

# COMBINED ANALYSIS OF NUCLEAR DATA AND PARTICLE MASSES

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## 1. Introduction

Neutron resonance spectroscopy could play an important role in the development of the Standard Model - a modern theory of all interactions [1] except gravitation and dark matter problem. A specific position of scalar and vector field masses among masses of other particles and constituent quarks was considered in [2]. Between masses of these fields (boxed in Table 1, top), other particle masses and stable nuclear intervals a correlation (named fine- and superfine structure) was established. Recently performed analysis [3] of mass spectra of all particles from the compilation PDG-2016 [1] confirmed discussed earlier "tuning effect" in particle masses and relations [4] between masses of nucleons and the electron (CODATA relations [2]).

Presence of stable intervals of 104 MeV and 142 MeV close to masses of the muon and the pion ( $n=13$  and  $17$  of the CODATA period  $\delta = 16m_e$ ) in the particle mass spectrum was noticed earlier by different authors [5,6]. The value  $\delta=8.176$  MeV was connected [5,6] with the proximity of d-quark mass estimate  $m_d=4.78$  MeV [1] and pion charge splitting  $4.594$  MeV to  $9m_e=4.599$  MeV  $= \Delta$ . Simultaneously, there is a proximity of pions parameters  $f_\pi$ ,  $m_\pi-m_e$  and  $\Delta M_\Delta=147$  MeV (quark interaction in NRCQM, Nonrelativistic Constituent Quark Model) to integers  $n=16,17,18$  of the common period  $\delta$ . It is shown in [7] that QCD dynamics is based on gluon quark-dressing effect (from the Dyson-Schwinger equations and lattice QCD calculations) and is resulted in the constituent quark mass  $M_q \approx 400$  MeV close to the standard estimates of constituent quark masses in NRCQM  $M_q = m_\Xi/3=441$  MeV  $= 3\Delta M_\Delta$  ( $n=3 \times 18$ ) and  $M_q'' = m_\rho/2=388$  MeV  $\approx 3f_\pi$  ( $n=3 \times 16$ ). The ratio between masses of two fermions, namely, the electron and constituent quark  $m_e/M_q=(0.511 \text{ MeV}/441 \text{ MeV})=115.8 \cdot 10^{-5}$  is close to the ratio  $1/27.32 = 115.7 \cdot 10^{-5}$  in the tuning effect and to the QED radiative correction  $\alpha/2\pi = 115.9 \cdot 10^{-5}$ . V. Belokurov, D. Shirkov and R. Feynman [8,9] suggested that similar factor close to  $\alpha/2\pi$  (correction to the electron magnetic moment) is contained also in the electron mass itself.

The fundamental origin of observed tuning effects (including common fine structure in particle masses and in nuclear data) is connected with an important role of QCD as SM-component. We observe the fine structure and long-range correlations with  $m_e$ ,  $\Delta = 9m_e$  and  $\Delta M_\Delta = 32\Delta$  [6] in nuclear data because the hadronization and mass generation in QCD is a base for the nuclear physics. Intervals of common fine structure in CODATA relations ( $n=17,18$ ) and in nuclear data ( $n=13,14-18$  [6]) are expressed as:

$$D = \Delta M = n \times 9.5 \text{ keV}; \quad n = 13, 14, 16, 17, 18 \quad (1)$$

The value of the period  $\delta'=9.5 \text{ keV}=8\varepsilon'$  is boxed in the central left part of Table 1. Manifestation of this parameter in positions of neutron resonances in light nuclei (top) and in the near-magic nuclei with  $N=82$  ( $^{141}\text{Ce}$  and  $^{142}\text{Pr}$ , center of Table 2 left) and in low-lying excitations of neighbour  $^{143}\text{Ce}$  is presented in Table 2 together with the position of resonances at integer values of  $1/8$  part of the  $\delta'$ , namely, at integers of the parameter  $\varepsilon'=1.188 \text{ keV}$ , found earlier [5,6] in nonstatistical effects in many nuclei.

In the distribution of differences ( $\Delta M$ ) between all accurately known particle masses the grouping effect was found at the muon mass ( $\Delta M=104$  eV,  $13\delta-m_e$ ), the pion mass ( $\Delta M=142$  MeV,  $17\delta+m_e$ ), in regions of the constituent quark mass in NRCQM ( $\Delta M=445-460$  MeV) and at the bottom quark mass ( $\Delta M=3959$  MeV close to  $9M_q=3969$  MeV). It allows to represent as a single mass sequence the vector boson masses  $M_Z=91.19$  GeV= $13\delta^\circ-M_q=L\cdot M_q$  and  $M_W=80.38$  GeV= $13\cdot 16M_q''$ , the top quark mass  $m_t=172$  GeV (close to  $3\times 16\delta^\circ=169$  GeV), and finally, scalar field mass,  $M_H=125$  GeV (close to  $18\delta^\circ=126$  GeV) with the period  $\delta^\circ=16M_q=(\alpha/2\pi)^{-1}\delta$ . Rapidly increasing number of accurately estimated values of particle masses allows to check CODATA relation with the forthcoming file PDG-2018. Besides nuclear fine structure effects with intervals multiple to 161-170 keV (n=17,18), additional systems of stable intervals corresponding to n=13,14,16 with the same period  $\delta=9.5$  keV were found [6]. Simultaneously, in neutron resonance spacing distributions second order effects with the same above mentioned small QED parameter  $\alpha/2\pi$  were found as superfine structure with the period  $\delta''=11$  eV= $(\alpha/2\pi)^2\delta=(\alpha/2\pi)^3\delta^\circ$ . It is shown in Table 1, where above discussed intervals of the tuning effect (starting from NRCQM parameters, line X=0, M=3), stable spacing in particle masses spectrum  $104$  MeV  $\approx m_\mu$  and  $m_\pi$  (n=13,17, line X=0, M=1) and corresponding intervals of fine and superfine structures (lines X=1 and 2) are presented as different power X of discussed factor  $\alpha/2\pi \approx 1/32 \times 27$  and numbers n=1,13,16,17,18 in the expression  $n\cdot 16m_e(\alpha/2\pi)^X M$ .

**Table 1.** Representation of parameters of tuning effects in particle masses (top) and nuclear data (bottom) with the expression  $n\cdot 16m_e(\alpha/2\pi)^X M$  and different values of the X-power of QED factor  $\alpha/2\pi$  and integers M,n. Boxed are groups of values differing with  $\alpha/2\pi$ .

X	M	n = 1	n = 13	n = 16	n = 17	n = 18	n = 18·6
-1	3/2			$m_t=172.0$			
GeV	1	$16M_q=\delta^\circ$	$M_Z=91.2$	$M'_H=115$		$M_H=126$	
	1/2	$(m_b-M_q)$		$M^{L3}=58$			
0	1	$16m_e=\delta=8\varepsilon_o$	$m_\mu=106$	$f_\pi=130.7$	$m_\pi-m_e$	$\Delta M_\Delta=147$	$2M_q$
MeV	3	NRCQM		$M''_q=m_\rho/2$		$M_q=441=\Delta E_B$	
1	1				$k\delta-m_n-m_e=$	$170 = m_e/3$	
					$=161.65$		
keV	8	CODATA			$\delta m_N=1293.3$		
1	1	$9.5=\delta'=8\varepsilon'$	123	152	$\Delta^{TF}=161$	170 (Sn)	$\varepsilon_o=2m_e$
keV	3				484 ( $E^*$ )	512 (Pd)	
	4		492		648 (Pd)	682 (Co)	
	6					1023 (Os)	
	8		984	1212	1293 ( $E^*$ )	1360 (Te)	
2	1	$11=\delta''=8\varepsilon''$	143	176	186 (Nd)		$\varepsilon'=1188$
eV	2				377 Nd)		
	4,6		570 (Sb)		749 (Br,Sb,Rh)	1205 (Os)*	
	8				1500 (Pd,Hf,Sb,Rh)		
	8×5				7498 (Pd)	M=3	$\varepsilon''=1.35$

\* Before recoil correction

## 2. Fine structure in nuclear excitations

General character of the QCD dynamics is reflected in proximities to QED correction of ratios of fine structure parameters in nuclear data and particle masses to well-known parameters of strong interaction  $m_\pi=140$  MeV and  $\Delta M_\Delta=147$  MeV ( $161 \text{ keV}/m_\pi=115 \cdot 10^{-5}$  and  $170.3 \text{ keV}/147 \text{ MeV}=116 \cdot 10^{-5}$ ). We should mention here three aspects.

1) Position of neutron resonance is a difference between excitation energy and neutron separation energy, hence, now one can assign nonstatistical effects in neutron resonance positions to the common structure in particle masses (CODATA) and nuclear data ( $n=17,18$  of the period  $9.5 \text{ keV}=\delta'$ ). This interval  $\delta'$  was directly observed by M. Ohkubo in the position of strong resonances of near-magic  $^{141}\text{Ce}$  [10] (Table 2).

2) Observed by K. Ideno [11] superfine structure in  $^{124}\text{Sb}$  with the period  $11 \text{ eV}=\delta''$  (see Table 1, Fig. 8 in [12]) could serve as a second example of a role of neutron spectroscopy in SM-development due to the fact that a ratio between these parameters  $\delta''/\delta'=11 \text{ eV}/9.5 \text{ keV}=115.8 \cdot 10^{-5}$  is close to  $\alpha/2\pi$ . In Table 1 (bottom) similar ratios between superfine intervals  $D=373\text{--}570\text{--}1501 \text{ eV}$  in  $^{124}\text{Sb}$  (Fig. 186 in [6]),  $D=748\text{--}1495 \text{ eV}$  in  $^{104}\text{Rh}$ ,  $D=749 \text{ eV}$  in  $^{80}\text{Br}$ ,  $D=1497\text{--}7498 \text{ eV}$  in  $^{107}\text{Pd}$  (Fig. 191 [6]),  $D=757\text{--}1509 \text{ eV}$  in  $^{127,179}\text{Hf}$ ,  $D=186\text{--}377 \text{ eV}$  in  $^{146,149}\text{Nd}$  (Fig. 192 [6]),  $D=1205 \text{ eV}$  in  $^{187,188}\text{Os}$  (Fig. 193 [6]), and corresponding stable fine structure excitations in the same or neighbour nuclei are presented. Such relation could provide an indirect confirmation of QED factor  $\alpha/2\pi$ .

**Table 2.** Comparison of positions and spacing in light and near-magic nuclei with the integer values of the parameter of the fine structure  $\varepsilon' = \delta'/8 = 1.188 \text{ keV}$  [6].

*Top:* Positions  $E'_n$  of strong neutron resonances in light and magic nuclei and the periodicity in spacing distributions in resonances of  $^{61}\text{Ni}$  (top right).

*Center:* Values  $E_n$  in nuclei with  $N=83=82+1$ , maxima in spacing distributions of  $^{141}\text{Ce}$ .

*Bottom left:* Positions of strong neutron resonances in isotopes with  $Z=35\text{--}39$  are compared with integer number of the period  $\varepsilon'=1.188 \text{ keV}=9.505 \text{ keV}/8$  found in positions of strong resonances in  $Z=57\text{--}59$ ,  $N=83$  nuclei (center). *Bottom right:* Excitation energies  $E^*$  of  $^{143}\text{Ce}$ .

Nucl.	Ca-Ni	$^{61}\text{Ni}$	$^{61}\text{Ni}$	$^{61}\text{Ni}$	$^{61}\text{Ni}$	$^{61}\text{Ni}$
$E_n, l_n=0, D(\text{keV})$	18.8	4.8	9.3	14.1	19.0	24.7
$k(\varepsilon')$	16	4	8	12	16	20
$k \times \varepsilon'$	19.0	4.8	9.6	14.4	19.0	24.7
Nucl.	$^{141}\text{Ce}$	$^{141}\text{Ce}$	$^{142}\text{Pr}$	$^{141}\text{Ce}$	$^{141}\text{Ce}$	$^{141}\text{Ce}$
$J_i^\pi$	$1/2^+$	$1/2^+$	$(5/2^-)$			
$\Gamma_n^o, \text{meV}$	660*	3060*	160	D	D	D
$E_n$	9.573	21.570	9.598	21.7	43.1	86.2
$E^*, E'_n$	<span style="border: 1px solid black;">9.505</span>	<span style="border: 1px solid black;">21.418</span>	<span style="border: 1px solid black;">9.530</span>			
$m(8\varepsilon')$	1	9/4	1	9/4	9/2	9
$m \times 8\varepsilon'$	<span style="border: 1px solid black;">9.504</span>	21.384	<span style="border: 1px solid black;">9.504</span>	21.4	42.5	85
Nucl.	$^{140}\text{La}$	$^{80}\text{Br}$	$^{82}\text{Br}$	$^{86}\text{Rb}$	$^{143}\text{Ce}$	$J_o^\pi=3/2^-$
$J_i^\pi$	$3^+$	$l_n=0$	$l_n=0$	$l_n=0$	$7/2^-$	$5/2^-$
$\Gamma_n^o, \text{meV}$	54	72.0	120	159	$E^*$	$E^*$
$E_n$	1.179	1.201	1.209	2.398		
$E^*, E'_n$	<span style="border: 1px solid black;">1.170</span>	<span style="border: 1px solid black;">1.186</span>	<span style="border: 1px solid black;">1.194</span>	2.370	18.9	42.3
$m(8\varepsilon')$	1/8	1	1	2	2	9/2
$m \times 8\varepsilon'$	1.188	1.188	1.188	2376	<span style="border: 1px solid black;">19.0</span>	42.77

In Fig. 1 and Table 3, new results of fine structure analysis in recently published data are presented. Boxed are excitations in light nuclei which belong to fine structure with  $n=17$  ( $E^*=\delta m_N$  etc. [12]). Such excitations in  $^{59}\text{Co}$ ,  $^{41}\text{K}$  and  $^{116}\text{Sn}$  were noticed by O.I. Sumbayev [13] in data from  $\gamma$ -ray compilation [14]. Presence of the fine and superfine structures simultaneously in low-lying excitations and in neutron resonances was found in the regions around  $N=50$ ,  $Z=51$  and  $Z=72$  (Hf, Os). Proximity of intervals of both structures in different nuclei could be assigned to meson exchange dynamics [6,15].

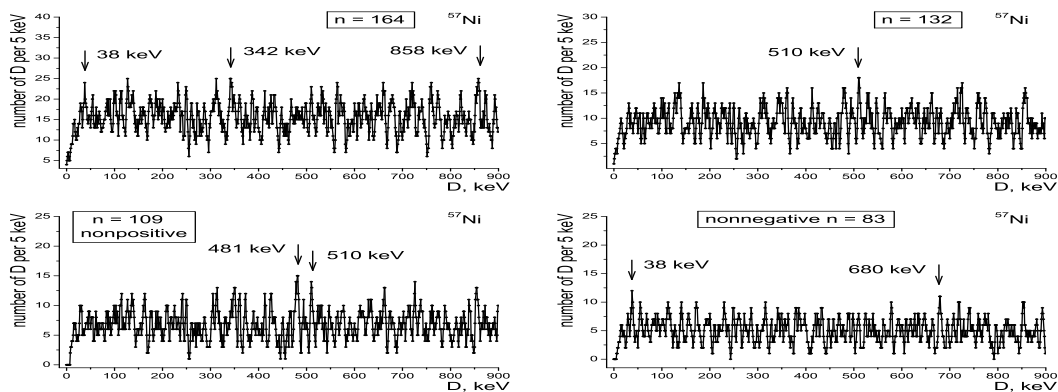
Neutron resonances correspond to a part of nuclear excitation spectra. In compilation ENSDF appearance of neutron resonances in the spectra of states can be seen as the groping effect. Such groupings were found by S.L. Sakharov [16] (periodicity in positions of these groupings). Results are similar to the correlation noticed earlier in [5].

Returning to the check of CODATA with files of nuclear data (CRF, NRF, MDF), we should notice that combined analysis of these files is important for development of truly microscopic models based on QCD. Quantum numbers of nuclear states should be measured. This time most of neutron resonances have uncertain spin/parity assignment. For example, in new data for excitations in near-magic  $^{57}\text{Ni}$  spacing distributions (shown in Fig. 1) could be determined only for groups of states (see partial distributions which contain maxima at  $D=342\text{ keV}=36\delta'$ , of low-lying levels),  $510\text{ keV}=3\times 18\delta'$  (negative parity levels),  $481\text{--}510\text{ keV}$  with small  $J < 9/2$  and  $680\text{ keV}$  (all positive parity levels).

Marked values in Table 3 [6] belong to the discussed system  $k(m_e/3)$  or  $k(\delta m_N/8)$ .

**Table 3.** Excitations (in keV) in nuclei  $N=21,22$  (top),  $N=28,27$  and the period of  $161\text{ keV}$ .

$(Z-14)/2$ $A/Z$	<span style="border: 1px solid black;">3</span> $^{41}\text{Ca}$	2 $^{39}\text{Ar}$	<span style="border: 1px solid black;">1</span> $^{37}\text{S}$	<span style="border: 1px solid black;">1</span> $^{38}\text{S}$	1 $^{33}\text{S}$	1 $^{43}\text{S}$	0 $^{32}\text{Si}$	0 $^{35}\text{Si}$	
$E^*$	0.0	<span style="border: 1px solid black;">1943</span>	1267	<span style="border: 1px solid black;">646.2</span>	<span style="border: 1px solid black;">1292</span>	322	<span style="border: 1px solid black;">320.7</span>	1942	973.9
$2J^\pi$	$7^-$	$3^-$	$3^-$	$3^-$	$2^+$	$D$	$7^-$	$2^+$	$(3^+)$
$k\frac{\delta m_N}{8}$	0.0	1941	1293	646	1293	322	322	1941	971
$A/Z$	$^{53}\text{Ni } 2J_o=7^-$		$^{58}\text{Ni}$	$^{59}\text{Ni}$	$^{61}\text{Ni}$	$^{53}\text{Co}$	$^{59}\text{Co}$		
$E^*$	<span style="border: 1px solid black;">320(3)</span>	<span style="border: 1px solid black;">1292*</span>	<span style="border: 1px solid black;">1456*</span>	<span style="border: 1px solid black;">1454.2</span>	<span style="border: 1px solid black;">339.4</span>	<span style="border: 1px solid black;">1454.8</span>	<span style="border: 1px solid black;">646.2*</span>	<span style="border: 1px solid black;">1291.6</span>	<span style="border: 1px solid black;">1459</span>
$2J^\pi$	$(5^-)$	$(3^-)$	$(11^-)$	$2^+$	$3^-5^-$	$7^-$	$7^-$	$3^-$	$11^-$
$k\frac{\delta m_N}{8}$	322	1293	1454	1454	322	1454	647	1293	1454



**Fig. 1.** *Top:* Spacing distribution in all levels of  $^{57}\text{Ni}$  (at left) and in negative parity levels. *Bottom:* The same for negative parity levels with small spins and for nonnegative parity levels.

### 3. Analysis of particle masses in PDG–2016 file

In Tables 4–6, a continuation of the analysis [3] of particle masses from PDG–2016 [1] is presented. Table 7 contains new file PDG–2017. Values are given in the same order as they appear in Summary Tables and marked according to their uncertainty  $\Delta M$  (as it was done in [6,12]). In this work, distributions for averaging intervals  $\Delta=5$  MeV and 9 MeV (Tables 4–6) were used.

**Table 4.** Particle masses [4] (in MeV) known with the uncertainty less than 6 MeV (intervals 193–1304 MeV).

	Particle	$m_i$	$\Delta$	193	584	794 $\Delta=9$	932	1092	1304
1	leptons	electron	0.0						
	$\mu$	105.658					931 (13)		1303 (1)
	$\tau$	1776.82		191 (11)	584 (4)	792 (18)			1304 (12)
2	Unflav. mesons								
	$\pi^\pm$	139.570						1090 (1)	
	$\eta$	547.86							1306 (2)
	$\eta'(958)$	957.78							
	$\phi(1020)$	1019.46						1093 (4)	
	$b_1(1235)^*$	1229.5	3.2			796 (2)		1090 (1)	1306 (4)
	$f_2(1270)^*$	1275.5	0.8						1302 (6)
	$f_1(1285)$	1282.0	0.5	194 (2)	583 (6)				
	$a_2(1320)$	1318.3	0.5			794 (4)	934 (5)		
	$\eta(1405)^*$	1408.8	1.8		587 (8)				1303 (1)
	$f_1(1420)^*$	1426.4	0.9	191 (4)	584 (10)		933 (2)	1092 (7)	
	$\eta(1475)^{**}$	1476	4	194 (2,5)	584 (1)				
	$f_2'(1525)^{**}$	1525	5		585 (2)		934 (9)		
	$\pi_1(1600)^{**}$	1662	8	192 (7)		793 (7)	930 (11)		1306 (10)
	$\eta_2(1645)^{**}$	1617	5	191 (3,4)		794 (8,9)			
	$\omega_3(1670)^{**}$	1667	4	191 (5)	585 (11)	794 (10,11)			
	$\pi_2(1670)^*$	1672.2	3.0	192 (7)		793 (12)		1094 (8)	
	$\rho_3(1690)^*$	1688.8	2.1			797 (1)			
	$f_0(1710)^{**}$	1723	6	191 (6)		795 (15)			
	$\phi_3(1850)^{**}$	1854	7	192 (7,11)	582 (5)	791 (19)			1306 (2)
	$a_4(2040)^{**}$	1995	8		587 (8,13)	797 (21)			
3	strange mesons								
	$K^\pm$	493.677					932 (1,2)		
	$K^*(892)^\pm$	891.66			584 (1)	797 (1)	931 (3)		
	$K_1(1270)^{**}$	1272	7		582 (5)				1306 (5)
	$K_1(1400)^{**}$	1403	7						1305 (8)
	$K_2^*(1430)^\pm$	1425.6	1.5	191 (3)	585 (9)		932 (1)	1093 (6)	
	$K_2(1770)^{**}$	1773	8			796 (16)			
	$K_3^*(1780)^{**}$	1776	7	192 (10)	583 (3)	793 (17)	932 (12)		1304 (11)
	$K_4^*(2045)^{**}$	2045	9	191 (12)	583 (15)				
4	charmed mesons								
	$D^\circ$	1864.83		192 (8,9)	583 (6)			1090 (2)	
	$D^\pm$	1869.58			584 (12)		930 (4)	1094 (3)	
	$D^*(2010)^\pm$	2010.28			585 (9,10,14)				
	$D_1(2420)^\circ$	2420.8	0.5					1090 (10)	1305 (3)
	$D_2^*(2460)^\pm$	2465.4	1.3			798 (11,12,13)	934(10)	1091 (11)	
5	charmed, strange mesons								
	$D_s^\pm$	1968.27		192 (10,11)	586 (7)	798 (20)			
	$D_s^{*\pm}$	2112.1	0.4		583 (16)	797 (3,4,5,23)		1093 (4)	1303 (13)
	$D_{s0}^*(2317)^\pm$	2317.7	0.6			794 (6,7)	934 (7)		
	$D_{s1}(2460)^\pm$	2459.5	0.6			798 (9,10)	934 (9)		
	$D_{s1}(2536)^\pm$	2535.10							1306 (4)
	$D_{s2}^*(2573)^*$	2569.1	0.8			794 (16,17,18)			1303 (17)
	$D_{s1}^*(2700)^\pm$	2708.3	3.4	190 (14)			932 (12,13,16)		1304 (8,9)
6	bottom mesons								
	$B^\pm$	5279.31					932 (19)		
	$B_1(5721)^{+*}$	5725.9	2.7	194 (20)					1305 (18)
7	bottom strange mesons								
	$B_s^\circ$	5366.82			582 (20)				
9	$c\bar{c}^*$ mesons								
	$\eta_c(1S)$	2983.4	0.5	191 (16)		790 (26)			
	$J/\psi(1S)$	3096.90		191 (17)		790 (28)			
	$\chi_{c0}(1P)$	3414.75					932 (18)		1303 (13)
	$\chi_{c1}(1P)$	3510.66					933 (14)	1090 (10)	

Table 4. Continued.

	Particle	$m_i$	$\Delta$	193	584	794 $\Delta=9$	932	1092	1304	
10	$h_c(1P)$	$?^?(0^{+-})$	3525.38		586(18)		933(15)			
	$\chi_{c2}(1P)$	$0^+(2^{++})$	3556.20			790(25,29)		1091(11)	1304 (14)	
	$\eta_c(2S)^*$	$0^+(0^{-+})$	3639.2	1.2	584(19)		931(16)			
	$\psi(2S)$	$0^-(1^{--})$	3686.10					1094(12)		
	$\psi(3770)$	$0^-(1^{--})$	3773.13			790(26)			1302 (15)	
	$\psi(3823)^*$	$?^?(2^{--})$	3822.2	1.2					1304 (16)	
	$X(3872)$	$0^+(1^{++})$	3871.69			792(27)	932(17)		1303 (17)	
	$X(3900)^*$	$1^+(1^{+-})$	3886.6	2.4		790(28)				
	$X(4140)^*$	$0^+(??^+)$	4146.9	3.1				1092(13)		
	$X(4140)^*$	$0^+(??^+)$	4146.9	3.1				1092(13)		
	$X(4360)^{**}$	$?^?(1^{--})$	4346.9	6			791(29)	932(18,19)		
	$\psi(4415)^{**}$	$0^-(1^{--})$	4421	4					1305 (18)	
	$X(4660)^{**}$	$?^?(1^{--})$	4643	9	193(18)				1306 (19)	
	11	$b\bar{b}$	mesons							
		$\eta_b(1S)^*$	$0^+(0^{-+})$	9399.0	2.3					
		$\Upsilon(1S)$	$0^-(1^{--})$	9460.30			795(30)			
		$\Upsilon(1D)^*$	$0^-(2^{--})$	10163.7	1.4	192(21)				
		$\chi_{b0}(2P)$	$0^+(0^{++})$	10232.5	0.4		584(21)			
$\chi_{b1}(2P)$		$0^+(1^{++})$	10255.46				795(30)			
$\Upsilon(3S)$		$0^-(1^{--})$	10355.2	0.5	192(21)					
$X(10610)^{\pm*}$		$1^+(1^+)$	10607.2	2.0		584(21)				
12		$n$	$1/2(1/2^+)$	939.5654		585(2)		930(4)		
		$\Lambda$	$0(1/2^+)$	1115.683						1305 (3)
		$\Lambda(1405)1/2^-*$	$0(1/2^-)$	1405.1	1.3					1303 (9)
		$\Lambda(1520)3/2^-*$	$0(3/2^-)$	1519.5	1.0			798(6)	934(8)	
		$\Sigma^\circ$	$1(1/2^+)$	1192.642		191(1)	584(3,4)			1094(5)
		$\Sigma(1385)^\circ*$	$1(3/2^+)$	1383.7	1.0	191(1)	586(7)		934(7)	
		$\Xi^\circ$	$1/2(1/2^+)$	1314.86	0.20			797(3)		
		$\Xi^-$	$1/2(1/2^+)$	1321.71	0.07			797(5)	930(6)	1306 (7)
		$\Xi(1530)3/2^{+\circ}$	$1/2(3/2^+)$	1531.80	0.32	191(6)			945(10)	
		$\Xi(1820)3/2^-*$	$1/2(3/2^-)^{**}$	1823	5				931(3)	
	$\Xi(2030)^{**}$	$1/2(\geq 3/2^?)$	2025	5			786(2,22)			
	$\Omega^-$	$0(3/2^+)$	1673.45		191(9)		794(13,14)		1092(9)	
	$\Omega(2250)^{-**}$	$0(?^?)$	2252	9		585(11)		932(5,6)	1304 (14)	
	13	charmed	baryons							
		$\Lambda_c^+$	$0(1/2^+)$	2286.46				793(24)	1094(5)	
		$\Lambda_c(2595)^+$	$0(1/2^-)$	2592.25			583(14)		930(11,15)	1094(12)
		$\Lambda_c(2625)^+$	$0(3/2^-)$	2628.11		191(15)	583(15)			1306 (7)
		$\Lambda_c(2940)^+*$	$0(5/2^+)$	2939.3	1.5		586(18)		932(17)	
$\Sigma_c(2455)^\circ$		$1(1/2^+)$	2453.75		192(13)	584(12)	792(8)	934(8)		
$\Sigma_c(2520)^\circ$		$1(3/2^+)$	2518.48		190(14)		795(15)		1092(6,7)	
$\Sigma_c(2800)^\circ^{**}$		$1(3/2^+)$	2906	7	190(17)		794(23)		1304 (16)	
$\Xi_c^\circ$		$1/2(1/2^+)$	2470.85			584(17)	797(14)		1302 (15)	
$\Xi_c^{\circ*}$		$1/2(1/2^+)$	2577.9	2.9		583(13)		933(14)	1304 (5,6)	
$\Xi_c(2645)^\circ$		$1/2(3/2^+)$	2645.9	0.5	192(13)		792(19)			
$\Xi_c(2790)^\circ*$		$1/2(1/2^-)$	2791.9	3.3	192(16)		797(21)			
$\Xi_c(2815)^\circ*$		$1/2(3/2^-)$	2819.6	1.2	191(15)		795(22)			
$\Xi_c(2970)^\circ*$		$1/2(?^?)$	2968.0	2.6					1306 (10)	
$\Xi_c(3055)^*$		$1/2(?^?)$	3055.1	1.7		584(17,19)			1092 (13)	
$\Xi_c(3080)^\circ*$		$1/2(?^?)$	3079.9	1.4			794(24,27)		1304 (11,12)	
$\Omega_c^{\circ*}$		$0(1/2^+)$	2695.2	1.7		583(16)				
$\Omega_c(2770)^\circ*$		$0(3/2^+)$	2765.9	2.0			798(20,25)		1092 (8,9)	
13	bottom	baryons								
	$\Lambda_b^\circ$	$0(1/2^+)$	5619.51		192(19)					
	$\Lambda_b(5920)^\circ$	$0(3/2^-)$	5919.81		194(20)					
	$\Sigma_b^{+*}$	$1(1/2^+)$	5811.3	1.9	192(19)					
	$\Xi_b(5945)^\circ*$	$1/2(3/2^+)$	5948.9	1.6		582(20)			1306 (19)	
	$P_c(4450)^{+*}$	4449.8	3.0	193(18)						

Table 5. Particle masses [4] (in MeV) known with the uncertainty less than 6 MeV (intervals 336–3371 MeV).

	Particle	$m_i$	$\Delta$	336	447	460	1673	1688	3371
1	leptons	el., $\nu$	0.0				1673 (1,2)	1688 (1)	
	$\mu$	105.658					1673 (3,4)		
	$\tau$	1776.82		336 (22)		460 (7,9)	1673 (4)		

Table 5. Continued.

	Particle	$m_i$	336	447	460	1673	1688	3371	
2	Unflav. mesons								
	$\pi^\pm$	$1^-(0^-)$	139.570					3371(1)	
	$\eta$	$0^+(0^{-+})$	547.86						
	$\rho(770)$	$1^+(1^{--})$	775.26	336(1)			1688(2,3)	3371(3)	
	$\omega(782)$	$0^-(1^{--})$	782.65	336(2)	447(2)		1673(5,6)	1688(4)	
	$\eta'(958)$	$0^+(0^{-+})$	957.78	336(6)	447(4,5,6)	460(1)	1673(8)	1688(7)	3371(2)
	$\phi(1020)$	$0^-(1^{--})$	1019.46			460(3)	1673(9)	1688(8)	
	$b_1(1235)^*$	$1^+(1^{+-})$	1229.5	336(3)	447(2,7,8)	460(4)	1673(11)		
	$f_2(1270)^*$	$0^+(2^{++})$	1275.5	336(5)	447(10)			1688(10)	3371(5)
	$f_1(1285)$	$0^+(1^{++})$	1282.0	336(9)				1688(11)	
	$\eta(1295)^{**}$	$0^+(0^{-+})$	1294	336(6)			1673(12)	1688(1)	
	$a_2(1320)$	$1^-(2^{++})$	1318.3			460(8,9)			
	$\eta(1405)^*$	$0^+(0^{--})$	1408.8		447(6,14)	460(13,14)	1673(17)	1688(14)	
	$f_1(1420)^*$	$0^+(1^{++})$	1426.4		447(16)		1673(19)		
	$\eta(1475)^{**}$	$0^+(0^{-+})$	1476			460(3)			
	$f_0(1500)^{**}$	$0^+(0^{++})$	1504			460(15)			
	$f_2'(1525)^{**}$	$0^+(2^{++})$	1525	336(7,13)	447(18)				
	$\pi_1(1600)^{**}$	$1^-(1^{-+})$	1662	336(10,16)	447(19)				
	$\eta_2(1645)^{**}$	$0^+(0^{-+})$	1617	336(9)					
	$\omega_3(1670)^{**}$	$0^-(3^{--})$	1667		447(20)				
	$\pi_2(1670)^*$	$1^-(2^{-+})$	1672.2	336(17)	447(7)		1673(1)		
	$\rho_3(1690)^*$	$1^+(3^{--})$	1688.8	336(19)		460(4)		1688(1)	
$f_0(1710)^{**}$	$0^+(0^{++})$	1723	336(11)	447(9,10)			1688(15)		
$\phi_3(1850)^{**}$	$0^-(3^{--})$	1854	336(12)	447(12,13,14)	460(18)	1673(20)			
$a_4(2040)^{**}$	$1^-(4^{++})$	1995	336(16)		460(16,19,21)		1688(19)	3371(6)	
3	strange mesons								
	$K^\pm$	$1/2(0^-)$	493.677		447(1)	460(1)			
	$K^*(892)^\pm$	$1/2(1^-)$	891.66	336(3)			1673(7)	1688(5)	
	$K_1(1270)^{**}$	$1/2(1^+)$	1272	336(4)	447(9)			3371(4)	
	$K_1(1400)^{**}$	$1/2(1^+)$	1403		447(4,12)	460(2,10)	1673(15)		
	$K_2^*(1430)^\pm$	$1/2(2^+)$	1425.6		447(15)		1673(12)		
	$K_2(1770)^{**}$	$1/2(2^-)$	1773	336(20)	447(11)	460(5)			
	$K_3^*(1780)^{**}$	$1/2(3^-)$	1776	336(21)		460(6,8)	1673(3)		
	$K_4^*(2045)^{**}$	$1/2(4^+)$	2045					3371(7)	
	4	charmed mesons							
$D^\circ$		$1/2(0^-)$	1864.83	336(13,14)		460(10,11,13)	1688(17)		
$D^\pm$		$1/2(0^-)$	1869.58	336(15)	447(15,16,21)	460(12,14)	1688(18)		
$D^*(2010)^\pm$		$1/2(1^-)$	2010.28	336(17,18)	447(22,23)	460(21)	1673(22)		
$D_1(2420)^\circ$		$1/2(1^+)$	2420.8			460(24)		3371(9)	
$D_2^*(2460)^\pm$		$1/2(2^+)$	2465.4				1688(3)	3371(13,14)	
5		charmed, strange mesons							
	$D_s^\pm$	$0^+(0^-)$	1968.27		447(17,18)	460(15)	1673(12)		
	$D_s^{*\pm}$	$0(?)$	2112.1	336(20,21,22)	447(19,20)	460(22)			
	$D_{s0}^*(2317)^\pm$	$0(0^+)$	2317.7		447(21,26)	460(18)			
	$D_{s1}(2460)^\pm$	$0(1^+)$	2459.5	336(25)	447(23,27)	460(20)	1673(6)	1688(2,20)	3371(11,12)
	$D_{s1}(2536)^\pm$	$0(1^+)$	2535.10		447(29)				
	$D_{s2}^*(2573)^*$	$0(2^+)$	2569.1	336(26)		460(22)	1673(7)		
	$D_{s1}^*(2700)^\pm$	$0(1^-)$	2708.3			460(23)	1688(8)		
6	bottom mesons								
	$B^\pm$	$1/2(0^-)$	5279.31	336(32)					
	$B^*$	$1/2(1^-)$	5324.65				1688(22)		
	$B_1(5721)^{+*}$	$1/2(1^+)$	5725.9		447(33)		1688(24)		
	$B_2^*(5747)^{+*}$	$1/2(2^+)$	5737.2			460(31)			
$B_J(5970)^+$	$1/1(?)^{**}$	5964					3371(17)		
7	bottom strange mesons								
	$B_s^\circ$	$0(0^-)$	5366.82		447(34)	460(32)		3371(6)	
	$B_s^{**}$	$0(1^-)$	5415.4					3371(7)	
	$B_{s1}(5830)^\circ$	$0(1^+)$	5828.63	447(35)	460(32)		3371(10,11)		
$B_{s2}^*(5640)^\circ$	$0(2^+)$	5839.84				3371(14,15)			
8	bottom charmed mesons								
	$B_c^{**}$	$0(0^-)$	6275.1	336(34)	447(35,36)	460(33)		3371(18)	
9	$c\bar{c}$ mesons								
	$\eta_c(1S)$	$0^+(0^{-+})$	2983.4	336(28)	447(29)		1673(13)	1688(12)	
	$J/\psi(1S)$	$0^-(1^{--})$	3096.90		447(30)	460(27)	1673(18,19)	1688(13,14)	
	$\chi_{c0}(1P)$	$0^+(0^{++})$	3414.75	336(29)	447(31)	460(28)		1688(15)	
	$\chi_{c1}(1P)$	$0^+(1^{++})$	3510.66			460(26)		1688(16)	3371(1)
	$h_c(1P)$	$?^?(0^{+-})$	3525.38		447(32)		1673(20)		

Table 5. Continued.

	Particle	$m_i$	336	447	460	1673	1688	3371
	$\chi_{c2}(1P)$	$0^+(2^{++})$	3556.20		460(27)		1688(17,18)	
	$\eta_c(2S)^*$	$0^+(0^{-+})$	3639.2			1673(21)	1688(22)	
	$\psi(2S)$	$0^-(1^{--})$	3686.10	336(30)	460(29)	1673(26)	1688(19)	
	$X(3872)$	$0^+(1^{++})$	3871.69		460(28)			
	$X(3900)^*$	$1^+(1^{+-})$	3886.6		460(30)			
	$X(3915)^*$	$0^+(?^{++})$	3918.4	336(31)				3371(2)
	$\chi_{c2}(1P)^*$	$0^+(2^{++})$	3927.2			1673(23)	1688(23)	
	$X(4020)^*$	$1(?^?)$	4024.1	336(30)				
	$\psi(4040)^{**}$	$0^-(1^{--})$	4039				1688(24)	
	$X(4140)^*$	$0^+(??^+)$	4146.9		460(29)	1673(24)	1688(20,25)	3371(3)
	$\psi(4160)^{**}$	$0^-(1^{--})$	4191			1673(25)		
	$X(4260)^{**}$	$?^?(1^{--})$	4251	336(31)		1673(28,26)	1688(26)	
	$X(4360)^{**}$	$?^?(1^{--})$	4346.9		460(30)			
	$X(4660)^{**}$	$?^?(1^{--})$	4643			1673(27)		3371(4,5)
10	$b\bar{b}$	mesons						
	$\eta_b(1S)^*$	$0^+(0^{-+})$	9399.0		460(34)			
	$\chi_{b0}(1P)$	$0^+(0^{++})$	9859.44		460(34)			
	$\chi_{b1}(1P)$	$0^+(0^{++})$	9892.78	336(35)	460(35)			
	$h_b(1P)^*$	$?^?(1^{+-})$	9899.3	336(36)	460(36)			
	$\chi_{b2}(1P)$	$0^+(2^{++})$	9912.21		447(37)			
	$\Upsilon(2S)$	$0^-(1^{--})$	10023.26	336(37)				
	$\Upsilon(1D)^*$	$0^-(2^{--})$	10163.7		447(38)			
	$\chi_{b0}(2P)$	$0^+(0^{++})$	10232.5	336(35,36)				
	$\chi_{b2}(2P)$	$0^-(2^{+-})$	10268.65	336(38)				
	$\Upsilon(3S)$	$0^-(1^{--})$	10355.2	336(37)	447(37)	460(35,36)		
10	$X(10610)^{\pm*}$	$1^+(1^+)$	10607.2	336(38)	447(38)			
11		baryons						
	n	$1/2(1/2^+)$	939.5654	336(4,5)	447(1,3)	460(2)	1688(6)	
	$\Lambda$	$0(1/2^+)$	1115.683	336(1,2)			1673(10)	
	$\Lambda(1405)1/2^-*$	$0(1/2^-)$	1405.1		447(5,13)	460(11,12)	1673(16)	1688(13)
	$\Lambda(1520)3/2^-*$	$0(3/2^-)$	1519.5	336(12)	447(17)			
	$\Sigma^\circ$	$1(1/2^+)$	1192.642	336(7,8)				1688(9)
	$\Sigma(1385)^\circ*$	$1(3/2^+)$	1383.7	336(11)	447(3)		1673(14)	
	$\Xi^\circ$	$1/2(1/2^+)$	1314.86			460(5,6,7)	1673(13)	
	$\Xi^-$	$1/2(1/2^+)$	1321.71	336(10)	447(11)			
	$\Xi(1530)3/2^{+\circ}$	$1/2(3/2^+)$	1531.80	336(8,14,15)		460(16)		
	$\Xi(1820)3/2^-$	$1/2(3/2^-)^{**}$	1823			460(17)	1688(16)	
	$\Xi(2030)^{**}$	$1/2(\geq 3/2^?)$	2025	336(19)	447(24)			
	$\Omega^-$	$0(3/2^+)$	1673.45	336(18)	447(8)		1673(2)	
	$\Omega(2250)^{-**}$	$0(?^?)$	2252	336(23)	447(25)	460(21)	1673(23)	3371(8)
12		charmed baryons						
	$\Lambda_c^+$	$0(1/2^+)$	2286.46		460(17)			
	$\Lambda_c(2595)^+$	$0(1/2^-)$	2592.25	336(23)	460(25)			3371(17)
	$\Lambda_c(2625)^+$	$0(3/2^-)$	2628.11	336(27)		1673(8)	1688(6)	
	$\Lambda_c(2880)^+$	$0(5/2^+)$	2881.53				1688(9)	
	$\Sigma_c(2455)^\circ$	$1(1/2^+)$	2453.75	336(24)	447(22)	460(19)	1673(5)	3371(10)
	$\Sigma_c(2520)^\circ$	$1(3/2^+)$	2518.48		447(28)		1673(12)	
	$\Sigma_c(2800)^\circ^{**}$	$1(3/2^+)$	2906	336(26)	447(27)		1673(11)	3371(18)
	$\Xi_c^\circ$	$1/2(1/2^+)$	2470.85		447(24)	460(21)	1673(24)	1688(4)
	$\Xi_c^{\prime\circ}$	$1/2(1/2^+)$	2577.9				1673(26)	1688(5)
	$\Xi_c(2645)^\circ$	$1/2(3/2^+)$	2645.9	336(28)	447(30)			1688(7)
	$\Xi_c(2790)^\circ*$	$1/2(1/2^-)$	2791.9	336(24,25)			1673(10)	
	$\Xi_c(2970)^\circ*$	$1/2(?^?)$	2968.0	336(27)	447(28,31)		1673(12,27)	1688(10,11)
	$\Xi_c(3055)^*$	$1/2(?^?)$	3055.1			460(25,26)	1673(14)	
	$\Xi_c(3080)^\circ*$	$1/2(?^?)$	3079.9	336(29)	447(32)		1673(15,16,17)	
	$\Omega_c^*$	$0(1/2^+)$	2695.2		447(25)		1673(9)	
	$\Omega_c(2770)^\circ*$	$0(3/2^+)$	2765.9		447(26)			1688(21)
13		bottom baryons						
	$\Lambda_b^\circ$	$0(1/2^+)$	5619.51	336(32,33)			1688(23)	3371(8)
	$\Sigma_b^{+*}$	$1(1/2^+)$	5811.3		447(34)	460(33)		
	$\Sigma_b^{*+*}$	$1(3/2^+)$	5832.1		447(36)		1688(25)	3371(12,13)
	$\Xi_b^\circ$	$1/2(1/2^+)$	5791.9					3371(9)
	$\Xi_b'(5935)^-$	$1/2(1/2^+)$	5935.02	336(34)			1688(26)	
	$\Xi_b(5945)^\circ*$	$1/2(3/2^+)$	5948.9					3371(16)
	$\Xi_b^*(5955)^-$	$1/2(1/2^+)$	5955.33	336(33)				
14		exotic baryons						
	$P_c(4450)^{+*}$		4449.8				1688(21)	



**Table 6.** Particle masses [4] (in MeV) known with the uncertainty less than 6 MeV (intervals 4425–3959 MeV).

	Particle	$m_i$	$\Delta$	4425	4640	3943	4406	4052	3959
1	leptons	el., $\nu$	0.0	4425(1)	4640(1)				
	$\mu$		105.658						
	$\tau$		1776.82					4052(13,14)	3960(11)
2	Unflav.	mesons							
	$\pi^\pm$	$1^-(0^-)$	139.570					4052(1)	
	$\eta$	$0^+(0^{-+})$	547.86						
	$\rho(770)$	$1^+(1^{--})$	775.26		4640(2)				
	$\eta'(958)$	$0^+(0^{-+})$	957.78				4406(1)		
	$b_1(1235)^*$	$1^+(1^{+-})$	1229.5	3.2				4052(2)	
	$f_2(1270)^*$	$0^+(2^{++})$	1275.5	0.8	4640(6,7)			4052(4)	
	$f_1(1285)$	$0^+(1^{++})$	1282.0	0.5	4640(8)				
	$\eta(1295)^{**}$	$0^+(0^{-+})$	1294	4	4640(9)				
	$a_2(1320)$	$1^-(2^{++})$	1318.3	0.5	4640(11)		4406(2)	4052(6)	3960(3)
	$\eta(1405)^*$	$0^+(0^{-+})$	1408.8	1.8	4425(10)	4640(15)	4406(7)		3960(7)
	$f_1(1420)^*$	$0^+(1^{++})$	1426.4	0.9			3940(3)	4406(10,11)	
	$\eta(1475)^{**}$	$0^+(0^{-+})$	1476	4			3939(4)		
	$f_0(1500)^{**}$	$0^+(0^{++})$	1504	6			4406(12)		
	$f_2'(1525)^{**}$	$0^+(2^{++})$	1525	5	4425(12)		4406(13)		
	$\pi_1(1600)^{**}$	$1^-(1^{-+})$	1662	8					3960(1)
	$\eta_2(1645)^{**}$	$0^+(0^{-+})$	1617	5	4425(14)				
	$\pi_2(1670)^*$	$1^-(2^{-+})$	1672.2	3.0		3947(5)		4052(7)	
	$\rho_3(1690)^*$	$1^+(3^{--})$	1688.8	2.1				4052(9)	
	$\phi_3(1850)^{**}$	$0^-(3^{--})$	1854	7	4425(15)				3960(12)
	$a_4(2040)^{**}$	$1^-(4^{++})$	1995	8		3940(10)		4052(17)	3960(16)
3	strange	mesons							
	$K^\pm$	$1/2(0^-)$	493.677						3960(1)
	$K_1(1270)^{**}$	$1/2(1^+)$	1272	7		4640(5)		4052(3)	
	$K_1(1400)^{**}$	$1/2(1^+)$	1403	7	4425(6,7)	4640(13)	4406(5)		3960(5)
	$K_2^*(1430)^\pm$	$1/2(2^+)$	1425.6	1.5			3941(2)	4406(8,9)	
	$K_2(1770)^{**}$	$1/2(2^-)$	1773	8				4052(10)	3960(9)
4	charmed	mesons							
	$D^0$	$1/2(0^-)$	1864.83			3046(7)	4406(15)	4052(15)	3960(13)
	$D^\pm$	$1/2(0^-)$	1869.58			3942(8)	4406(16)	4052(16)	3960(14,15)
	$D^*(2010)^\pm$	$1/2(1^-)$	2010.28			3943(11,12)			
5	charmed,	strange	mesons						
	$D_s^\pm$	$0^+(0^-)$	1968.27			3944(9)			
	$D_{s1}^*(2700)^\pm$	$0(1^-)$	2708.3	3.4					
6	bottom	mesons							
	$B^\pm$	$1/2(0^-)$	5279.31					4052(2)	3960(2)
	$B^*$	$1/2(1^-)$	5324.65			3941(1)		4052(3,4)	
	$B_1(5721)^{+*}$	$1/2(1^+)$	5725.9	2.7			4406(2,3)	4052(7,8)	
	$B_2^*(5747)^{+*}$	$1/2(2^+)$	5737.2	0.7	4425(4,16)			4052(9)	3960(9,10,11)
	$B_J(5970)^+$	$1/1(?)^{**}$	5964	5		4640(12,17)	3939(13)		
7	bottom	strange	mesons						
	$B_s^0$	$0(0^-)$	5366.82		4425(2)		3941(2,3)	4406(1)	4052(5,6)
	$B_s^{*0}$	$0(1^-)$	5415.4	1.5		4640(2)	3939(4)		
	$B_{s1}(5830)^0$	$0(1^+)$	5828.63		4425(6,8,18)	4640(1)	(8,10,18)	4052(10,11,13)	3960(13,14)
	$B_{s2}^*(5640)^0$	$0(2^+)$	5839.84		4425(20)			4052(19)	
8	bottom	charmed	mesons						
	$B_c^{*0}$	$0(0^-)$	6275.1	1.0	4425(15)		4406(15,16)		3960(17,22)
9	$cc''$	mesons							
	$\psi(4160)^{**}$	$0^-(1^{--})$	4191	5				4052(1)	
	$\psi(4415)^{**}$	$0^-(1^{--})$	4421	4	4425(1)				
	$X(4660)^{**}$	$?^?(1^{--})$	4643	9		4640(1)			
10	$b\bar{b}$	mesons							
	$\chi_{b0}(1P)$	$0^+(0^{++})$	9859.44			3943(14,15)		4052(18)	
	$\chi_{b1}(1P)$	$0^+(0^{++})$	9892.78			3944(16)		4052(19)	3960(18)
	$h_b(1P)^*$	$?^?(1^{+-})$	9899.3	0.8		3944(17)			3960(19)
	$\chi_{b2}(1P)$	$0^+(2^{++})$	9912.21						3960(20,21)
	$\Upsilon(2S)$	$0^-(1^{--})$	10023.26		4425(17)		4406(17)		
	$\Upsilon(1D)^*$	$0^-(2^{--})$	10163.7	1.4	4425(1)				
	$\chi_{b0}(2P)$	$0^+(0^{++})$	10232.5	0.4			4406(18)		3960(22)
	$\chi_{b1}(2P)$	$0^+(1^{++})$	10255.46		4425(18,19)	4640(16)			

**Table 6.** Continued.

	Particle	$m_i$	$\Delta$	4425	4640	3943	4406	4052	3959	
11	$\chi_{b2}(2P)$	$0^-(2+-)$	10268.65	4425(20)						
	$\Upsilon(3S)$	$0^-(1--)$	10355.2				4406(19)			
	$X(10610)^{\pm*}$	$1^+(1+)$	10607.2		4640(17)					
	baryons									
	n	$1/2(1/2^+)$	939.5654	4425(2)						
	$\Lambda$	$0(1/2^+)$	1115.683							
	$\Lambda(1405)1/2^-*$	$0(1/2^-)$	1405.1	4425(8,9)	4640(14)		4406(6)		3960(6)	
	$\Lambda(1520)3/2^-*$	$0(3/2^-)$	1519.5	4425(11)						
	$\Sigma^o$	$1(1/2^+)$	1192.642	4425(3)	4640(3,4)					
	$\Sigma(1385)^o*$	$1(3/2^+)$	1383.7	4425(5)		3941(1)	4406(4)			
	$\Xi^o$	$1/2(1/2^+)$	1314.86	4425(4)	4640(9)			4052(5)	3960(2)	
$\Xi^-$	$1/2(1/2^+)$	1321.71	0.07	4640(12)			4406(3)	3960(4)		
$\Xi(1530)3/2^{+o}$	$1/2(3/2^+)$	1531.80	0.32	4425(13)			4406(14)			
$\Xi(2030)**$	$1/2(\geq 3/2^2)$	2025	5			3939(13)				
$\Omega^-$	$0(3/2^+)$	1673.45				3946(6)		4052(8)		
13	bottom baryons									
	$\Lambda_b^o$	$0(1/2^+)$	5619.51	4425(3)	4640(16)	3947(5,6)	4406(17)		3960(8)	
	$\Lambda_b(5912)^o$	$0(1/2^-)$	5912.11		4640(5,6)	3944(9,14)	4406(12)			
	$\Lambda_b(5920)^o$	$0(3/2^-)$	5919.81		4640(7,8)	3940(15)		4052(15,16)		
	$\Sigma_b^{+*}$	$1(1/2^+)$	5811.3	1.9	4425(5,17)		3943(7,8)	4406(5,6,7)	4052(18)	3960(12)
	$\Sigma_b^{*+*}$	$1(3/2^+)$	5832.1	1.9	4425	4640(4)		4406(9,11)	4052(12,14)	3960(15)
					(7,9,10,18)					
	$\Xi_b^o$	$1/2(1/2^+)$	5791.9	0.5				4406(4)		
	$\Xi_b'(5935)^-$	$1/2(1/2^+)$	5935.02			4640(9)	3940(10)	4406(13,14)		3960(18,19)
	$\Xi_b(5945)^o*$	$1/2(3/2^+)$	5948.9	1.6	4425(11,12)		3938(11,16)	4406(19)		3960(20)
	$\Xi_b^*(5955)^-$	$1/2(1/2^+)$	5955.33		4425(13)	4640(10,11)	3945(12,17)			3960(16,21)
$\Omega_b^-$	$0(3/2^+)$	6046.4	1.9	4425(14)	4640(13,14,15)			4052	(17)	
14	exotic baryons									
$P_c(4450)^{+*}$		4449.8	3.0						3960(1)	

#### 4. General conclusions

Performed confirmation of CODATA relations between masses of nucleons and the electron provides a base for the Symmetry Motivated Electron–Based approach to the Standard Model development with the dominant role of two parameters of the electron: the mass value  $m_e$  and QED radiative correction [8,9]. This approach requires collection and analysis of new accurately measured data on particle masses and nuclear states.

Three parts of CODATA relations were considered:

1) The period  $\delta = 16m_e$  common for many different particles, including leptons and hadrons; this period is confirmed with the analysis of data from PDG reviews. Distinguished position of the pions parameters  $f_\pi, m_\pi, \Delta M_\Delta$  with  $n=16,17,18$  provide a direct confirmation of symmetry motivated origin of the common period  $\delta$ .

2) Fine structure with values of shifts 161 keV and  $8 \times 161$  keV coinciding with nucleon mass splitting was earlier observed in nuclear excitations. Only recently this splitting was estimated theoretically within very large uncertainty, but its appearance in nuclear data was noticed long ago.

Now members of fine structure in nuclear data are determined within 1 keV uncertainty.

3) Similar situation exists with the parameter 170 keV= $m_e/3$  frequently seen as the analog of above mentioned fine structure. A possibility to study directly this common fine structure is a unique opportunity of the nuclear and neutron resonance spectroscopies which should not be ignored (taking into account a possibility to study position of nucleon mass within the first just discussed correlation).

4) Confirmation of CODATA relations suggested by Y. Nambu should be supplement with efforts from neutron resonance spectroscopy to check the role of the QED correction.

**Table 7.** Particle masses (MeV) from PDG–2017 known with an uncertainty  $< 30$  MeV given without rounding up; values with one and two meaningful numbers after the point are given directly; values with uncertainty  $< 8$  MeV are marked by \*; values with uncertainty  $> 8$  MeV are marked by \*\*; values which belong to members of multiplets excluded from the analysis (see text and [3,6,12]) are marked by \*\*\*.

		Particle	$m_i$	$\Delta$			Particle	$m_i$	$\Delta$	
1	1	leptons	electron, $\nu$	0.511		5	$D_2^*(2460)^{\pm*}$	1/2(2 <sup>+</sup> )	2465.4	1.3
	2		$\mu$	105.658			charmed	strange	mesons	
	3		$\tau$	1776.82		54	$D_s^{\pm}$	0 <sup>+</sup> (0 <sup>-</sup> )	1968.18	
2		Unflav.	mesons			55	$D_s^{*\pm}$	0(??)	2112.1	0.4
		$f_\pi$		130.7	0.4	56	$D_{s0}^*(2317)^{\pm}$	0(0 <sup>+</sup> )	2317.7	0.6
	4	$\pi^{0***}$	1 <sup>-</sup> (0 <sup>-</sup> )	134.977		57	$D_{s1}(2460)^{\pm}$	0(1 <sup>+</sup> )	2459.5	0.6
	5	$\pi^{\pm}$	1 <sup>-</sup> (0 <sup>-</sup> )	139.571		58	$D_{s1}(2536)^{\pm}$	0(1 <sup>+</sup> )	2535.10	
	6	$\eta$	0 <sup>+</sup> (0 <sup>+</sup> )	547.862		59	$D_{s2}^*(2573)^*$	0(2 <sup>+</sup> )	2569.1	0.8
	7	$\rho(770)$	1 <sup>+</sup> (1 <sup>-</sup> )	775.26		60	$D_{s1}^*(2700)^{\pm*}$	0(1 <sup>-</sup> )	2708.3	3.4
	8	$\omega(782)$	0 <sup>-</sup> (1 <sup>-</sup> )	782.65		6	bottom	mesons		
	9	$\eta'(958)$	0 <sup>+</sup> (0 <sup>+</sup> )	957.78		61	$B^{\pm}$	1/2(0 <sup>-</sup> )	5279.32	
	10	$\phi(1020)$	0 <sup>-</sup> (1 <sup>-</sup> )	1019.46		62	$B^{0***}$	1/2(0 <sup>-</sup> )	5279.63	
	11	$b_1(1235)^*$	1 <sup>+</sup> (1 <sup>+</sup> )	1229.5	3.2	63	$B^*$	1/2(1 <sup>-</sup> )	5324.65	
	12	$f_2(1270)^*$	0 <sup>+</sup> (2 <sup>+</sup> )	1275.5	0.8	64	$B_1(5721)^{+*}$	1/2(1 <sup>+</sup> )	5725.9	2.7
	13	$f_1(1285)$	0 <sup>+</sup> (1 <sup>+</sup> )	1281.9	0.5	65	$B_1(5721)^{0***}$	1/2(1 <sup>+</sup> )	5726.0	1.3
	14	$\eta(1295)^*$	0 <sup>+</sup> (0 <sup>+</sup> )	1294	4	66	$B_2^*(5747)^{+*}$	1/2(2 <sup>+</sup> )	5737.2	0.7
	15	$a_2(1320)$	1 <sup>-</sup> (2 <sup>+</sup> )	1318.3	0.5	67	$B_2^*(5747)^{0***}$	1/2(2 <sup>+</sup> )	5739.5	0.7
		$\pi(1400)$	1 <sup>-</sup> (1 <sup>-</sup> )	1354	25	68	$B_J(5970)^+$	1/1(??)**	5964	5
	16	$\eta(1405)$	0 <sup>+</sup> (0 <sup>-</sup> )	1408.8	1.8	69	$B_J(5970)^{0***}$	1/1(??)**	5971	5
	17	$f_1(1420)$	0 <sup>+</sup> (1 <sup>+</sup> )	1426.4	0.9	7	bottom	strange	mesons	
	18	$\eta(1475)^*$	0 <sup>+</sup> (0 <sup>+</sup> )	1476	4	70	$B_s^0$	0(0 <sup>-</sup> )	5366.89	
		$a_0(1450)^{**}$	1 <sup>-</sup> (0 <sup>+</sup> )	1474	19	71	$B_s^{**}$	0(1 <sup>-</sup> )	5415.4	1.5
	19	$f_0(1500)^*$	0 <sup>+</sup> (0 <sup>+</sup> )	1504	6	72	$B_{s1}(5830)^0$	0(1 <sup>+</sup> )	5828.63	
	20	$f_2'(1525)^*$	0 <sup>+</sup> (2 <sup>+</sup> )	1525	5	73	$B_{s2}^*(5640)^0$	0(2 <sup>+</sup> )	5839.85	
	21	$\pi_1(1600)^*$	1 <sup>-</sup> (1 <sup>+</sup> )	1662	8	8	bottom	charmed	mesons	
	22	$\eta_2(1645)^*$	0 <sup>+</sup> (2 <sup>+</sup> )	1617	5	74	$B_c^{**}$	0(0 <sup>-</sup> )	6274.9	1.0
	23	$\omega_3(1670)^*$	0 <sup>-</sup> (3 <sup>-</sup> )	1667	4	9	$c\bar{c}$	mesons		
	24	$\pi_2(1670)$	1 <sup>-</sup> (2 <sup>+</sup> )	1672.2	3.0	75	$\eta_c(1S)$	0 <sup>+</sup> (0 <sup>+</sup> )	2983.4	0.5
	25	$\rho_3(1690)$	1 <sup>+</sup> (3 <sup>-</sup> )	1688.8	2.1	76	$J/\psi(1S)$	0 <sup>-</sup> (1 <sup>-</sup> )	3096.90	
		$\rho(1700)$	1 <sup>+</sup> (1 <sup>-</sup> )	1720	20	77	$\chi_{c0}(1P)$	0 <sup>+</sup> (0 <sup>+</sup> )	3414.75	
	26	$f_0(1710)^*$	0 <sup>+</sup> (0 <sup>+</sup> )	1723	6	78	$\chi_{c1}(1P)$	0 <sup>+</sup> (1 <sup>+</sup> )	3510.66	
	27	$\phi(1800)^{**}$	1 <sup>-</sup> (0 <sup>+</sup> )	1812	12	79	$h_c(1P)$	??(1 <sup>+</sup> )	3525.38	
	28	$\phi_3(1850)^*$	0 <sup>-</sup> (3 <sup>-</sup> )	1854	7	80	$\chi_{c2}(1P)$	0 <sup>+</sup> (2 <sup>+</sup> )	3556.20	
	29	$\pi_2(1880)^{**}$	1 <sup>-</sup> (2 <sup>+</sup> )	1895	16	81	$\eta_c(2S)$	0 <sup>+</sup> (0 <sup>+</sup> )	3639.2	1.2
	30	$f_2(1950)^{**}$	0 <sup>+</sup> (2 <sup>+</sup> )	1944	12	82	$\psi(2S)$	0 <sup>-</sup> (1 <sup>-</sup> )	3686.10	
	31	$a_4(2040)^*$	1 <sup>-</sup> (4 <sup>+</sup> )	1995	8	83	$\psi(3770)$	0 <sup>-</sup> (1 <sup>-</sup> )	3773.13	
	32	$f_2(2050)^{**}$	0 <sup>+</sup> (4 <sup>+</sup> )	2018	11	84	$\psi(3823)$	??(2 <sup>-</sup> )	3822.2	1.2
	33	$\psi(2170)^{**}$	0 <sup>-</sup> (1 <sup>-</sup> )	2188	10	85	$X(3872)$	0 <sup>+</sup> (1 <sup>+</sup> )	3871.69	
3		strange	mesons			86	$X(3900)$	1 <sup>+</sup> (1 <sup>+</sup> )	3886.6	2.4
	34	$K^{\pm}$	1/2(0 <sup>-</sup> )	493.677		87	$X(3915)$	0 <sup>+</sup> (?++)	3918.4	1.9
	35	$K^{0***}$	1/2(0 <sup>-</sup> )	497.01	0.013	88	$\chi_{c2}(1P)$	0 <sup>+</sup> (2 <sup>+</sup> )	3927.2	2.6
	36	$K^*(892)^{\pm}$	1/2(1 <sup>-</sup> )	891.76	0.29	89	$X(4020)$	1(??)	4024.1	1.9
	37	$K^*(892)^{0***}$	1/2(1 <sup>-</sup> )	895.85	0.20	90	$\psi(4040)^*$	0 <sup>-</sup> (1 <sup>-</sup> )	4039	1
	38	$K_1(1270)^*$	1/2(1 <sup>+</sup> )	1272	7	91	$X(4140)$	0 <sup>+</sup> (?1 <sup>+</sup> )	4146.8	3.1
	39	$K_1(1400)^*$	1/2(1 <sup>+</sup> )	1403	7	92	$\psi(4160)^*$	0 <sup>-</sup> (1 <sup>-</sup> )	4191	5
	40	$K^*(1410)^*$	1/2(1 <sup>-</sup> )	1421	9	93	$X(4260)^*$	??(1 <sup>-</sup> )	4230	8
	41	$K_2^*(1430)^{\pm}$	1/2(2 <sup>+</sup> )	1425.6	1.5	94	$X(4360)^*$	??(1 <sup>-</sup> )	4341	8
	42	$K_2^*(1430)^{0***}$	1/2(2 <sup>+</sup> )	1432.4	1.3	95	$\psi(4415)^*$	0 <sup>-</sup> (1 <sup>-</sup> )	4421	4
		$K^*(1680)^{**}$	1/2(1 <sup>-</sup> )	1718	18	96	$X(4430)^{**}$	??(1 <sup>+</sup> )	4418	15
	43	$K_2(1770)^*$	1/2(2 <sup>-</sup> )	1773	8	97	$X(4660)^*$	??(1 <sup>-</sup> )	4643	9
	44	$K_3^*(1780)^*$	1/2(3 <sup>-</sup> )	1776	7	10	$b\bar{b}$	mesons		
	45	$K_2^*(1820)^{**}$	1/2(2 <sup>-</sup> )	1819	12	98	$\eta_b(1S)$	0 <sup>+</sup> (0 <sup>+</sup> )	9399.0	2.3
	46	$K_4^*(2045)^*$	1/2(4 <sup>+</sup> )	2045	9	99	$\Upsilon(1S)$	0 <sup>-</sup> (1 <sup>-</sup> )	9460.30	
4		charmed	mesons			100	$\chi_{b0}(1P)$	0 <sup>+</sup> (0 <sup>+</sup> )	9859.44	
	47	$D^0$	1/2(0 <sup>-</sup> )	1864.83		101	$\chi_{b1}(1P)$	0 <sup>+</sup> (0 <sup>+</sup> )	9892.78	
	48	$D^{\pm}$	1/2(0 <sup>-</sup> )	1869.59	0.20	102	$h_b(1P)$	??(1 <sup>+</sup> )	9899.3	0.8
	49	$D^*(2007)^{0***}$	1/2(1 <sup>-</sup> )	2006.85		103	$\chi_{b2}(1P)$	0 <sup>+</sup> (2 <sup>+</sup> )	9912.21	
	50	$D^*(2010)^{\pm}$	1/2(1 <sup>-</sup> )	2010.28		104	$\Upsilon(2S)$	0 <sup>-</sup> (1 <sup>-</sup> )	10023.26	
	51	$D_1(2420)^0$	1/2(1 <sup>+</sup> )	2420.8	0.5	105	$\Upsilon(1D)$	0 <sup>-</sup> (2 <sup>-</sup> )	10163.7	1.4
	52	$D_2^*(2460)^{0***}$	1/2(2 <sup>+</sup> )	2460.7	0.4	106	$\chi_{b0}(2P)$	0 <sup>+</sup> (0 <sup>+</sup> )	10232.5	0.4

Table 7. Continued.

	Particle	$m_i$	$\Delta$		Particle	$m_i$	$\Delta$
107	$\chi_{b1}(2P)$	$0^+(1^{++})$	10255.46	143	$\Sigma_c(2520)^{++***}$	$1(3/2^+)$	2518.41
108	$\chi_{b2}(2P)$	$0^-(2^{+-})$	10268.65	144	$\Sigma_c(2520)^{+***}$	$1(3/2^+)$	2517.5 2.3
109	$\Upsilon(3S)$	$0^-(1^{--})$	10355.2 0.5	145	$\Sigma_c(2520)^\circ$	$1(3/2^+)$	2518.48
110	$\chi_{b1}(3P)$	$0^+(1^{++})$	10512.1 2.3	146	$\Sigma_c(2800)^{++***}$	$1(3/2^+)$	2801 6
111	$\Upsilon(4S)$	$0^-(1^{--})$	10579.4 1.2	147	$\Sigma_c(2800)^{+**}$	$1(3/2^+)$	2792 14
112	$X(10610)^\pm$	$1^+(1^+)$	10607.2 2.0	148	$\Sigma_c(2800)^\circ*$	$1(3/2^+)$	2806 7
113	$X(10610)^\circ$	$1^+(1^+)$	10609 6	149	$\Xi_c^{+***}$	$1/2(1/2^+)$	2467.87
114	$\Upsilon(10860)$	$0^-(1^{--})$	10889.9 3.2	150	$\Xi_c^\circ$	$1/2(1/2^+)$	2470.87
115	$\Upsilon(11020)^*$	$0^-(1^{--})$	10993 10	151	$\Xi_c'^{+***}$	$1/2(1/2^+)$	2577.4 1.2
11	baryons			152	$\Xi_c^\circ$	$1/2(1/2^+)$	2577.8 0.3
116	$p^{***}$	$1/2(1/2^+)$	938.2721	153	$\Xi_c(2645)^{+***}$	$1/2(3/2^+)$	2645.53
117	$n$	$1/2(1/2^+)$	939.5654	154	$\Xi_c(2645)^\circ$	$1/2(3/2^+)$	2646.32
118	$\Lambda$	$0(1/2^+)$	1115.683	155	$\Xi_c(2790)^{+***}$	$1/2(1/2^-)$	2792.0 0.5
119	$\Lambda(1405)1/2^-*$	$0(1/2^-)$	1405.1 1.3	156	$\Xi_c(2790)^\circ$	$1/2(1/2^-)$	2792.8 1.2
120	$\Lambda(1520)3/2^-*$	$0(3/2^-)$	1519.5 1.0	157	$\Xi_c(2815)^{+***}$	$1/2(3/2^-)$	2816.67 0.31
121	$\Sigma^{+***}$	$1(1/2^+)$	1189.37 0.07	158	$\Xi_c(2815)^\circ$	$1/2(3/2^-)$	2820.22 0.32
122	$\Sigma^\circ$	$1(1/2^+)$	1192.642	159	$\Xi_c(2970)^{+***}$	$1/2(?)^?$	2969.4 0.8
123	$\Sigma^{-***}$	$1(1/2^+)$	1197.45 0.03	160	$\Xi_c(2970)^\circ$	$1/2(?)^?$	2967.8 0.8
124	$\Sigma(1385)^{+***}$	$1(3/2^+)$	1382.80 0.35	161	$\Xi_c(3055)$	$1/2(?)^?$	3055.9 0.4
125	$\Sigma(1385)^\circ$	$1(3/2^+)$	1383.7 1.0	162	$\Xi_c(3080)^{+***}$	$1/2(?)^?$	3077.2 0.4
126	$\Sigma(1385)^{-***}$	$1(3/2^+)$	1387.2 0.5	163	$\Xi_c(3080)^\circ$	$1/2(?)^?$	3079.9 1.4
127	$\Xi^\circ$	$1/2(1/2^+)$	1314.86 0.20	164	$\Omega_c^\circ$	$0(1/2^+)$	2695.2 1.7
128	$\Xi^-$	$1/2(1/2^+)$	1321.71 0.07	165	$\Omega_c(2770)^\circ$	$0(3/2^+)$	2765.9 2.0
129	$\Xi(1530)3/2^{\circ+}$	$1/2(3/2^+)$	1531.80	13	bottom baryons		
130	$\Xi(1530)3/2^{-***}$	$1/2(3/2^+)$	1535.0	166	$\Lambda_b^\circ$	$0(1/2^+)$	5619.58
131	$\Xi(1820)3/2^-*$	$1/2(3/2^-)$	1823 5	167	$\Lambda_b(5912)^\circ$	$0(1/2^-)$	5912.18 0.21
132	$\Xi(2030)^*$	$1/2(\geq 3/2^?)$	2025 5	168	$\Lambda_b(5920)^\circ$	$0(3/2^-)$	5919.90 0.19
133	$\Omega^-$	$0(3/2^+)$	1673.45	169	$\Sigma_b^{+*}$	$1(1/2^+)$	5811.3 1.9
134	$\Omega(2250)^{-**}$	$0(?)^?$	2252 9	170	$\Sigma_b^{-***}$	$1(1/2^+)$	5815.5 1.8
12	charmed baryons			171	$\Sigma_b^{*+*}$	$1(3/2^+)$	5832.1 1.9
135	$\Lambda_c^+$	$0(1/2^+)$	2286.46	172	$\Sigma_b^{*-***}$	$1(3/2^+)$	5835.1 1.9
136	$\Lambda_c(2595)^+$	$0(1/2^-)$	2592.25	173	$\Xi_b^{-***}$	$1/2(1/2^+)$	5794.5 1.4
137	$\Lambda_c(2625)^+$	$0(3/2^-)$	2628.11	174	$\Xi_b^\circ$	$1/2(1/2^+)$	5791.9 0.5
138	$\Lambda_c(2880)^+$	$0(5/2^+)$	2881.53	175	$\Xi_b'(5935)^-$	$1/2(1/2^+)$	5935.02
139	$\Lambda_c(2940)^*$	$0(5/2^+)$	2939.3 1.5	176	$\Xi_b(5945)^\circ$	$1/2(3/2^+)$	5949.8 1.4
140	$\Sigma_c(2455)^{+***}$	$1(1/2^+)$	2453.97	177	$\Xi_b^*(5955)^-$	$1/2(1/2^+)$	5955.33
141	$\Sigma_c(2455)^{+***}$	$1(1/2^+)$	2452.9 0.4	178	$\Omega_b^-$	$0(3/2^+)$	6046.1 1.9
142	$\Sigma_c(2455)^\circ$	$1(1/2^+)$	2453.75				

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