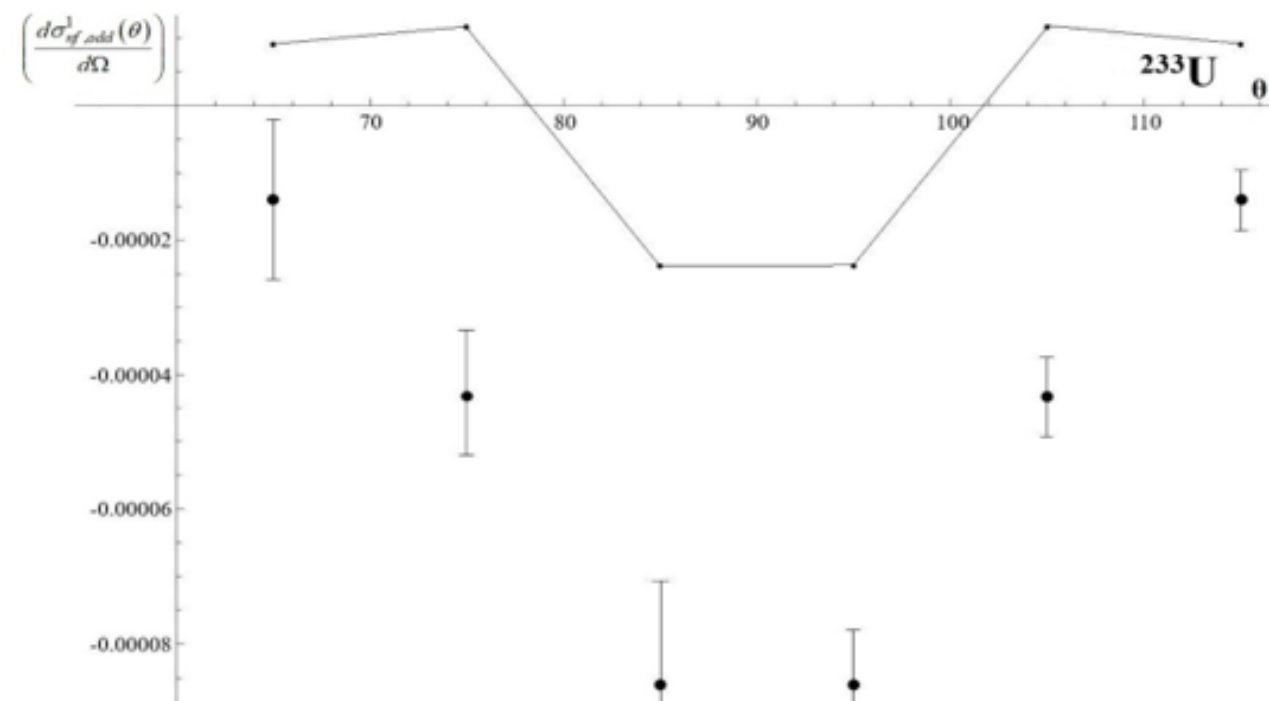


Fig. 1. Experimental (closed circles) and calculated within the framework of the quantum approach - continuous line cross section  $\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_+$  for the  $^{233}\text{U}$  target nucleus

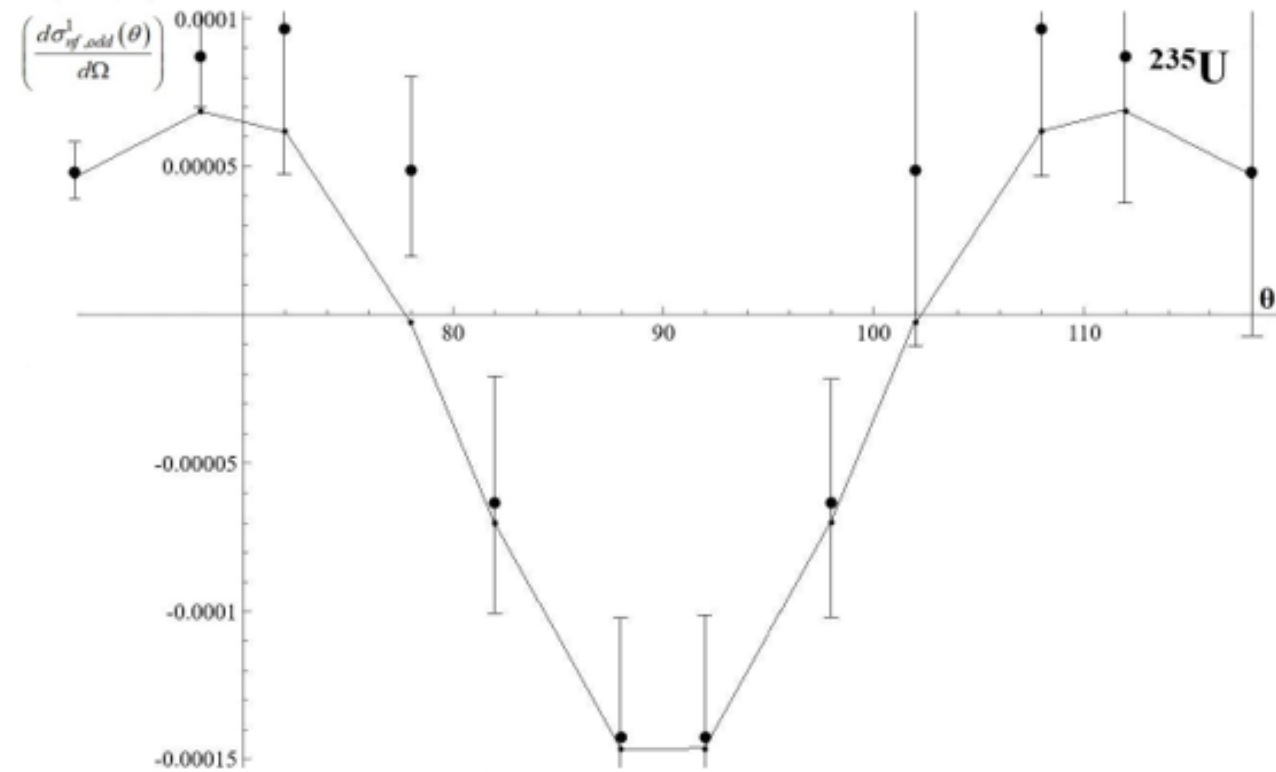


Fig. 2. Experimental (closed circles) and calculated within the framework of the quantum approach - continuous line cross section  $\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_+$  for the  $^{235}\text{U}$  target nucleus

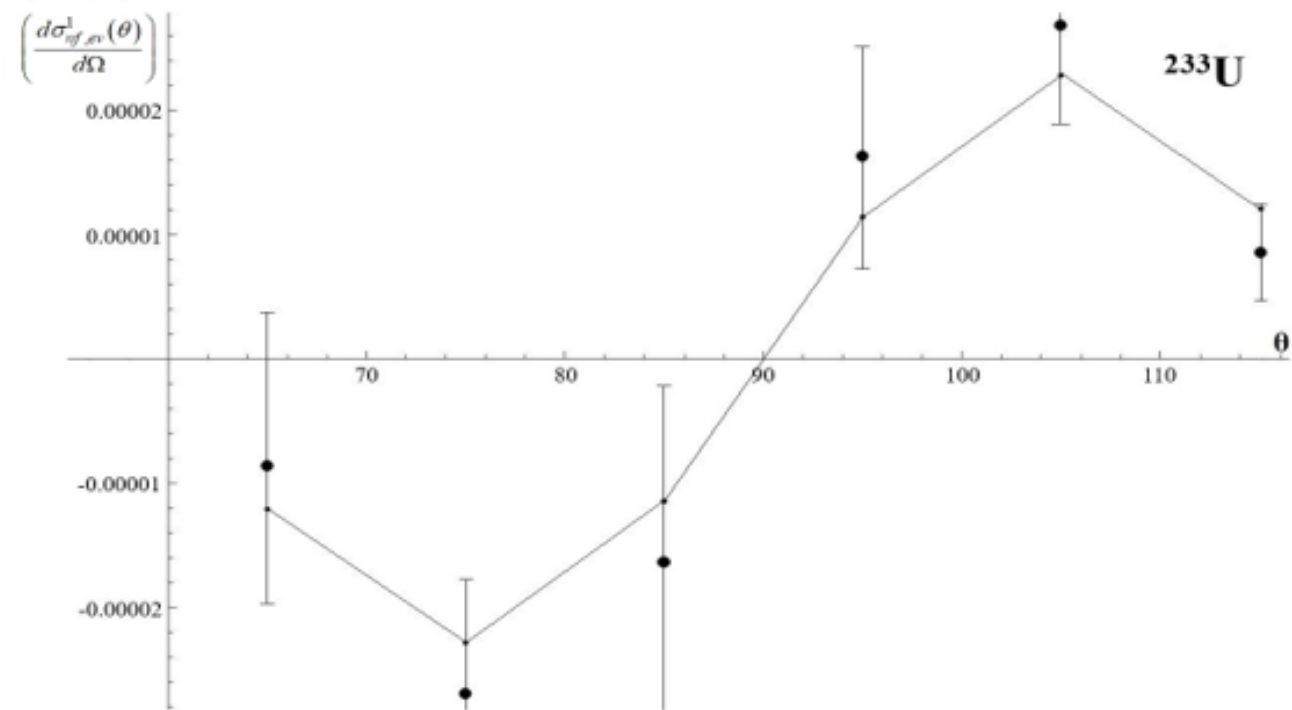


Fig. 3. Experimental (closed circles) and calculated within the framework of the quantum approach - continuous line cross section  $\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_-$  for the  $^{233}\text{U}$  target nucleus

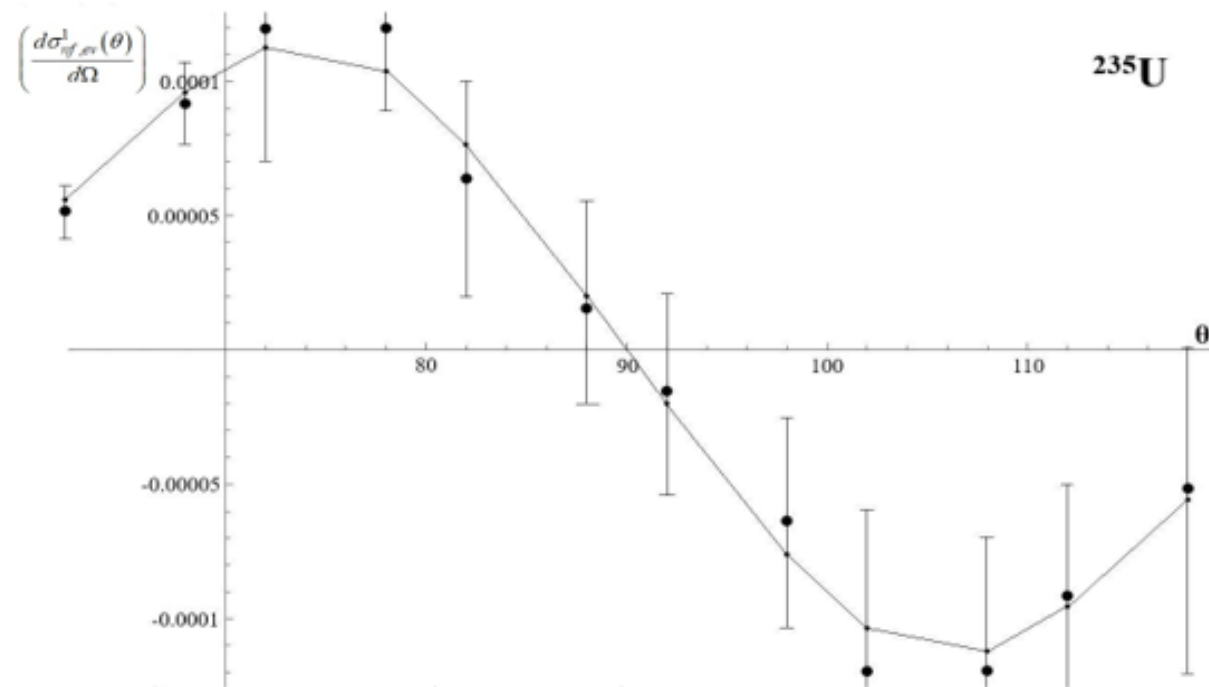


Fig. 4. Experimental (closed circles) and calculated within the framework of the quantum approach - continuous line cross section  $\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_-$  for the  $^{235}\text{U}$  target nucleus

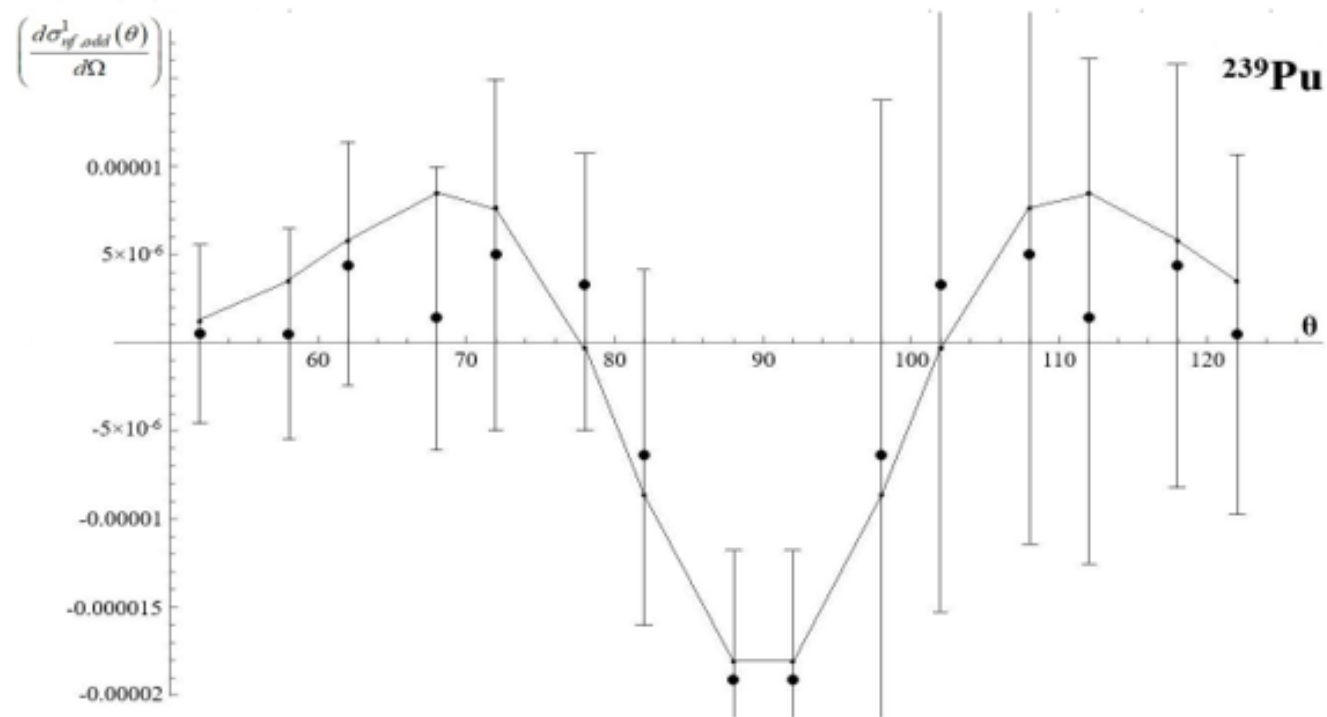


Fig. 5. Experimental (closed circles) and calculated within the framework of the quantum approach - continuous line cross section  $\left(d\sigma_{nf,\alpha}^1(\theta)/d\Omega\right)_+$  for the  $^{239}\text{Pu}$  target nucleus

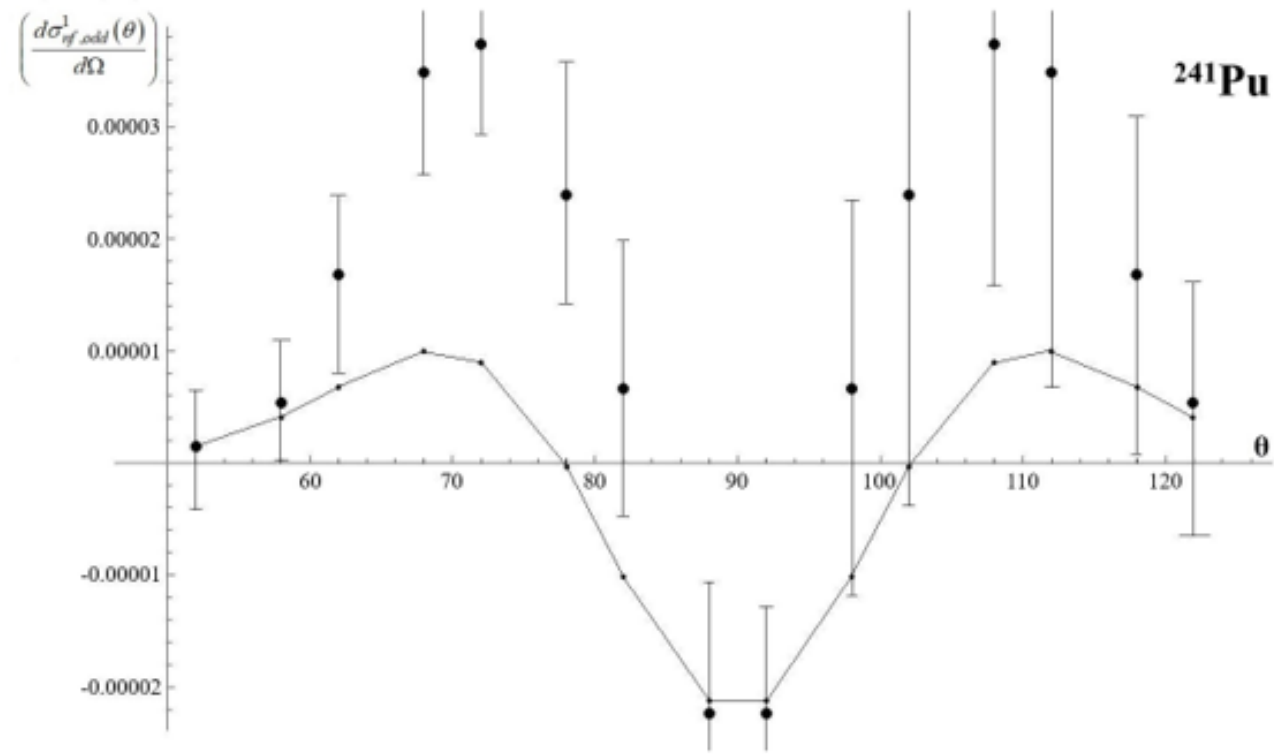


Fig. 6. Experimental (closed circles) and calculated within the framework of the quantum approach - continuous line cross section  $\left( \frac{d\sigma_{rf,\alpha}^1(\theta)}{d\Omega} \right)_+$  for the  $^{241}\text{Pu}$  target nucleus

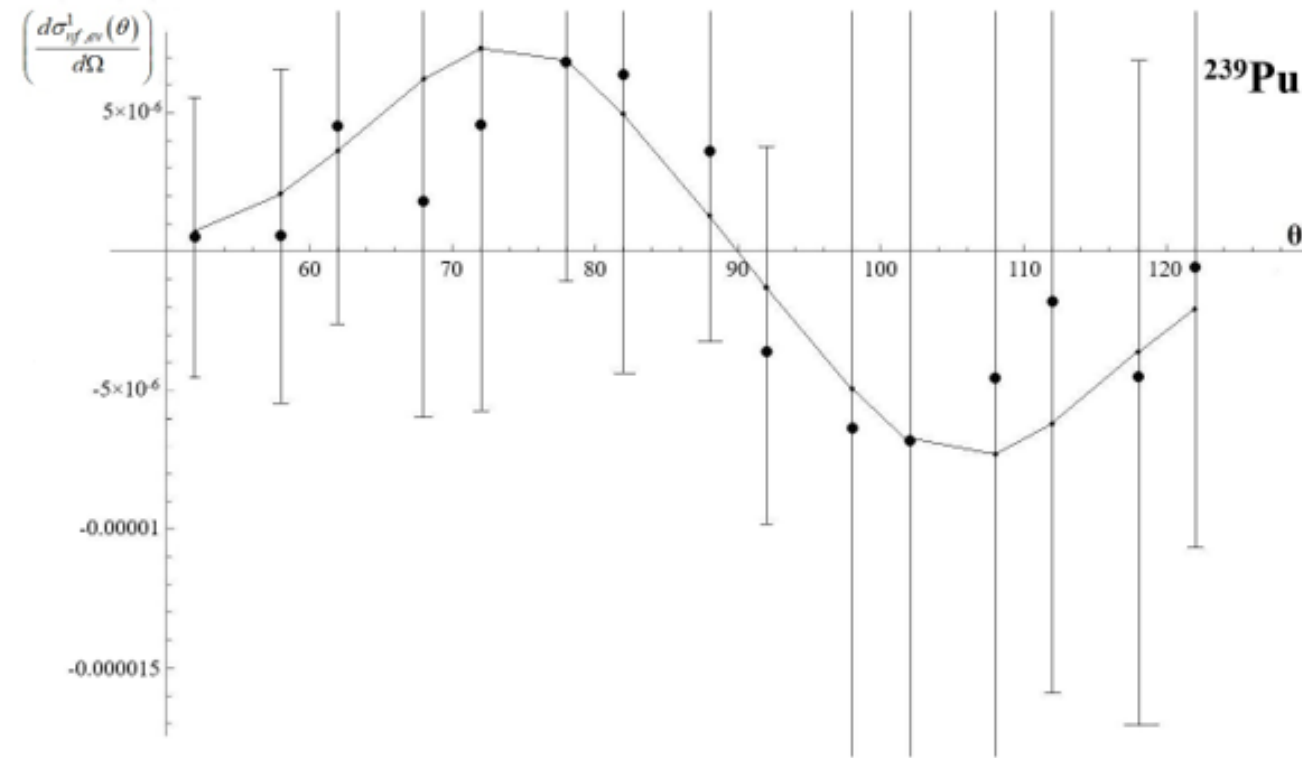


Fig. 7. Experimental (closed circles) and calculated within the framework of the quantum approach - continuous line cross section  $\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_-$  for the  $^{239}\text{Pu}$  target nucleus

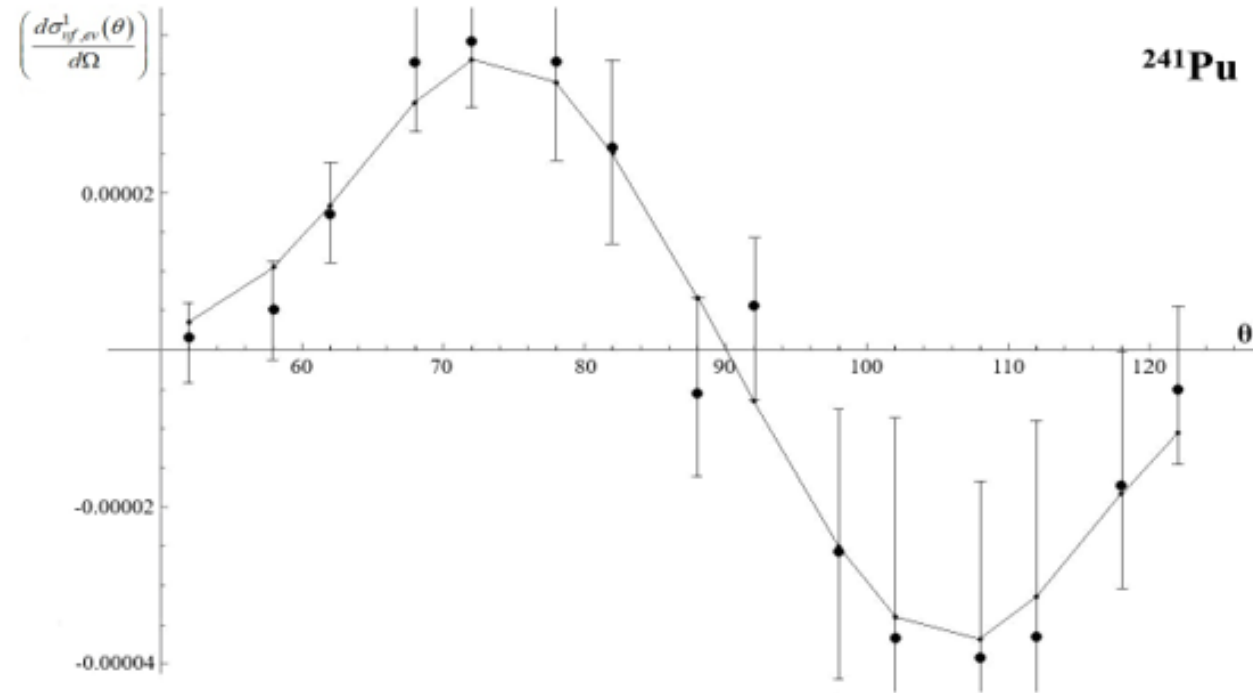


Fig. 8. Experimental (closed circles) and calculated within the framework of the quantum approach - continuous line cross section  $\left(\frac{d\sigma_{nf,\alpha}^1(\theta)}{d\Omega}\right)_-$  for the  $^{241}\text{Pu}$  target nucleus



## 2. Characteristics of P - even T - odd asymmetries in the differential cross sections of nuclear fission reactions with the emission of prompt gamma quanta and neutrons

The unperturbed experimental angular distributions  $P^0(\theta)$  of prompt neutrons and  $\gamma$  - quanta are determined by:

$$P^0(\theta) \sim (1 + A \cos^2 \theta), \quad (14)$$

where  $\theta$  is the angle between the direction of emission of prompt neutrons ( $\gamma$  - quanta) and the direction of emission of a light fission fragment. Since in this case  $P^0(\theta) = P_-^0(\theta)$ , using (9) for an even component  $\left(d\sigma_{nf,p}^1/d\Omega\right)_-$  we can get:

$$\left(\frac{d\sigma_{nf,p}^1(\theta)}{d\Omega}\right)_- = \Delta_{n,\gamma} \frac{dP^0(\theta)}{d\theta}, \quad (15)$$

where  $\Delta_n$  ( $\Delta_\gamma$ ) are the angles of rotation of the wave vectors of the prompt neutron  $\mathbf{k}_n$  ( $\gamma$  - quantum  $\mathbf{k}_\gamma$ ) relative to the direction of the wave vector  $\mathbf{k}_{LF}$  of the light fission fragment.

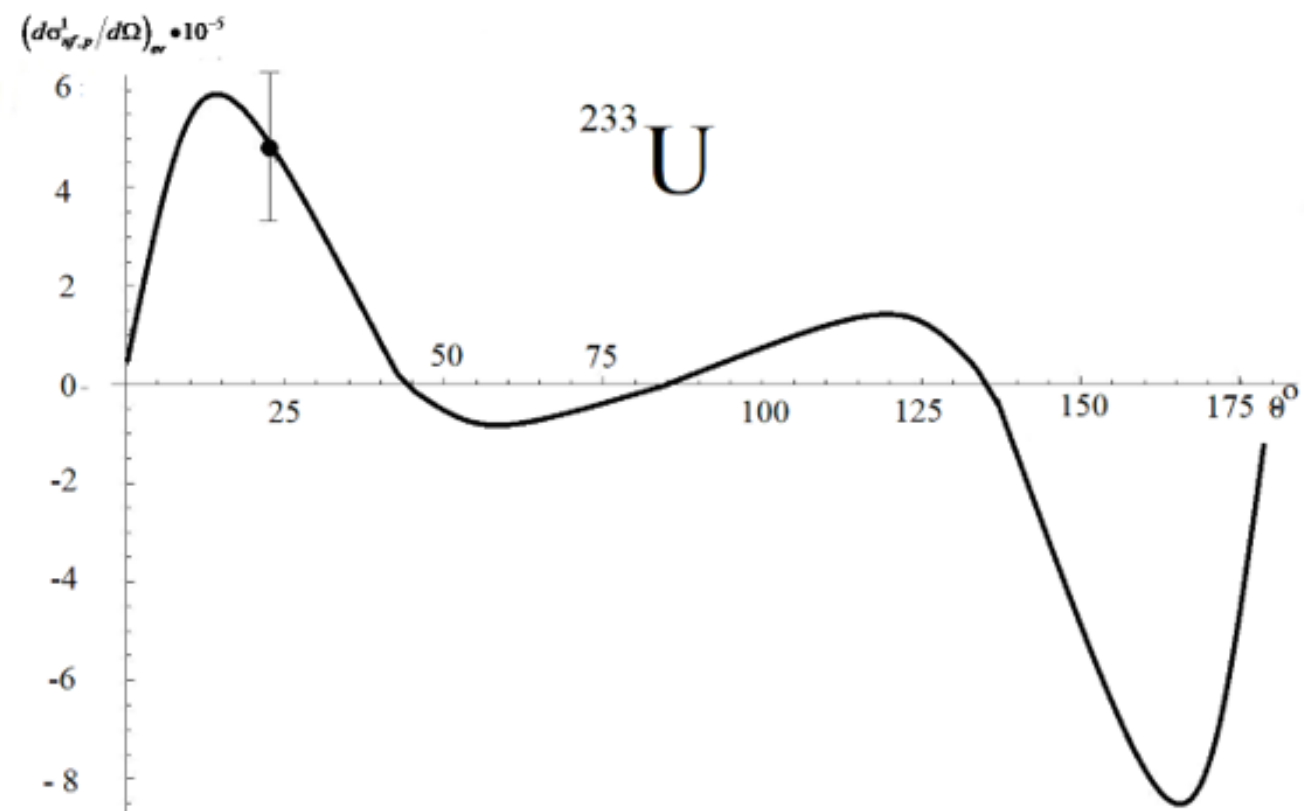


Fig. 9. Cross section  $(d\sigma_{nf,p}^1/d\Omega)_{-}$  for  $^{233}\text{U}$  neutrons

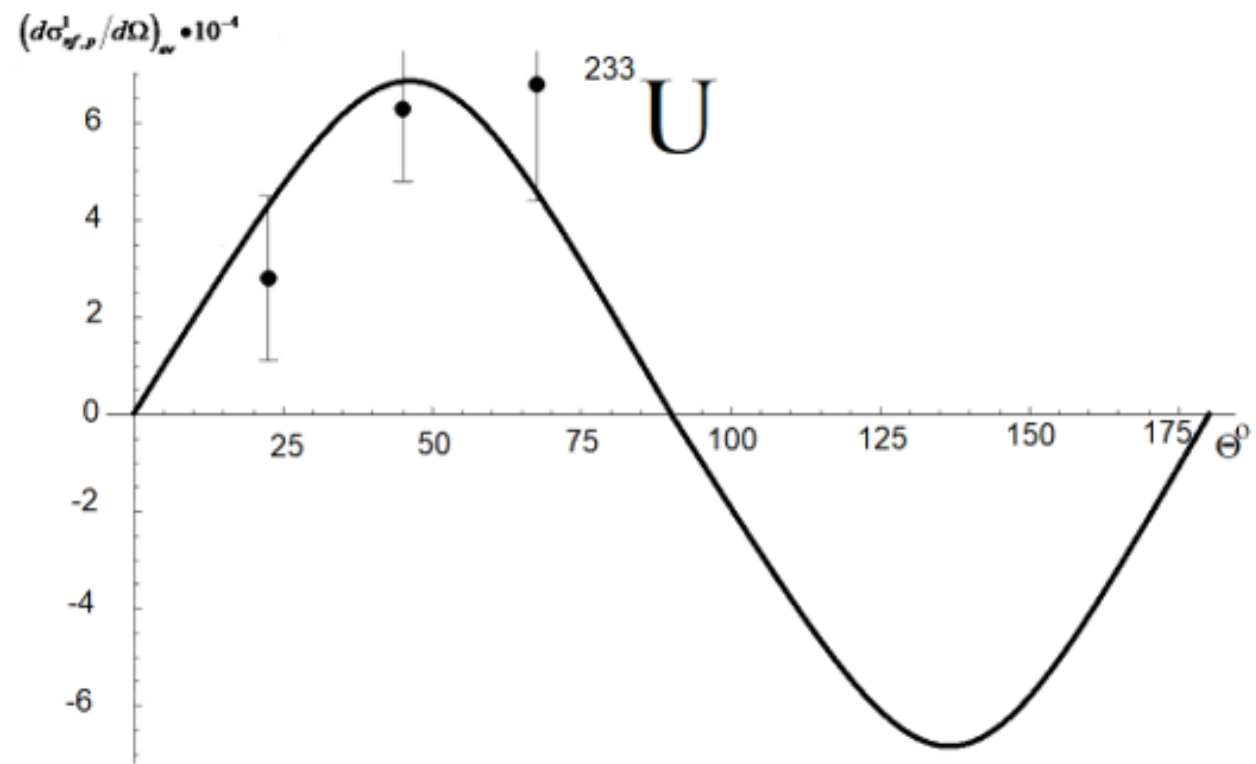


Fig. 10. Cross section  $(d\sigma_{nf,p}^1/d\Omega)_-$  for evaporative  $^{233}\text{U}$   $\gamma$  - quanta

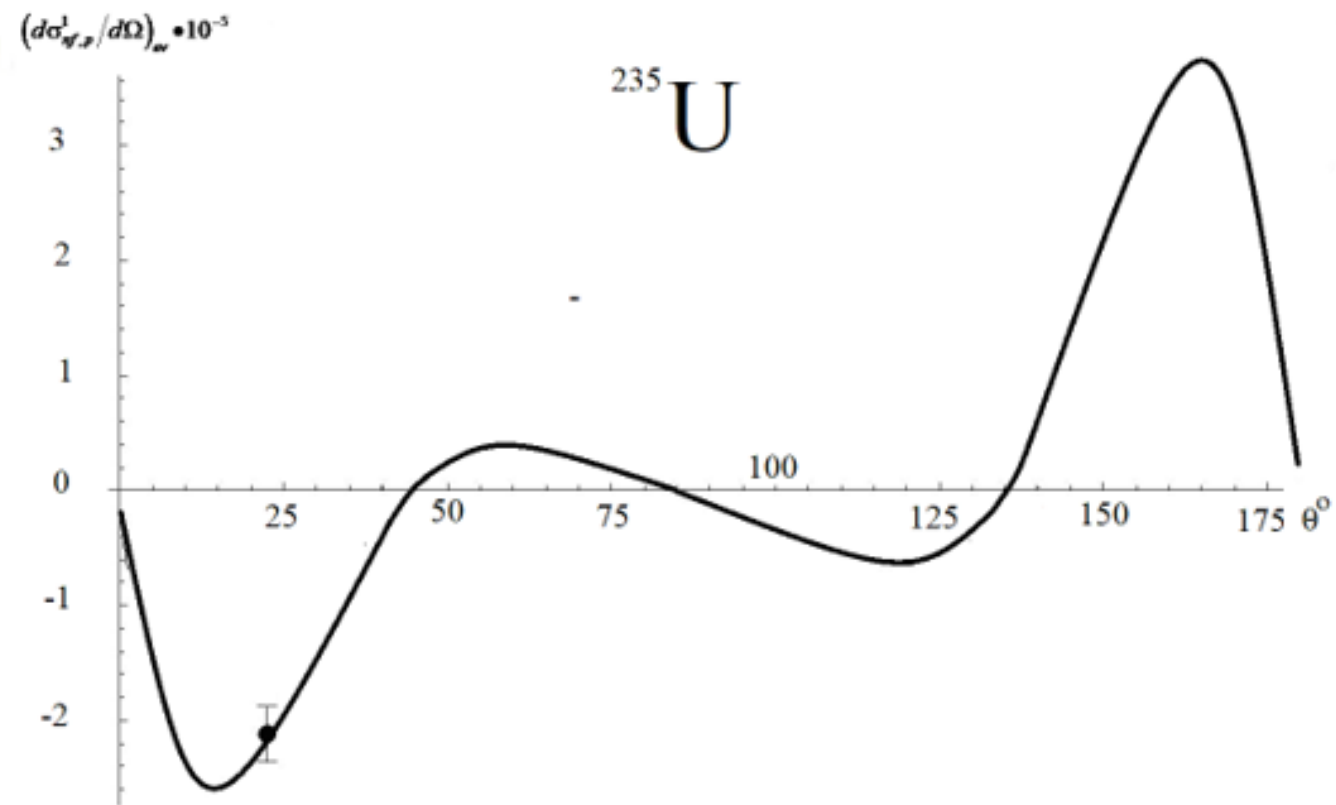


Fig. 11. Cross section  $(d\sigma_{nf,p}^1/d\Omega)_-$  for  $^{235}\text{U}$  neutrons

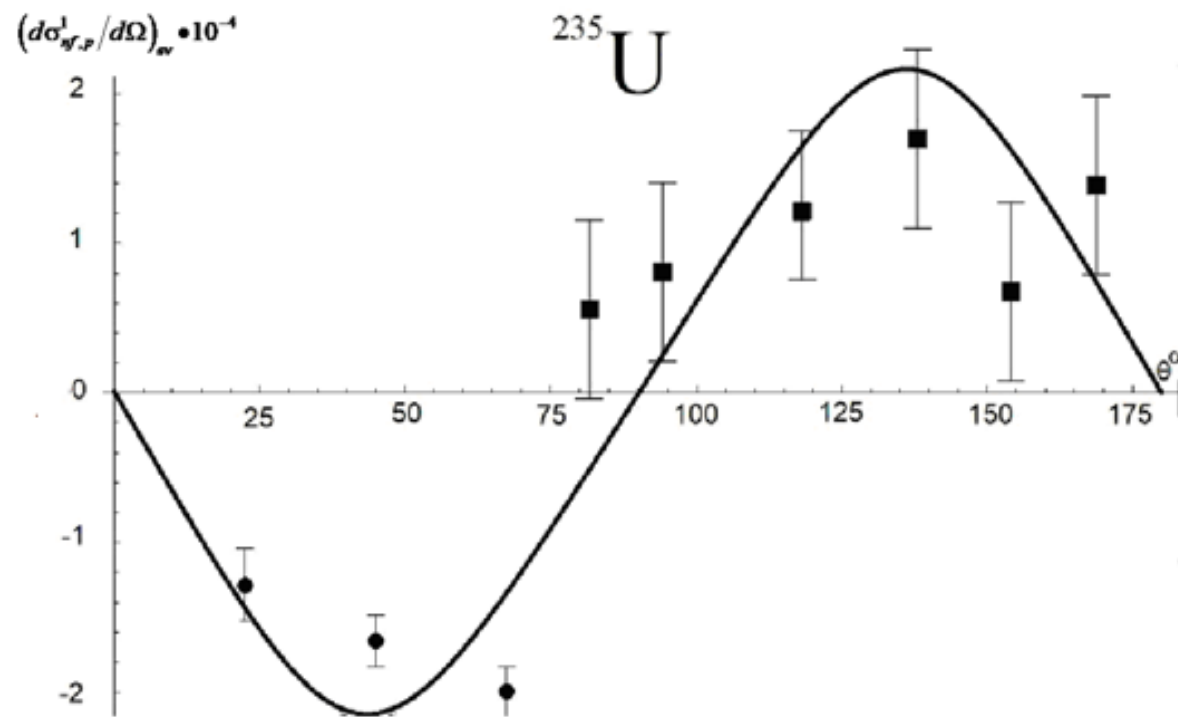


Fig. 12. Cross section  $\left(d\sigma_{nf,p}^1/d\Omega\right)_{ev}$  for evaporative  $^{235}\text{U}$   $\gamma$  - quanta, where the circles are experimental data from [Danilyan G.V., Krakhotin V.A., Novitsky V.V. et al. // Phys. Atom. Nucl. 2014. V. 77. № 6. P. 677.], and the squares are similar data from [Gagarski A., Goennenwein F., Guseva I., et al., // Phys. Rev C. 2016. V.93. P.054619.]

## Conclusion

1. The existence of a single mechanism for the appearance of ternary  $(\sigma_n, [\mathbf{k}_{LF}, \mathbf{k}_3])$  and  $(\sigma_n, [\mathbf{k}_{LF}, \mathbf{k}_3])(\mathbf{k}_{LF}, \mathbf{k}_3)$  quintuple P - even, T - odd scalar correlations in the differential cross sections of reactions of ternary nuclear fission by cold polarized neutrons with the release of precession  $\alpha$  - particles due to the influence of the Coriolis interaction of the total spin of a rotating fissile system with the orbital moments of fission fragments and  $\alpha$  - particles was confirmed.
2. The connection of P - even T - odd asymmetries in the angular distributions of prompt neutrons and  $\gamma$  - quanta emitted from fragments of binary fission of nuclei by cold polarized neutrons with quintuple  $(\sigma_n, [\mathbf{k}_{LF}, \mathbf{k}_3])(\mathbf{k}_{LF}, \mathbf{k}_3)$  scalar correlations caused by the influence of the Coriolis interaction of the total spin of a rotating fissile system with the orbital angular momenta of fission fragments was demonstrated.

Thank you for attention!