

# ANALYSIS OF NONSTATISTICAL EFFECTS IN NEUTRON RESONANCES

S.I.Sukhoruchkin

Petersburg Nuclear Physics Institute, Gatchina, Russia

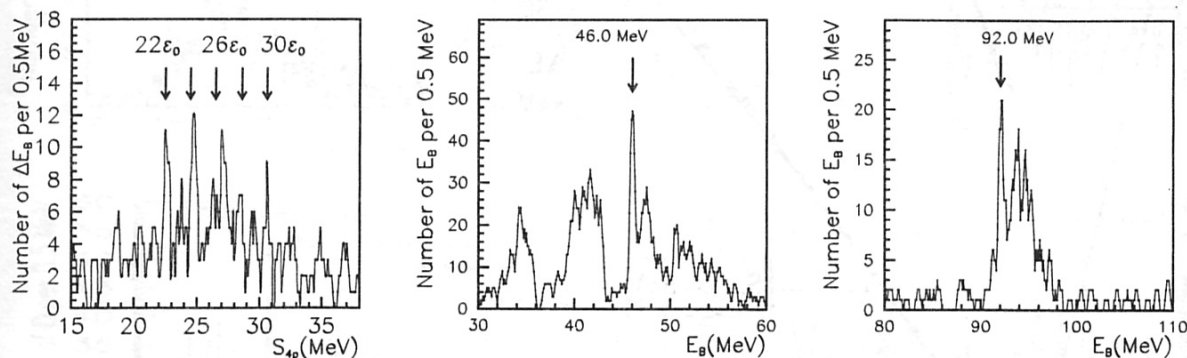
## 1 Introduction

In this report we discuss nonstatistical effects in neutron resonances as a reflection of a "tuning effect" in nuclear data. The study of spacing distributions in neutron resonances in near-magic nuclei permitted a conclusion that stable intervals between resonances are close or rational to the stable intervals in low-lying levels [1]. On the other hand systematic effects in excitations ( $E^*$ ) and spacing ( $D$ ) in near-magic nuclei are described by parameters close to that observed in differences of nuclear binding energies  $\Delta E_B$  [2,3]. This concerns such common parameters as  $\varepsilon_o=1022$  keV and values rationally connected with  $\varepsilon_o$  (where  $\varepsilon_o/2$  is close to the electron rest mass  $m_e$ ). First we discuss effect in  $\Delta E_B$ .

In the next section we consider the systematic character of excitations in near-magic nuclei which permitted to introduce the parameter  $D_o=1293$  keV close to the mass difference of nucleons as a part of series of stable intervals rationally connected with  $D_o$  (period  $D_o/8=161$  keV) seen in general  $E^*$ -distributions and in data for some near-magic nuclei.

In conclusion we consider some features of tuning effects in nuclear data and particle masses in line with suggestions and findings made by S.Devons [4] and Y.Nambu [5,6].

The character of data on nuclear binding energies  $E_B$ , namely the grouping of  $\Delta E_B$  in nuclei differing by nuclear clusters: four protons, four  $\alpha$ -clusters and  ${}^6\text{He}$ -cluster (see 3 parts of Fig.1) are the major arguments for the presence of general "tuning effect" in nuclear data. By the substitution of the experimental values  $E_B$  [8] with the calculated values (according to different models like FRDM etc.) it was shown that models do not describe the observed correlation (exact rational ratios) in  $\Delta E_B$  of the near-magic nuclei.



**Fig. 1.** *Left:* Distributions of four-proton separation energies  $S_{4p}$  in N-even nuclei with  $N=50-82$ ; *Center and right:* Distributions of  $\Delta E_B$  in N-even nuclei differing by one and two  ${}^6\text{He}$  configurations; parameters  $\varepsilon_o$  and  $\Delta=(9/2)\varepsilon_o$  are discussed in the text.

A standard procedure for the determination of the residual interaction between valence nucleons consists in calculation of differences of separation energies of valence proton or neutron in nuclei with different number of nucleons of the other type ( $\Delta S_N=\varepsilon_{NN}$ ). In Fig.2-3 a linear dependence of 51-th valence proton separation energy (upon N) is shown.

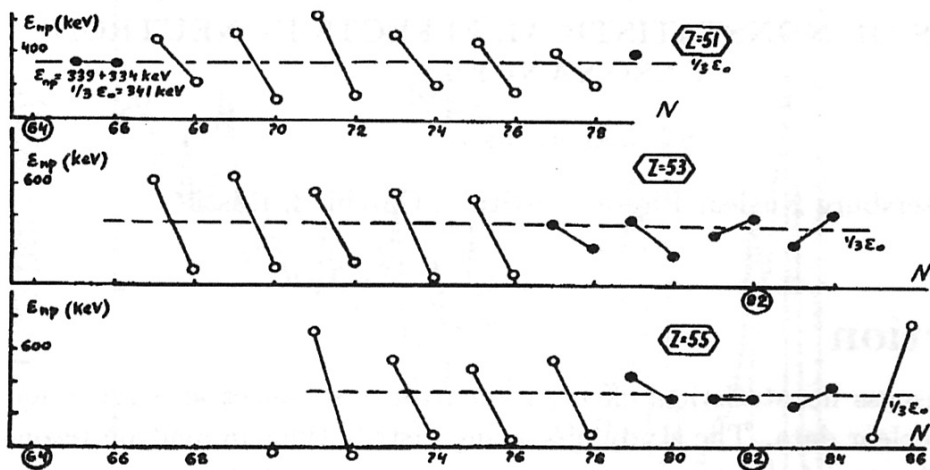


Fig.2. Parameters of the residual interaction  $\epsilon_{np}$  from differences of  $S_p$  in  $Z$ -odd nuclei differing with  $\Delta N=1$ . Mean value  $341 \text{ keV} = \epsilon_o/3$  is given by the horizontal line [7].

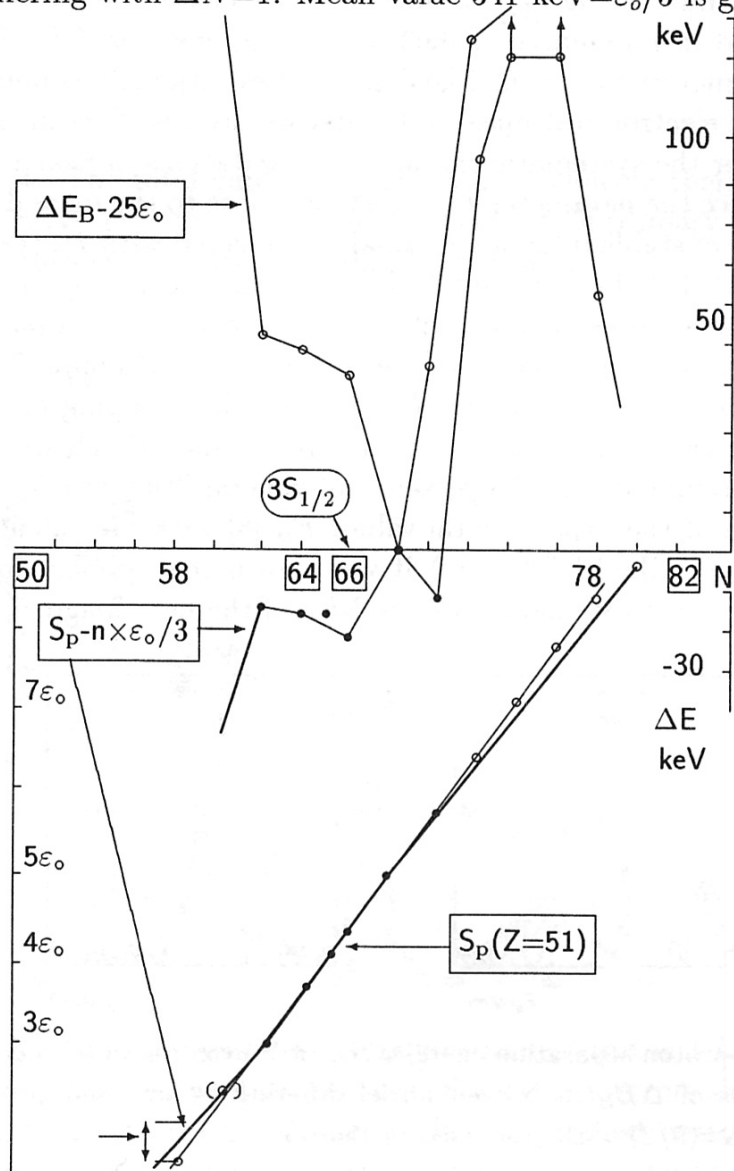
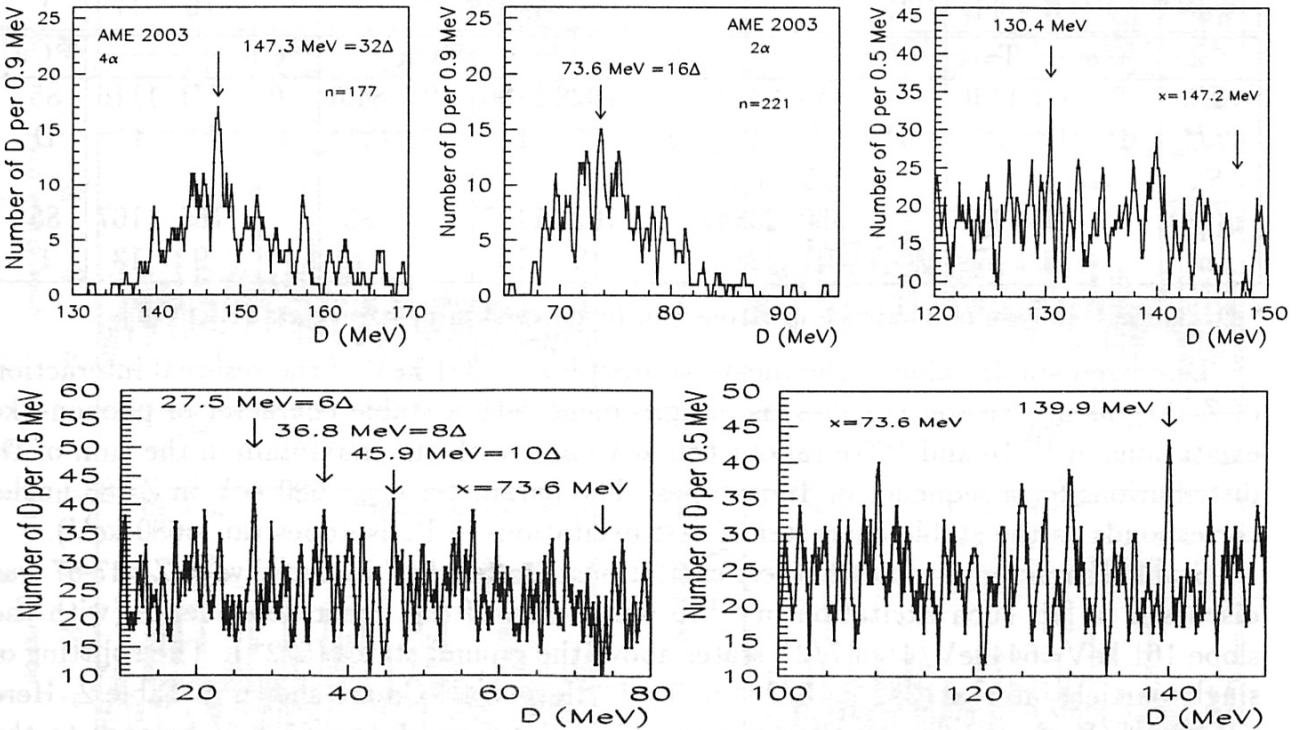


Fig.3. Bottom: Separation energies  $S_p$  of the valence 51-th proton and differences between  $S_p$  and the integer number of the period  $\epsilon_o/3=340 \text{ keV}$  (dark circles) as a function of  $N$ . Top: Difference between  $\Delta E_B = \Sigma(S_p(Z=50) + S_{2n}(Z=50))$  and  $25\epsilon_o$  (see Table 1).

Parameters  $\varepsilon_{pn}$  for nuclei with  $Z=51,53,55$  presented in Fig.2 show N-even-odd effect which becomes small in the regions of filling up of the well-known shells  $N=64, 82$  (dark circles). The same stable parameter  $340 \text{ keV} = \varepsilon_o/3$  was found in case of 83-th proton and 83-th neutron. Similar stabilizing effect (with  $\varepsilon_{pn} \approx 680 \text{ keV} = 2\varepsilon_o/3$ ) exists in nuclei with valence proton  $Z=29$ . Values  $S_p$  themselves are close to integers ( $n$ ) of  $\varepsilon_o/3$  (Table 1).

**Table 1.** Comparison of valence proton  $Z=29$  and  $Z=51$  separation energies with integers ( $n$ ) of the parameter  $\varepsilon_o/3=341 \text{ keV}$  (in keV) [7]. Boxed are small differences  $S_p - n \cdot 341 \text{ keV}$  and  $N$  corresponding to the closed subshells (Fig.2-3. Values  $S_p$  from FRDM are given below.

$A Z$	$^{57}\text{Cu}$	$^{59}\text{Cu}$	$^{61}\text{Cu}$	$^{63}\text{Cu}$	$^{65}\text{Cu}$	$^{67}\text{Cu}$	$^{69}\text{Cu}$	$^{62}\text{Zn}$
$S_p, \text{keV}$	695	3418	4801	6122	7452	8561	9543	6477
$n \times \varepsilon_o/3$	682	3407	4770	6132	7495	8517	9539	6473
$n$	2	10	14	18	22	25	28	19
diff.	13(18)	11(1)	31(1)	10(1)	43	44(18)	4(18)	4(10)
$N$	58	60	62	64	65	66	68	70
$A Z$	$^{109}\text{Sb}$	$^{111}\text{Sb}$	$^{113}\text{Sb}$	$^{115}\text{Sb}$	$^{116}\text{Sb}$	$^{117}\text{Sb}$	$^{119}\text{Sb}$	$^{121}\text{Sb}$
$S_p, \text{keV}$	1541	(2928)	3044	3734	4074	4406	5109	5779
$n \times \varepsilon_o/3$	1533		3066	3748	4088	4428	5110	5792
$n$	(9/2)		9	11	12	13	15	17
diff.	8(47)		22(22)	14(20)	14(7)	22(10)	1(9)	13(3)
$\varepsilon_{p2n}, \varepsilon_{pn}$				690	340	672	703	670
$S_p, \text{FRDM}$	759		2308	3238	4039	4278	5198	5978



**Fig.4** Top:  $\Delta E_B$ -distribution in nuclei  $Z \leq 26$ ) differing by four and two  $\alpha$  clusters. Top right and bottom: Distribution of  $\Delta E_B$  adjacent to  $x=147.2 \text{ MeV}$  and to  $x=73.6 \text{ MeV}$ .

An example of a study of correlations in  $\Delta_B$  is shown in Fig.4. The correlation program "AIM – Adjacent Interval Method" detects the appearance of triplets in spectra of nuclear binding energies ( $E_B$ ) or excitations. AIM plots the distribution of spacing ( $D^{AIM}$ ) from those levels (states) which form stable intervals  $D=x$  under investigation. Grouping of  $\Delta_B$  in light nuclei ( $Z \leq 26$ ) differing by four and two  $\alpha$ -cluster configurations ( $\Delta Z = \Delta N = 8, 4$ ) which take place at  $\Delta_B = 147.2 \text{ MeV} = 32\Delta$  and  $73.6 \text{ MeV} = 16\Delta$  were checked by observation of other  $\Delta_B$ -grouping in AIM intervals (for  $x = 147.2 \text{ MeV}$  and  $x = 73.6 \text{ MeV}$ , Fig.4 bottom). Parameter  $\Delta = (9/2)\epsilon_o = 4.6 \text{ MeV}$  was found [2,3] from the grouping of  $\Delta_B = n \cdot \Delta$  ( $n = 9, 10, 11$ ) in nuclei differing by  ${}^6\text{He}$ -cluster ( $N \leq 126, 82, 50$ ).

## 2 Tuning effect in nuclear excitations

Stable character of energy intervals due to valence nucleon interactions was studied also in data for nuclear excitations: interval 340 keV and its doubled value 682 keV were seen as maxima in D-distributions for  ${}^{43}\text{Ca}$ ,  ${}^{43}\text{Sc}$ ,  ${}^{47}\text{V}$ ,  ${}^{57}\text{Ni}$ ,  ${}^{62}\text{Ni}$  [2] and  ${}^{55}\text{Fe}$ . Data on  $E^*$  and spectroscopic factors ( $S_N$ ) collected recently in CRF (Combined Reaction File [8]) permitted to show that a periodicity in  $E^*$  in nuclei around  ${}^{56}\text{Ni}$  with the period 85 keV  $= \epsilon_o/12$  (Table 2,  $D = 85 \text{ keV}$  seen in  ${}^{55}\text{Co}$ ,  ${}^{65}\text{Cu}$  [2]) is connected with the large  $S_N$ .

**Table 2.** Comparison of energies and  $S_N$  with integers of  $\epsilon_o/12 = 85 \text{ keV}$  ( $E^*$  in keV).

$AZ$	${}^{55}\text{Fe}$	${}^{55}\text{Co}$	$T = \frac{3}{2}$	${}^{57}\text{Ni}$	${}^{59}\text{Ni}$	${}^{58}\text{Cu}$	$T = 1$	${}^{55}\text{Co}$
$E^*$	0 411 931	4721 4748 5743		0 769 1113	0 * 339	203 1051 1652		84
$2J^\pi$	3 <sup>-</sup> 1 <sup>-</sup> 5 <sup>-</sup>	3 <sup>-</sup> 3 <sup>-</sup> 5 <sup>-</sup>		3 <sup>-</sup> 5 <sup>-</sup> 1 <sup>-</sup>	3 <sup>-</sup> 5 <sup>-</sup>	0 <sup>+</sup> (1 <sup>+</sup> ) 2 <sup>+</sup>		D
$S_N$	0.7 0.6 0.7	0.45 0.37 1.2		0.9 0.5 0.12	3.3 4.1			
diff		1022 965				848 1449		
$n(\frac{\epsilon_o}{12})$	425 935	1022		765 1107	340	850 1445		85
n	5 11	12		9 13	2	10 17		1
$AZ$	${}^{54}\text{Co}$	$T = 1$	${}^{52}\text{Fe}$	${}^{57}\text{Cu}$	${}^{68}\text{Cu}$	${}^{65}\text{Cu}$		${}^{65}\text{Cu}$
$E^*$	0 937 1146		0 849 2384	0 1028 1106	0 84.6	0 771 1116		85
$2J^\pi$	0 <sup>+</sup> 1 <sup>+</sup> 2 <sup>+</sup>		0 <sup>+</sup> 2 <sup>+</sup> 4 <sup>+</sup>	3 <sup>-</sup> 5 <sup>-</sup> 1 <sup>-</sup>	1 <sup>+</sup> (2 <sup>+</sup> )	3 <sup>-</sup> 5 <sup>-</sup> 1 <sup>-</sup>		D
$S_N$			2.2 1.5 1.1					
$n(\frac{\epsilon_o}{12})$	935 1147		850 2384	1022 1107	85	765 1107		85
n	11 17		10 28	12 13	1	9 13		1

\*  $D = 340 \text{ keV}$  in case of 3 valence neutrons can be checked in neutron data (EXFOR).

Discussed stable value of the mean parameter  $\epsilon_{pn} = 341 \text{ keV}$  of the residual interaction of  $Z = 51$  valence proton (Fig.2-3) is in agreement with a stable character of phonon-like excitations in  ${}^{118}\text{Te}$  and  ${}^{126}\text{Te}$  (about 680 keV) and with the maximum in the sum of D-distributions for a sequence of Te-isotopes. The parameter  $\epsilon_{p2n} = 680 \text{ keV}$  in  $Z = 83$  nuclei corresponds to the stable character of first excitations in Po-isotopes (at  $\approx 680 \text{ keV}$ ).

Stable character of somewhat less excitations  $E^* = 644 \text{ keV}$  in nuclei with  $Z = 47-57$  was discussed in [9]: such excitation in  ${}^{111}\text{Sb}$  was a part of the linear dependence (with the slope  $161 \text{ keV} = 644 \text{ keV}/4$ ) of  $7/2^+$  states above the ground states ( $5/2^+$ ). The splitting of single-particle interval ( $3/2^- - 5/2^-$ ) in  $T = 3/2$  levels of  ${}^{55}\text{Co}$  are shown in Table 2. Here  $D = 1022 \text{ keV} = \epsilon_o$  belongs to the sequence  $170 \text{ keV} \times n$  while  $D = 965 \text{ keV}$  belongs to the sequence  $161 \text{ keV} \times n$ ,  $n = 6$ . Intervals  $D = \epsilon_o$ ,  $D = \epsilon_o/2$  and  $324 \text{ keV} = 965 \text{ keV}/3$  are forming stable triplets in  ${}^{55}\text{Co}$  states observed by AIM.

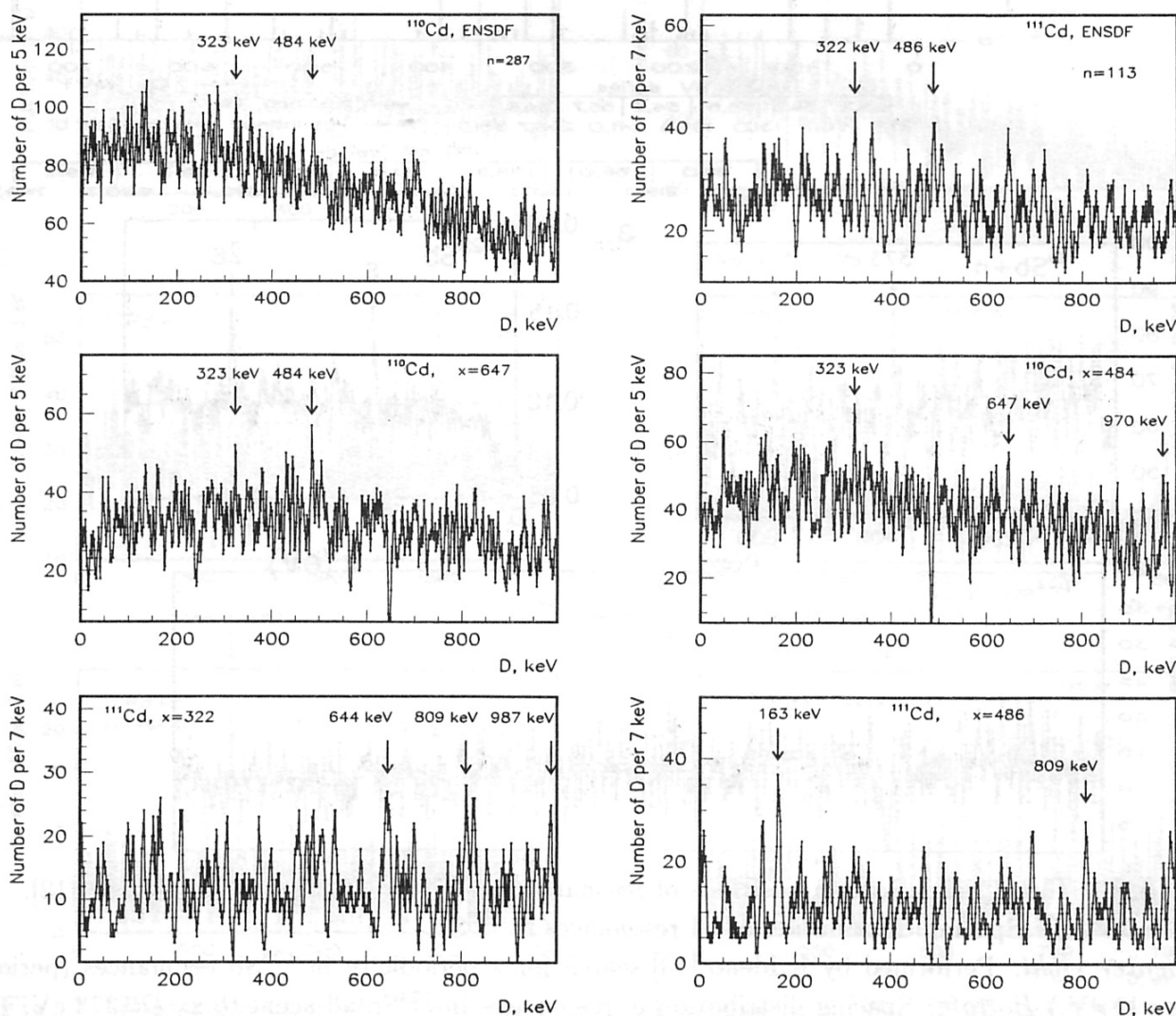


Stable intervals  $D=D_o=1293$  keV  $\approx 161 \times 8$  were found in  $^{32,33}\text{S}$ . In many nuclei  $E^*$  at  $(1/2)D_o=647$  keV,  $D_o=1293$  keV,  $(3/2)D_o=1942$  keV and  $2D_o=2586$  keV were noticed [10]. Data from CRF on  $E^*$  and  $S_N$  for nuclei with  $N=21$  (Table 3) were used to check a linear trend with the slope 647 keV derived from the ratio  $1942.8/646.2=3.006$  in  $E^*$  of  $7/2^-$  states with large  $S_N$ . Excitations  $E^*=159-484$  keV in  $^{33}\text{Mg}$  triplet correspond to  $(1/4)-(3/4)$  of  $D_o/2=647$  keV. Data for  $^{35}\text{Si}$ ,  $^{32}\text{Si}$  and  $^{38}\text{S}$  are given for comparison.

**Table 3.** Comparison of energies with integers of  $647$  keV  $=D_o/2$  ( $E^*$  in keV, large  $S_N$ )

$A/Z$	$^{41}\text{Ca}$		$^{39}\text{Ar}$		$^{37}\text{S}$		$^{35}\text{Si}$	$^{33}\text{Mg} (3^+)$		$^{32}\text{Si}$		$^{38}\text{S}$	
$E^*$	0	1943	0	1267	0	646	910	159	484	0	1942	0	1292
$2J^\pi$	$7^-$	$3^-$	$7^-$	$3^-$	$7^-$	$3^-$	$(3^-)$	$(7^-)$	$(3^-)$	$0^+$	$2^+$	$0^+$	$2^+$
$S_N$	0.85	0.67	0.64	0.57	5.54	1.75				1.6	5.3		
$n \frac{D_o}{8}$	0	1941	0	1293	0	646		161	483		1941		1293
n		12		8		4		1	3		12		8

Close to each other stable intervals  $D=322-323$  keV and  $484-486$  keV were found in spectra of  $^{110}\text{Cd}$  and  $^{111}\text{Cd}$  (Fig.5 top, numbers of levels 287 and 113). These  $D$  were checked by AIM-analysis by fixation of  $D=x=647-484$  keV and  $D=x=322-486$  keV (Fig.5). All maxima correspond to series of values  $n \times 161$  keV  $=n \times D_o/8$  ( $n=1,2,3,4,5,6$ ). The intervals are close to  $2^+$  excitations in  $^{106,108,110}\text{Cd}$  (632, 632, 658 keV) and  $E^*(\Delta J=1^+)$  in  $^{111}\text{Cd}$ .

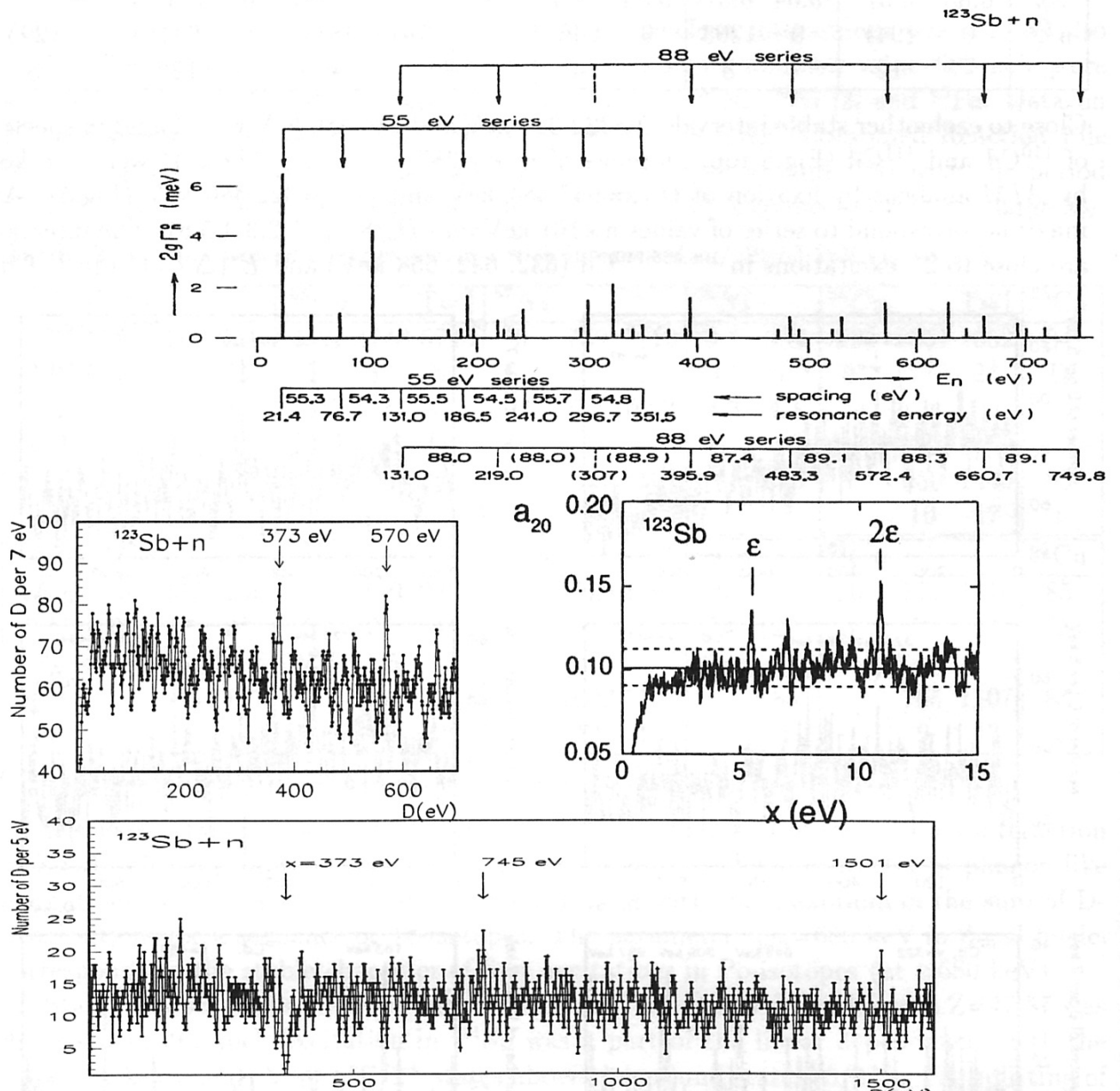


**Fig. 5.** Top: D-distribution in all levels of  $^{110}\text{Cd}$  and  $^{111}\text{Cd}$ . Center and bottom: Distribution of intervals adjacent to  $x=D=647$  and  $484$  keV in  $^{110}\text{Cd}$  and  $x=D=322$  and  $486$  keV in  $^{111}\text{Cd}$ .

### 3 Superfine structure in neutron resonance positions

In a study of nonstatistical effects in complex nuclear spectra seen as neutron resonances different method of correlation analysis should give consistent results. For example, four pictures in Fig.6 illustrate results obtained for near-magic compound  $^{123}\text{Sb}$  ( $Z=50+1$ ) where earlier [11] intervals rational to the period 5.5 eV were noticed.

1) M. Ohkubo [12] marked the sequence of resonances (with the period 88 eV) from 131 eV up to the second strongest resonance at 750 eV (see two-dimensional plot of the reduced widths vs. the energy in Fig.6 top). From the ratio  $131/88=1.49$  one can conclude that resonance positions are expressed in odd units of 44 eV, from  $n=3$  up to 17. Additional strong resonances correspond to  $n=9$  (396 eV) and  $n=13$  (572 eV).



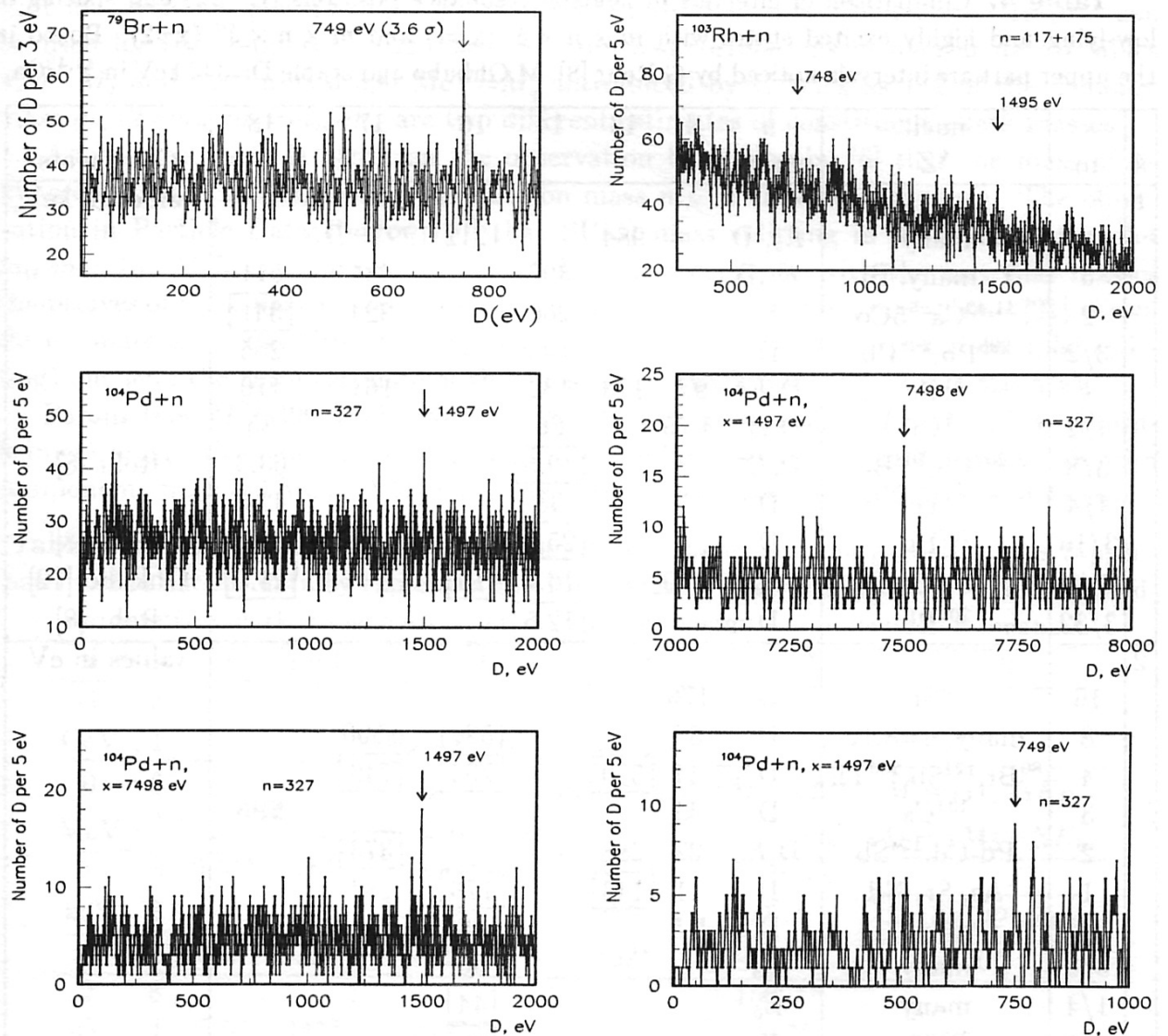
**Fig. 6.** Top: Correlations in positions of resonances in  $^{123}\text{Sb}$  discussed by M. Ohkubo [12]. Center left: Spacing distribution of all resonances in  $^{123}\text{Sb}$ . Center right: Performed by K. Ideno [13] search for a periodicity in  $^{123}\text{Sb}$  resonances (period  $2\epsilon=11$  eV.) Bottom: Spacing distribution of resonances in  $^{123}\text{Sb}$  adjacent to  $x=D=373$  eV.

2) K.Ideno developed several methods of the study of superfine structure in resonance positions [13-15]. His observation of the distinguished period  $11 \text{ eV} = 44 \text{ eV}/4$  in the same data shown in Fig 6 (center right) is complementary to the results by M.Ohkubo.

3) In spacing distribution of all resonances (mainly s-resonances) of  $^{123}\text{Sb}$  shown in Fig.6 (center left) one can see two clear maxima which correspond to  $n=13$  and  $n=17$  with the period found by M.Ohkubo in resonance positions.

4) It is shown by AIM-analysis [16] that intervals 373 eV, 745 eV and 1501 eV (with a ratio 1:2:4) are appearing as triplets in highly excited states of  $^{124}\text{Sb}$  (Fig.6, bottom). Stable intervals 750-1500 eV were found also in D-distributions for  $^{80}\text{Br}$ ,  $^{104}\text{Rh}$  and  $^{105}\text{Pd}$  (Fig.7). In the distribution of intervals adjacent to  $D=1497 \text{ eV}$  in resonances of  $^{105}\text{Pd}$  large interval  $D=7498 \text{ eV}$  with values close to  $5 \times 1497(2) \text{ eV} = 7485(10) \text{ eV}$  and intervals equal to its half were also observed.

Stable intervals and resonance positions in  $^{124}\text{Sb}$  ( $n=9,13,17$ ) and stable intervals in  $^{76}\text{As}$  ( $n=13/4$  period 44 eV) noticed by K.Ideno and M.Ohkubo are presented (and boxed) in Table 4. Stable intervals in  $^{233}\text{Th}$ ,  $^{88}\text{Sr}$ ,  $^{134}\text{Cs}$  and grouping of  $(E^* - S_n)$  in nuclei with  $Z=31-56$  and  $56-94$  were also included in this Table.



**Fig. 7.** Top and center left: D-distributions of all resonances in  $^{79}\text{Br}$ ,  $^{103}\text{Rh}$  and  $^{104}\text{Pd}$ . Center right and bottom: Spacing distributions of resonances in  $^{104}\text{Pd}$  adjacent to interval  $x=1497 \text{ eV}$  and  $x=7498 \text{ eV}$  (distribution only in downward direction).

The above discussed value  $D_o=1293(2)$  keV coincides with the nucleon mass difference 1293.3 keV. Together with the coincidence of the nuclear parameter  $\varepsilon_o$  with  $2m_e$  and the third coincidence, namely, of the electromagnetic mass difference of the pion with the nuclear parameter  $\Delta=9m_e=4.6$  MeV, they all were considered as signals about the presence of the tuning effect in nuclear data similar to that in the particle masses.

It was concluded in [17] that:

- 1) intervals of the fine-structures  $161 \text{ keV}=D_o/8$  and  $170 \text{ keV}=\varepsilon_o/6$  are in the same ratio  $17/18$  as  $m_\pi=140 \text{ MeV}$  and  $147 \text{ MeV}$  – the half of the nucleon  $\Delta$ -excitation ( $294 \text{ MeV}/2$ );
- 2) the dimensionless ratio between these two pairs of hadronic parameters, namely the ratio  $(D=341 \text{ keV}=\varepsilon_o/3)/294 \text{ MeV}=1.16 \cdot 10^{-3}$  or  $1/(27 \cdot 32)=1.157 \cdot 10^{-3}$  is close to the QED radiative correction  $\alpha/2\pi=1.159 \cdot 10^{-3}$ . It means that empirically observed parameters of the fine- and superfine structures ( $\delta'=9.5 \text{ keV}$  and  $\delta''=11 \text{ eV}$ ) form the ratio close to  $\alpha/2\pi$  between themselves and with the value  $16m_e=\delta=2\Delta-\varepsilon_o=8.176 \text{ MeV}$ .

Different stable intervals observed in neutron resonances and in low-lying levels are displayed in Tables 4 and 5 in accordance with this empirical findings:  $D=m \times n \times \delta'$  ( $x=1$ ) and  $m \times n \times \delta''$  ( $x=2$ ).

**Table 4.** Comparison of intervals in neutron resonance positions ( $E^*-S_n$ ) and spacing in low-lying and highly excited states with  $m \times n \times \delta'$  ( $x=1$ ) and  $m \times n \times \delta''$  ( $x=2$ ). Boxed in the upper part are intervals noticed by G.Rohr [8], M.Ohkubo and stable  $D=340 \text{ keV}$  in  $^{41,43}\text{Ca}$ .

x	m	nucl. $A Z$	n	1	13	14	16	17	18	Comments
1			param.							values in keV
	8	many	$E_o, D$		984		1212	1293= $D_o$		
	3	Y, many, Bi,	$E_\gamma, D$			397		484	511	
	2	$^{41,43}\text{Ca}, ^{55}\text{Co}$	D			266		324	<span style="border: 1px solid black;">341</span>	
	3/2	$^{205}\text{Pb}, ^{208}\text{Pb}$	D			198			255	
	1	$^{51}\text{Cr}$	$D, E^*$	9.5	123	132		161	170	
	1/2	$^{51}\text{Cr}$	$D, E^*$	4.75		66			85	
	3/8	$^{207}\text{Pb}, ^{208}\text{Bi}$	$D, E^*$			<span style="border: 1px solid black;">49.5</span>			63.3	Rohr [8]
	1/4	$^{57}\text{Fe}$	D			33			42.5	
	3/16	$^{207}\text{Pb}$	D			<span style="border: 1px solid black;">25.0</span>				Rohr [8]
	1/8	$^{140}\text{Ce}, ^{207}\text{Pb}$	$E_o$	1.19		16.4	<span style="border: 1px solid black;">19</span>		<span style="border: 1px solid black;">21.5</span>	Ohkubo [12]
	3/32	$^{207}\text{Pb}$	D			<span style="border: 1px solid black;">12.5</span>				Rohr [8]
2										values in eV
	16	$^{88}\text{Sr}$	D	176						
	8	many, n=8,12	D	88			(528)	1500		
	4	$^{80}\text{Br}, ^{124}\text{Sb}, ^{233}\text{Th}$	D	44	<span style="border: 1px solid black;">570</span>		<span style="border: 1px solid black;">704</span>	<span style="border: 1px solid black;">749</span>		
	3	$^{134}\text{Cs}$	D	33					<b>595</b>	
	2	Pd-Cd, $^{124}\text{Sb}$	$D, E_o$	22	288			<span style="border: 1px solid black;">373</span>		
	1	As, Sr, Nd	D	11	<span style="border: 1px solid black;">143</span>		<span style="border: 1px solid black;">176</span>	187		
	1/2	many	D	5.5			88			
	3/8	many	$E_o$				66			
	1/4	many	$E_o$				<span style="border: 1px solid black;">44</span>			
	1/8	$^{233}\text{Th}$	$E_o$				<span style="border: 1px solid black;">22</span>			



## 4 Tuning effect in particle masses

The presence of similar stable intervals in nuclei where different shells are filling up was interpreted as a manifestation of a tuning effects of the general origin connected with the nucleon structure as it was suggested by S.Devons. In existing constituent-quark models nucleon mass is treated as a sum of three fermion components of about 300-400 MeV. The following three constituent quark masses were considered.

The value  $M_q=441$  MeV close to  $3/2$  of the well-known value of nucleon  $\Delta$ -excitation (294 MeV) was introduced by R.Sternheimer and P.Kropotkin [18,19] as  $3/2(m_\Delta-m_N=m_\eta-m_\mu=m_N-m_K=m_\Xi/3=M_q)$ . It can be considered as one third of the "initial mass" of non-strange baryon  $M_N^{init}=M_\Delta^{init} \approx 1350$  MeV (that's the theoretical mass before inclusion of the residual quark interaction) in the Quark Model with Goldstone Boson Exchange [20]  $M_N^{init}$  which is close to the octet  $\Xi^-$ -hyperon mass (1324 MeV= $3 \times 441$  MeV= $3 \times M_q$ ) due to the compensation of the mass reduction from quark interaction ( $\approx 294$  MeV) and the mass increasing from the strangeness ( $S=2$ ,  $m_s-m_d \approx 150$  MeV).

It was noticed in 70-ties [17] that the parameter  $\varepsilon_o/2=511$  keV in nuclear data (or  $m_e$ ) forms the ratio  $1/(32 \cdot 27) = \alpha/2\pi$  with the Sternheimer's mass parameter. It means that four different powers ( $n=-1,0,1,2$ ) of QED radiative correction  $\alpha/2\pi=1.16 \cdot 10^{-3}$  can be used for the comparison the observed empirical correlations in nuclear data (Tables 4,5).  $M_q$  and the interval  $390$  MeV= $M_q''$  introduced by G.Wick as  $1/2$  of the  $\omega$ -meson mass  $m_\omega/2=m_N-m_\eta=m_K-m_\mu$  are two different estimates of constituent quark masses.

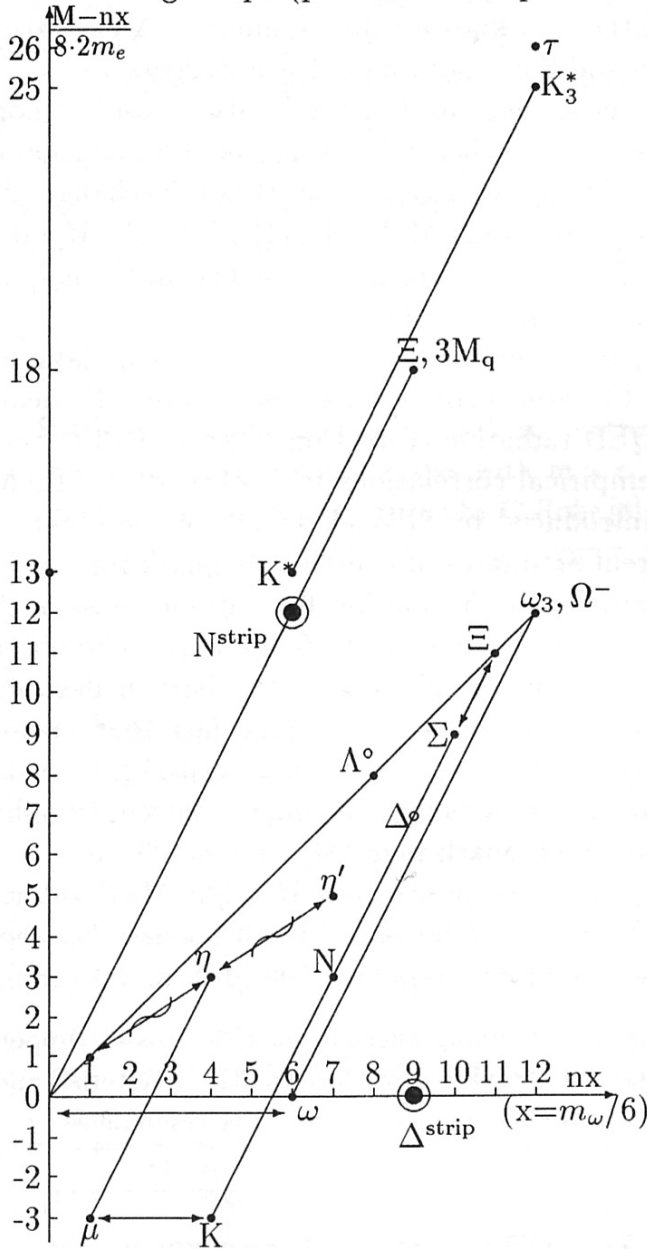
Another estimate is based on the observation by Y.Nambu [6] that the mass of  $\Lambda$ -hyperon is close to  $8m_\pi$  (while the nucleon mass  $m_N$  is close to  $6m_\pi+m_\mu$ ). The observation in Particle Data Review [20] that SU(3) mass splitting in the baryon decuplet  $m_\Omega-m_\Xi=137$  MeV is close to  $m_\pi=139$  MeV is in accordance with the fact that masses themselves of these baryons are close to integers of  $m_\pi$  ( $m_\Omega=12m_\pi$ ,  $m_\Xi=11m_\pi$ ) [21]. From the estimate of the constituent strange baryon quark mass  $m_\Omega/3=4m_\pi$  (and decuplet splitting) one gets the third estimate of the nonstrange quark mass  $M_q'=3m_\pi=420$  MeV.

Parameters  $M_q''=390$  MeV (Wick),  $M_q'=3m_\pi$  (Nambu) and  $M_q=440$  MeV (Sternheimer) are in the relation 16:17:18 and the similar relation 17:18:13:1 exists between components  $m_\pi=139$  MeV,  $\Delta M_\Delta=147$  MeV, the muon mass  $m_\mu=106$  MeV and  $\delta=16m_e$ .

**Table 5 from [1].** Representation of parameters of tuning effect in particle masses (upper part) and in nuclear data by expression  $(n \times 16m_e(\alpha/2\pi)^x) \times m$  with  $\alpha = 137^{-1}$ . Asterisk and two asterisks mark stable nuclear intervals at low energy and in neutron resonances.

$x$	$m$	$n=\frac{1}{8}$	$n=1$	$n=13$	$n=16$	$n=17$	$n=18$
-1	3				$2m_t=348$		
GeV	1			$M_Z=91.188$	$M_H=115$		
0	3				$M_q''=m_\omega/2$	$M_q'=420$	$M_q=441, \Delta E_B$
MeV	1	$\varepsilon_o$	$16m_e$	$m_\mu=105.658$		$m_\pi - m_e$	$147=\Delta M_\Delta, \Delta E_B$
1	8	$9.5^{**}$	$76^*$	$984^*$	$1212^*$	$1293=D_o$	
keV	3			$368^*$	$455^*$	$481^*$	$511=\varepsilon_o/2=m_e$
	1	$1.2^*$	$9.48^*$	$123^*$	$152^*$	$161^*$	$170^*$
2	8					$1500^{**}$	
eV	4	$5.5^*$	$44^{**}$	$572^{**}$		$750^{**}$	
	1		$11^{**}$	$143^{**}$	$176^{**}$	$187^{**}$	

Three above discussed estimates of constituent quark masses are shown together in two-dimensional presentation in Fig.8. Masses ( $M_i$ ) are expressed as "integers" of the period  $16 \cdot 16m_e = 130$  MeV (close to  $1/3$  of Wick's interval  $390$  MeV  $= m_\omega/2$ ) and "residuals"  $M_i - k \times (16 \cdot 16m_e = \delta)$  plotted along the vertical axis in  $16m_e = \delta$  units. Masses integer with pion mass are shown on the line with the minimal slope. Masses and mass differences which are integer with  $147$  MeV (half of  $\Delta$ -excitation,  $m_{\Xi^-}$ ,  $M_q$  etc.) correspond to lines with the large slope (parallels correspond to equal periods in mass differences).



**Fig.8.** Position of different mass intervals and  $\tau$ -lepton mass close to integer number of  $M_q = m_{\Xi^-}/3$  on the two-dimensional mass-presentation with the horizontal axis in units  $16 \cdot 16m_e$  close to  $m_\omega/6$  and  $M_i - k \times (16 \cdot 16m_e = \delta)$  along the vertical axis in  $16m_e$  units. Two lines with the discrete slopes correspond to the pion mass ( $140$  MeV  $= m_\omega/6 + \delta$ ) and to the nucleon  $\Delta$ -excitation  $m_\omega/6 + 2\delta$ . Crossed arrows correspond to intervals  $m'_{\eta} - m_{\eta} = m_{\eta} - m_{\pi}^{\pm}$  ( $n=50$ ). Parameters  $\Delta^{strip}$  and  $N^{strip} = 880$  MeV are marked by black circles. The lines corresponding to  $2^+$  - excitation of both vector mesons ( $J^{\pi} = 1^- - J^{\pi} = 3^-$ , from  $K^*$  to  $K_3^*$  and from  $\omega$  to  $\omega_3$ ) are parallel with  $\Delta$ -excitation and Sternheimer's interval  $M_q = m_{\Xi^-}/3$  between  $\eta$ -meson and muon, from the kaon to the nucleon and from the nucleon to the  $\Sigma$ -hyperon.

The discussed discreteness of pion and muon masses (17:13:1) with the period  $\delta$  takes place also in stable intervals in mesons masses. For example, intervals  $m_\varphi - m_\omega = m_\omega - m_\eta = 236$  MeV and  $m'_\eta - m_\eta = m_\eta - m_\pi^\pm = 409$  MeV are close to  $n=29$  and  $n=50$ . The second interval ( $n=50$ ) shown as crossed arrow coincides with  $2m_{\pi^0} + m_\pi$ .

Four additional relations with Sternheimer's parameter  $M_q = 441$  MeV were found:

1) Consideration of the possible origin of large mass intervals was connected with the fact that  $M_q = 441$  MeV is equal to a half of nucleon "stripped" mass  $M_N^{\text{stripped}} \approx 880$  MeV from lattice calculations. One can add to this value ( $2M_q = 6\Delta M_\Delta$ ) the nucleon  $\Delta$ -excitation ( $2\Delta M_\Delta$ ) for obtaining the corresponding "stripped" mass for  $\Delta$ -baryon. The resulting estimate  $8\Delta M_\Delta = 3M_q''$  of "stripped" mass of  $\Delta$ -baryon and the above discussed its "initial" mass are both represented as three-fold values of parameters of the parameters  $M_q''$  and  $M_q$  found independently in other data.

2) Coincidence of  $2M_q$  with  $2^+$ -excitations of both vector mesons ( $J^\pi = 1^- - J^\pi = 3^-$ ) can be seen in Fig.8. Both lines: from  $K^*$  to  $K_3^*$  and from  $\omega$  to  $\omega_3$ ) are going parallel to the nucleon  $\Delta$ -excitation and Sternheimer's interval.

3) Closeness of  $\tau$ -lepton mass to  $4M_q$  is evident from Fig.8.

4) Both estimates  $M_q$  and  $M_q''$  of the constituent quarks form ratios with vector boson masses close to the lepton ratio ( $L = m_m u / m_e$ ). We know that boson masses are parameters of the Standard Model (together with masses of fundamental fermions  $m_e, m_\mu$  etc.). According to Y.Nambu the present state of the Standard Model "is theoretically unsatisfactory because a) the unification of forces is only partially realized; and b) there are too many input parameters, especially concerning the masses, which are not explained. ... When we discover phenomena which we do not understand, the first thing to do is ... to try to find some empirical regularities among them. The mass problem: a) The fermion masses ...; b) The Higgs sector; c) The hierarchy problem ... with the Standard Model, we have reached the third stage of a three-stage cycle, and we are now at the door step of a new cycle. The mass problem is already an early signal for it" [5].

Small relative downward shift  $1.126 \cdot 10^{-3}$  in the muon mass (from the nearby value  $13 \times 16 m_e - m_e$ ) is close to the QED radiative correction for electron magnetic moment  $\alpha/2\pi = 1.16 \cdot 10^{-3}$ . After a small "correction" of the electron mass  $m_e^* = m_e(1 - \alpha/2\pi)$  the ratios between  $m_e^*$ , the mass splitting of pion  $\delta_\pi$  and the muon mass become close to the integers, namely  $m_e^* : \delta_\pi : m_\mu = 1:9.000:(207.02 = L = 9 \times 23 = 13 \times 16 - 1)$  [1]. The ratios  $M_Z/M_q$  and  $M_W/M_q''$  are close to  $L$  and ratios  $M_q/M_q''$  and  $M_Z/M_W$  are close to  $9/8 = 1.125$  ( $M_Z/M_W = 91.188/80.423 = 1.134$ ) [1]. The ratio between the well-known SM-parameters  $m_\mu/M_Z = 105.658/91188 \text{ MeV} = 1.159 \cdot 10^{-3}$  is really very close to  $\alpha/2\pi \dots = 1.159 \cdot 10^{-3}$ . These values are shown in the left part of Table 5 while  $m_e$  and  $M_q = 3\Delta M_\Delta$  are shown at right. The preliminary value of the Higgs boson mass from the LEP measurements and the top-quark mass are given in the upper part of Table 5 [1].

This report contains findings in nuclear data concerning the common tuning effect (common energy/mass parameters) and dimensionless relations between them. In addition to the discussed empirical relation with the well-known QED correction it was noticed [1] that similar QED correction for small distances ( $\alpha_Z = 1/129$  [22] instead of  $1/137$ ) also could be considered if the existing uncertainty in the Higgs boson mass will be removed.

Independent argument for a presence of the discussed here tuning effects in particle masses was obtained by R.Frosch [23]. He performed the correlation analysis of 47 values of particle masses and has found that the first candidate for the common period in these

masses is the value  $3m_e$ . It was shown in [24,25] that nucleon masses ( $m_n, m_p$ ) are shifted downwards relative to the value  $n=6 \times 17 + 13$  (in units  $\delta=16m_e$ ) corresponding to the Nambu's relation. Such shifts are  $m_e+162(1)$  keV and  $m_e+1455(1)$  keV while the mass splitting of nucleon  $\delta_N=1293$  keV relate to them as  $1:8:9 = 162 \text{ keV}:1293 \text{ keV}:1455 \text{ keV}$ . We see that a direct study of stable nuclear intervals with values integer to  $161 \text{ keV}=D_o$  (and related to the pion mass, Table 5) could be connected with the results by R.Frosch.

## 5 Conclusions

Nuclear forces are the result of a process of the spilling out of strong interaction between quarks forming nucleons. The possible involvement of three well-known parameter of the particle physics: the electromagnetic mass differences of nucleon ( $D_o$ ), pion (about  $9m_e$ ) and lepton ( $m_e$ ) in nuclear data can be considered in line with the suggestion by S.Devons [4] about fine nuclear effects which reflect nucleon structure and which would be difficult to observe in high energy physics.

## REFERENCES

1. S.I.Sukhoruchkin, Proc. 8-th Int. Conf. on Low Energy Antiproton Physics (LEAP'05), Bonn, 2005, AIP 796, p. 221, 2005.
2. Z.N.Soroko *et al.*, *Nucl. Phys. A* **680**, 254c (2001); *ibid*: 98c.
3. S.I.Sukhoruchkin, D.S.Sukhoruchkin, *Nucl. Phys. A* **722**, 553c (2003).
4. S.Devons, *Proc. Rutherford Jubilee Conf.*, Ed. J.Birks, Heywood, 611 (1961).
5. Y.Nambu, *Nucl. Phys. A* **629**, 3c (1998).
6. Y.Nambu, *Progr. Theor. Phys.* **7**, 595 (1952).
7. S.I.Sukhoruchkin, Proc. 9-th Int. Symp. Capt. Gamma-Ray, Budap., 1996, v.1, 358.
8. Z.N.Soroko *et al.*, these Proceedings.
9. Z.N.Soroko *et al.*, Proc. ISINN-10, 2002, JINR E3-2003-10, p.289; 308; 299.
10. Z.N.Soroko *et al.*, Proc.ISINN-7, 1999, JINR E3-99-212, p.313.
11. Ideno, K., Ohkubo, M., *J. Phys. Soc. Japan* **30**, 620 (1971).
12. M.Ohkubo *et al.*, Rep. JAERI-M-93-012, 1993.
13. Ideno, K., *J. Phys. Soc. Jpn.* **37** (1974), p.581.
14. Ideno, K., Proc. Int. Conf. Neutr. Research, Crete, SPIE Vol.2867, 1997, p.398.
15. Ideno, K., Proc. Int. Conf. Nucl. Struct., Tokyo, 1977, Contib. papers, 478,479.
16. Z.N.Soroko *et al.*, Proc ISINN-9, 2001, Dubna, E3-2001-192, p.p.334;351;342.
17. S.I.Sukhoruchkin, *Stat. Prop. Nuclei*, Ed. J.B.Garg, Pl. Press, p.215 (1972).
18. R.Sternheimer, *Phys. Rev.* **136**, 1364 (1964); **170**, 1267 (1968).
19. P.N.Kropotkin, *Field and Matter*, Moscow State Univ. p.106 (1971).
20. N.P.Samios *et al.*, *Rev. Mod. Phys.*, **46**, 49 (1974).
21. S.I.Sukhoruchkin, *Symmetry in Subat. Phys.*, Adelaide, AIP-539, 142 (2000).
22. A.A.Pivovarov, *Yadernaja Fizika* **65**, no.7, 1352 (2002).
23. R.Frosch, *Nuovo Cimento A* **104**, 913 (1991) and references therein.
24. S.I.Sukhoruchkin, Proc. Symp. New Projects Nucl. Phys., Messina, 2002. World Sci., 2003, p.362.
25. S.I.Sukhoruchkin, *Progr. Theor. Phys., Suppl.*, **146**, 623 (2002).